

Analysis of Horizontal Shear Data,

J. K., Lewis

A. D. Kirwan

MEES DOCUMENT IS BEST QUALITY PRACTICADIC WHE COPY PUBNISHED TO DDC CONTAINED A FIGNIFICANT NUMBER OF PAGES WHICH DO NOT 'MPRODUCE LEGIBLY.

Final Report for contract NØ0014-81-C-2102

Date: 1981/

JUL 2 1 1981

DISTRIBUTION STATEMENT A

Approved for public release; Distribution Unlimited

Bryan, TX

090

Analysis of Horizontal Shear Data,

J. K., Lewis

A. D. Kirwan

MEES DOCUMENT IS BEST QUALITY PRACTICADIC WHE COPY PUBNISHED TO DDC CONTAINED A FIGNIFICANT NUMBER OF PAGES WHICH DO NOT 'MPRODUCE LEGIBLY.

Final Report for contract NØ0014-81-C-2102

Date: 1981/

JUL 2 1 1981

DISTRIBUTION STATEMENT A

Approved for public release; Distribution Unlimited

Bryan, TX

090

# **DISCLAIMER NOTICE**

THIS DOCUMENT IS BEST QUALITY PRACTICABLE. THE COPY FURNISHED TO DTIC CONTAINED A SIGNIFICANT NUMBER OF PAGES WHICH DO NOT REPRODUCE LEGIBLY.

# **DISCLAIMER NOTICE**

THIS DOCUMENT IS BEST QUALITY PRACTICABLE. THE COPY FURNISHED TO DTIC CONTAINED A SIGNIFICANT NUMBER OF PAGES WHICH DO NOT REPRODUCE LEGIBLY.

## Table of Contents

1.	Introduction		1
2.	Background		3
	2.1	Theoretical Basis of Analysis	3
	2.2	Analysis Procedures	7
	2.3	Sources of Errors in Data	8
3.	Critique of Data		
	3.1	General Considerations	10
	3.2	Discussion of Trajectories	11
4.	Data	Analysis	12
	4.1	Shear and Normal Deformation Rates - Large-Scale	
		Cluster	12
	4.2	Shear and Normal Deformation Rates - Small-Scale	
		Cluster	13
	4.3	Vorticity Balance - Large-Scale Cluster	13
	4.4	Vorticity and Divergence rates - Small-Scale Cluster	26
	4.5	Assessment of Interpolation Procedure	26
5.	Conc	Conclusions and Recommendations	
6.	References		63
	Appendices		
	A Program Listing		A-1
	В 0	utput from Production Runs	B-1



## Table of Contents

1.	Introduction		1
2.	Background		3
	2.1	Theoretical Basis of Analysis	3
	2.2	Analysis Procedures	7
	2.3	Sources of Errors in Data	8
3.	Critique of Data		
	3.1	General Considerations	10
	3.2	Discussion of Trajectories	11
4.	Data	Analysis	12
	4.1	Shear and Normal Deformation Rates - Large-Scale	
		Cluster	12
	4.2	Shear and Normal Deformation Rates - Small-Scale	
		Cluster	13
	4.3	Vorticity Balance - Large-Scale Cluster	13
	4.4	Vorticity and Divergence rates - Small-Scale Cluster	26
	4.5	Assessment of Interpolation Procedure	26
5.	Conc	Conclusions and Recommendations	
6.	References		63
	Appendices		
	A Program Listing		A-1
	В 0	utput from Production Runs	B-1



## Introduction

The purpose of this study was to assess the value of drifter data taken by NRL for determining horizontal shears in the ocean. \ In the course of the study, we have addressed two general issues. The first is an evaluation of shears from the smoothed data supplied by NRL along with an assessment of the significance of these evaluations. The other issue is a general assessment of the use of drifters for inferring horizontal shears.

There are a number of interrelated questions concerning these issues. The more saliment of these are: How representative of natural conditions is the smoothed data set? What effect does the smoothing procedure\have on the results? Is the theoretical basis of the analysis sound? What does the analysis tell us about physical processes occurring in the ocean? It appeared that three tasks were required to resolve these issues. These were:

(Task 1) Perform an analysis on drogues 1, 3, 5, 9, 16 and 20 to obtain the differential kinematic properties (shear deformation, normal deformation, vorticity, and horizontal divergence) in a geographic coordinate system (i.e. north and east components): These are presented in tables and accompanied by graphs of the functions versus time. Two clusters are analyzed. One was a small-scale cluster composed of drifters 1, 3 and 5. The other was a large-scale cluster composed of 1, 9 and 16. Perform the analysis as stated in Task 1 but with a coordinate /Task 2

system moving with the center of mass of the clusters. Both the

کے حربہ

## Introduction

The purpose of this study was to assess the value of drifter data taken by NRL for determining horizontal shears in the ocean. \ In the course of the study, we have addressed two general issues. The first is an evaluation of shears from the smoothed data supplied by NRL along with an assessment of the significance of these evaluations. The other issue is a general assessment of the use of drifters for inferring horizontal shears.

There are a number of interrelated questions concerning these issues. The more saliment of these are: How representative of natural conditions is the smoothed data set? What effect does the smoothing procedure\have on the results? Is the theoretical basis of the analysis sound? What does the analysis tell us about physical processes occurring in the ocean? It appeared that three tasks were required to resolve these issues. These were:

(Task 1) Perform an analysis on drogues 1, 3, 5, 9, 16 and 20 to obtain the differential kinematic properties (shear deformation, normal deformation, vorticity, and horizontal divergence) in a geographic coordinate system (i.e. north and east components): These are presented in tables and accompanied by graphs of the functions versus time. Two clusters are analyzed. One was a small-scale cluster composed of drifters 1, 3 and 5. The other was a large-scale cluster composed of 1, 9 and 16. Perform the analysis as stated in Task 1 but with a coordinate /Task 2

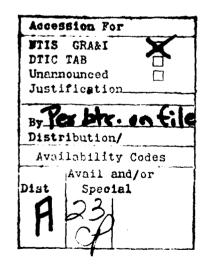
system moving with the center of mass of the clusters. Both the -

کے حربہ

large and small scale clusters were analyzed. The results are presented in tables and accompanied by graphs of the functions versus time;

Task 3) Make a qualitative assessment of the calculation and the effect of turbulent processes.

Each of these task was accomplished and the results are described in the following sections.



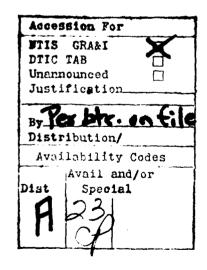




large and small scale clusters were analyzed. The results are presented in tables and accompanied by graphs of the functions versus time;

Task 3) Make a qualitative assessment of the calculation and the effect of turbulent processes.

Each of these task was accomplished and the results are described in the following sections.







## 2. Background

2.1 Theoretical Basis of Analysis.

The raw data obtained from drifters are estimates of position at discreet times. If a cluster of drifters are located within a small parcel of the ocean, then a Taylor's expansion yields for the velocity of the  $i^{th}$  drifter (Molinari and Kirwan (1975), Okubo and Ebbesmeyer (1976))

$$U_{i} = U + g_{i} + [(D+N)X_{i}]/2 + [(S-\zeta)Y_{i}]/2$$

$$V_{i} = V + h_{i} + [(S+\zeta)X_{i}]/2 + [(D-N)Y_{i}]/2$$

$$i = 1, ..., n.$$
(1)

The U and V are the components of the velocity of the center of mass of the parcel; the coordinates with respect to the cluster center of mass of drifter i are  $X_i$  and  $Y_i$ ; and  $g_i$  and  $h_i$  represent the sum of the higher order nonlinear terms in the expansion. From the experimental standpoint, these terms also include measurement errors and, perhaps, random turbulent motion. In these equations, the velocity gradients across the parcel have been expressed in terms of the elementary differential kinematic properties (DKP):

D=au/ax+av/ay (divergence) z=av/ax-au/ay (vorticity)

 $S=\partial V/\partial X+\partial U/\partial Y$  (shearing deformation rate)

 $N=\partial u/\partial x-\partial v/\partial y$  (normal or stretching deformation rate)

Kirwan (1975) has provided physical interpretations of these quantities. The horizontal divergence D is a measure of the parcel area change without change of orientation or shape. The vorticity is  $\zeta$  and is a measure of the orientation change without area or shape change of the parcel. Shape

## 2. Background

2.1 Theoretical Basis of Analysis.

The raw data obtained from drifters are estimates of position at discreet times. If a cluster of drifters are located within a small parcel of the ocean, then a Taylor's expansion yields for the velocity of the  $i^{th}$  drifter (Molinari and Kirwan (1975), Okubo and Ebbesmeyer (1976))

$$U_{i} = U + g_{i} + [(D+N)X_{i}]/2 + [(S-\zeta)Y_{i}]/2$$

$$V_{i} = V + h_{i} + [(S+\zeta)X_{i}]/2 + [(D-N)Y_{i}]/2$$

$$i = 1, ..., n.$$
(1)

The U and V are the components of the velocity of the center of mass of the parcel; the coordinates with respect to the cluster center of mass of drifter i are  $X_i$  and  $Y_i$ ; and  $g_i$  and  $h_i$  represent the sum of the higher order nonlinear terms in the expansion. From the experimental standpoint, these terms also include measurement errors and, perhaps, random turbulent motion. In these equations, the velocity gradients across the parcel have been expressed in terms of the elementary differential kinematic properties (DKP):

D=au/ax+av/ay (divergence) z=av/ax-au/ay (vorticity)

 $S=\partial V/\partial X+\partial U/\partial Y$  (shearing deformation rate)

 $N=\partial u/\partial x-\partial v/\partial y$  (normal or stretching deformation rate)

Kirwan (1975) has provided physical interpretations of these quantities. The horizontal divergence D is a measure of the parcel area change without change of orientation or shape. The vorticity is  $\zeta$  and is a measure of the orientation change without area or shape change of the parcel. Shape

changes without change of area or orientation are given by S and N respectively. The former is for the shape change produced by differential motions parallel to the boundaries, while the latter is for motions normal to the boundaries.

The physical picture given by the model equations is that an individual drifter's velocity is composed of the mean translatory velocity of the parcel, plus a velocity induced by the rotation, divergence, and distortion of the parcel, plus a random or turbulent velocity. The mean parcel velocity is attributed to large-scale (relative to cluster size) motions, the induced velocity to cluster-scale motions, and the random component to the small-scale turbulent field. The scale of these latter motions is assumed to be much less than that of the cluster.

Of course, the DKP in (1) vary as a function of time. However, the analysis procedure (described below) requires that their time scales of variation be larger than that of the velocities. At this time there is no way of establishing that this is true for the ocean. In practice, one makes fixes as often as possible and hopes for the best. Otherwise it would be necessary to incorporate the method of stationary phase in the analysis. Such an effort is not justified under the goals of the study.

In (1) the velocity for the  $i^{th}$  drifter was calculated by taking centered differences of the smoothed position data:

$$U_{i}(t) = [x_{i}(t+\Delta t) - x_{i}(t-\Delta t)]/2\Delta t$$

$$V_{i}(t) = [y_{i}(t+\Delta t) - y_{i}(t-\Delta t)]/2\Delta t$$
(2)



changes without change of area or orientation are given by S and N respectively. The former is for the shape change produced by differential motions parallel to the boundaries, while the latter is for motions normal to the boundaries.

The physical picture given by the model equations is that an individual drifter's velocity is composed of the mean translatory velocity of the parcel, plus a velocity induced by the rotation, divergence, and distortion of the parcel, plus a random or turbulent velocity. The mean parcel velocity is attributed to large-scale (relative to cluster size) motions, the induced velocity to cluster-scale motions, and the random component to the small-scale turbulent field. The scale of these latter motions is assumed to be much less than that of the cluster.

Of course, the DKP in (1) vary as a function of time. However, the analysis procedure (described below) requires that their time scales of variation be larger than that of the velocities. At this time there is no way of establishing that this is true for the ocean. In practice, one makes fixes as often as possible and hopes for the best. Otherwise it would be necessary to incorporate the method of stationary phase in the analysis. Such an effort is not justified under the goals of the study.

In (1) the velocity for the  $i^{th}$  drifter was calculated by taking centered differences of the smoothed position data:

$$U_{i}(t) = [x_{i}(t+\Delta t) - x_{i}(t-\Delta t)]/2\Delta t$$

$$V_{i}(t) = [y_{i}(t+\Delta t) - y_{i}(t-\Delta t)]/2\Delta t$$
(2)



Also, the average velocity components were calculated from

$$U = \left( \begin{array}{cc} \mathbf{\hat{\Sigma}} & U_{\mathbf{i}} \right) / n$$

$$V = \left( \begin{array}{cc} \mathbf{\hat{\Sigma}} & V_{\mathbf{i}} \right) / n$$

$$(3)$$

where n is the total number of drifters. Finally, the drifter positions with respect to the center of the cluster or crigin for (1) is

$$X_{i} = X_{i} - \sum_{i} X_{i} / n$$

$$Y_{i} = y_{i} - \sum_{i} Y_{i} / n$$
(4)

Thus, in (1), U, V,  $U_i$ ,  $V_i$ ,  $X_i$  and  $Y_i$  are known from measurements at each discreet time. The DKP can be calculated by minimizing the residual kinetic energy term E  $\equiv \sum_{i=1}^{n} (g_i^2 + h_i^2)/2$  (5)

This, however, is not a standard least squares problem since there may be measurement errors in both the velocities and the positions. Moreover, depending upon the analysis procedure, the position and velocity errors may be correlated (Kirwan and Chang, 1979).

Let us see how these errors may affect the analysis. First we express the observed positions as sums of the true values and random errors (for least squares, errors in the velocities can be incorporated in  $g_1$  and  $h_4$ ). We can write

$$X_{i}/2 = \widehat{X}_{i} + \alpha_{i}$$

$$Y_{i}/2 = \widehat{Y}_{i} + \beta_{i}$$
(6)

where

 $(\widetilde{\chi}_{1}, \widetilde{\gamma}_{1}) = \frac{1}{2}$  true position values,  $(\alpha_{1}, \beta_{1}) = \frac{1}{2}$  random errors.



Also, the average velocity components were calculated from

$$U = \left( \begin{array}{cc} \mathbf{\hat{\Sigma}} & U_{\mathbf{i}} \right) / n$$

$$V = \left( \begin{array}{cc} \mathbf{\hat{\Sigma}} & V_{\mathbf{i}} \right) / n$$

$$(3)$$

where n is the total number of drifters. Finally, the drifter positions with respect to the center of the cluster or crigin for (1) is

$$X_{i} = X_{i} - \sum_{i} X_{i} / n$$

$$Y_{i} = y_{i} - \sum_{i} Y_{i} / n$$
(4)

Thus, in (1), U, V,  $U_i$ ,  $V_i$ ,  $X_i$  and  $Y_i$  are known from measurements at each discreet time. The DKP can be calculated by minimizing the residual kinetic energy term E  $\equiv \sum_{i=1}^{n} (g_i^2 + h_i^2)/2$  (5)

This, however, is not a standard least squares problem since there may be measurement errors in both the velocities and the positions. Moreover, depending upon the analysis procedure, the position and velocity errors may be correlated (Kirwan and Chang, 1979).

Let us see how these errors may affect the analysis. First we express the observed positions as sums of the true values and random errors (for least squares, errors in the velocities can be incorporated in  $g_1$  and  $h_4$ ). We can write

$$X_{i}/2 = \widehat{X}_{i} + \alpha_{i}$$

$$Y_{i}/2 = \widehat{Y}_{i} + \beta_{i}$$
(6)

where

 $(\widetilde{\chi}_{1}, \widetilde{\gamma}_{1}) = \frac{1}{2}$  true position values,  $(\alpha_{1}, \beta_{1}) = \frac{1}{2}$  random errors.



Next, substitute (6) into (1) to obtain

$$u_{\underline{i}} = (D+N) (\widetilde{X}_{\underline{i}} + \alpha_{\underline{i}}) + (S-\zeta) (\widetilde{Y}_{\underline{i}} + \beta_{\underline{i}}) + g_{\underline{i}}$$

$$v_{\underline{i}} = (S+\zeta) (\widetilde{X}_{\underline{i}} + \alpha_{\underline{i}}) + (D-N) (\widetilde{Y}_{\underline{i}} + \beta_{\underline{i}}) + h_{\underline{i}}$$
(7)

where

$$u_{i} = U_{i} - U$$

$$v_{i} = V_{i} - V$$

are the drifter velocity components with respect to the center of mass of the cluster. The least squares equations for the DKP give.

$$\frac{D+N}{2} = \left| \frac{(\overline{ux} + \sigma_{ux})}{(\overline{uy} + \sigma_{uy})} \frac{(\overline{xy} + \sigma_{xy})}{(\overline{y^2} + \sigma_{y}^2)} \right| / \Delta$$

$$\frac{S-\zeta}{2} = \left| \frac{(\overline{x^2} + \sigma_{xy}^2)}{(\overline{xy} + \sigma_{xy})} \frac{(\overline{ux} + \sigma_{ux})}{(\overline{uy} + \sigma_{uy})} \right| / \Delta$$
(8)

$$\frac{S+\zeta}{2} = \begin{vmatrix} (\overline{vx} + \sigma_{vx}) & (\overline{xy} + \sigma_{xy}) \\ (\overline{vy} + \sigma_{vy}) & (\overline{y}^2 + \sigma_y^2) \end{vmatrix} / \Delta$$

$$\frac{D-N}{2} = \left| (\overline{x^2} + \sigma_X^2) (\overline{vx} + \sigma_{vx}) \right| / \Delta.$$

Here

$$\Delta = \begin{vmatrix} (\overline{x^2} + \sigma_X^2) & (\overline{xy} + \sigma_{Xy}) \\ (\overline{xy} + \sigma_{Xy}) & (\overline{y^2} + \sigma_y^2) \end{vmatrix} \text{ and }$$



Next, substitute (6) into (1) to obtain

$$u_{\underline{i}} = (D+N) (\widetilde{X}_{\underline{i}} + \alpha_{\underline{i}}) + (S-\zeta) (\widetilde{Y}_{\underline{i}} + \beta_{\underline{i}}) + g_{\underline{i}}$$

$$v_{\underline{i}} = (S+\zeta) (\widetilde{X}_{\underline{i}} + \alpha_{\underline{i}}) + (D-N) (\widetilde{Y}_{\underline{i}} + \beta_{\underline{i}}) + h_{\underline{i}}$$
(7)

where

$$u_{i} = U_{i} - U$$

$$v_{i} = V_{i} - V$$

are the drifter velocity components with respect to the center of mass of the cluster. The least squares equations for the DKP give.

$$\frac{D+N}{2} = \left| \frac{(\overline{ux} + \sigma_{ux})}{(\overline{uy} + \sigma_{uy})} \frac{(\overline{xy} + \sigma_{xy})}{(\overline{y^2} + \sigma_{y}^2)} \right| / \Delta$$

$$\frac{S-\zeta}{2} = \left| \frac{(\overline{x^2} + \sigma_{xy}^2)}{(\overline{xy} + \sigma_{xy})} \frac{(\overline{ux} + \sigma_{ux})}{(\overline{uy} + \sigma_{uy})} \right| / \Delta$$
(8)

$$\frac{S+\zeta}{2} = \begin{vmatrix} (\overline{vx} + \sigma_{vx}) & (\overline{xy} + \sigma_{xy}) \\ (\overline{vy} + \sigma_{vy}) & (\overline{y}^2 + \sigma_y^2) \end{vmatrix} / \Delta$$

$$\frac{D-N}{2} = \left| (\overline{x^2} + \sigma_X^2) (\overline{vx} + \sigma_{vx}) \right| / \Delta.$$

Here

$$\Delta = \begin{vmatrix} (\overline{x^2} + \sigma_X^2) & (\overline{xy} + \sigma_{Xy}) \\ (\overline{xy} + \sigma_{Xy}) & (\overline{y^2} + \sigma_y^2) \end{vmatrix} \text{ and }$$



 $\overline{ux}$ ,  $\overline{uy}$ ,  $\overline{vx}$ ,  $\overline{vy}$ ,  $\overline{x^2}$ ,  $\overline{y^2}$ , and  $\overline{xy}$  are estimates from the observations of the true values of the appropriate correlations. The  $\sigma$ 's are variances and covariances of the measurement errors in these estimates. (Equations (8) correct algebraic mistakes in Kirwan and Chang, 1979).

Several points should be noted about (8). First, if  $\alpha_1 \equiv \beta_1 \equiv 0$  (i.e. the position measurements are exact), then the equations reduce to the usual normal equations for multivariate least squares. Second, if the position errors are known but are uncorrelated with the velocity errors, then the estimates of the DKP provided by (8) will be less than the theoretic estimate given by

$$\frac{D+N}{2} = \left| \begin{array}{cc} \overline{ux} & \overline{xy} \\ \overline{uy} & \overline{y^2} \end{array} \right| \left| \left( \overline{x^2} \ \overline{y^2} - \overline{xy^2} \right) \right|$$

etc. However, this bias is easily removed by subtracting the known position error statistics from estimates of  $\frac{1}{x^2}$ ,  $\frac{1}{y^2}$  and  $\frac{1}{xy}$  obtained from the data.

In principle, unbiased estimates of the DKP may be obtained in the general case by correcting the velocity-position correlations for correlations of their errors. Unfortunately, these correlations are much harder to determine than the position error correlation matrix. Moreover, if the velocities are constructed from smoothed trajectories, the smoothing procedure may introduce a substantial correlation between the velocities and positions.

#### 2.2 Analysis Procedures

The comments above emphasize the importance of proper planning of the data analysis. They suggest a data analysis flow diagram of the form

 $\overline{ux}$ ,  $\overline{uy}$ ,  $\overline{vx}$ ,  $\overline{vy}$ ,  $\overline{x^2}$ ,  $\overline{y^2}$ , and  $\overline{xy}$  are estimates from the observations of the true values of the appropriate correlations. The  $\sigma$ 's are variances and covariances of the measurement errors in these estimates. (Equations (8) correct algebraic mistakes in Kirwan and Chang, 1979).

Several points should be noted about (8). First, if  $\alpha_1 \equiv \beta_1 \equiv 0$  (i.e. the position measurements are exact), then the equations reduce to the usual normal equations for multivariate least squares. Second, if the position errors are known but are uncorrelated with the velocity errors, then the estimates of the DKP provided by (8) will be less than the theoretic estimate given by

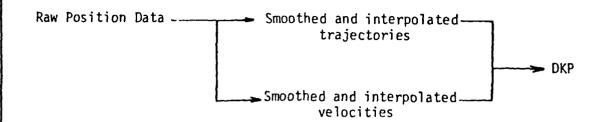
$$\frac{D+N}{2} = \left| \begin{array}{cc} \overline{ux} & \overline{xy} \\ \overline{uy} & \overline{y^2} \end{array} \right| \left| \left( \overline{x^2} \ \overline{y^2} - \overline{xy^2} \right) \right|$$

etc. However, this bias is easily removed by subtracting the known position error statistics from estimates of  $\frac{1}{x^2}$ ,  $\frac{1}{y^2}$  and  $\frac{1}{xy}$  obtained from the data.

In principle, unbiased estimates of the DKP may be obtained in the general case by correcting the velocity-position correlations for correlations of their errors. Unfortunately, these correlations are much harder to determine than the position error correlation matrix. Moreover, if the velocities are constructed from smoothed trajectories, the smoothing procedure may introduce a substantial correlation between the velocities and positions.

#### 2.2 Analysis Procedures

The comments above emphasize the importance of proper planning of the data analysis. They suggest a data analysis flow diagram of the form



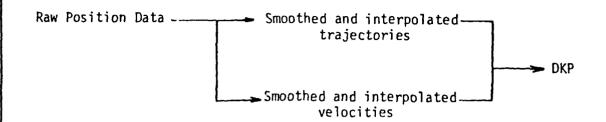
Unfortunately, the usual procedure is to process the data in series rather than parallel. Thus velocities are normally not obtained directly from the raw position data but from smoothed and interpolated trajectories.

Our experience has shown that the effects of the procedure of serially processing data are two-fold. The first is that it may alter to a varying degree the magnitude of the elements of the velocity-position error correlation matrix

But the more serious effect is that it can produce long term trends in the matrix elements. This can hamper quantitative interpretations of the results in terms of physical mechanisms operating in the ocean. It is less likely that this would have as much an effect on qualitative studies such as establishing orders of magnitude of the DKP.

#### 2.3 Sources of Error in Data

There are three potential sources of error in the data supplied to SAI by NRL. These are position errors, windage errors, and bias produced by the smoothing operator. NRL personnel (T. Gordon) has indicated that at-sea tests of the position fixing system suggest that the most probable position error is  $\frac{1}{2}$  350 m and that there is negligible correlation between north and east measurements.



Unfortunately, the usual procedure is to process the data in series rather than parallel. Thus velocities are normally not obtained directly from the raw position data but from smoothed and interpolated trajectories.

Our experience has shown that the effects of the procedure of serially processing data are two-fold. The first is that it may alter to a varying degree the magnitude of the elements of the velocity-position error correlation matrix

But the more serious effect is that it can produce long term trends in the matrix elements. This can hamper quantitative interpretations of the results in terms of physical mechanisms operating in the ocean. It is less likely that this would have as much an effect on qualitative studies such as establishing orders of magnitude of the DKP.

#### 2.3 Sources of Error in Data

There are three potential sources of error in the data supplied to SAI by NRL. These are position errors, windage errors, and bias produced by the smoothing operator. NRL personnel (T. Gordon) has indicated that at-sea tests of the position fixing system suggest that the most probable position error is  $\frac{1}{2}$  350 m and that there is negligible correlation between north and east measurements.

For this study, we have taken the most probable error as the rms error. In fact, this is probably an over-estimate since the smoothing routine will tend to reduce random position errors.

The windage problem was investigated by the procedures suggested by Kirwan et al. (1975). For the wind conditions encountered in this experiment and the type of buoy used, it was established that the windage effect was negligible.

From the data supplied, it was not possible to establish the effect of the smoothing operator on velocity errors or on the correlation of velocity and position errors. Despite this, it is felt that the data is sufficient to meet the objectives of the study.



For this study, we have taken the most probable error as the rms error. In fact, this is probably an over-estimate since the smoothing routine will tend to reduce random position errors.

The windage problem was investigated by the procedures suggested by Kirwan et al. (1975). For the wind conditions encountered in this experiment and the type of buoy used, it was established that the windage effect was negligible.

From the data supplied, it was not possible to establish the effect of the smoothing operator on velocity errors or on the correlation of velocity and position errors. Despite this, it is felt that the data is sufficient to meet the objectives of the study.



## 3. Critique of Data

#### 3.1 General Considerations

Before discussing the results of the analysis, it is useful to summarize the essential characteristics of the data. They have played a role in the design of our procedures.

Gordon (1980) has described the procedure for smoothing and interpolating the raw position data. On the average, raw position data were taken every 4 hours. These data were then fitted by least squares polynomials ranging in degree from 3 to 7. These polynomials were then evaluated at hourly intervals. These smoothed and interpolated positions were subjected to a number of analyses as described below.

It has been our experience that polynomial fits, especially if the degree is low relative to the number of data points, is a satisfactory procedure for smoothing trajectory data. It should be noted that other techniques are available which, in our view, are superior. A discussion of other such options is outside the scope of this work.

There are, however, two characteristics of the data which have limited our ability to interprete quantatively physical processes in the ocean. One of these is that a separate parallel analysis was not made for trajectories and velocities. Problems arising from this characteristic were discussed in section 2.2. The other problem is that the interpolation procedure provided approximately 4 times more data points than were observed. This means that the data points have a built-in correlation with a lag of about 4 hours. This effect was minimized by running a special analysis utilizing every fourth point. This procedure also should reduce some-

## 3. Critique of Data

#### 3.1 General Considerations

Before discussing the results of the analysis, it is useful to summarize the essential characteristics of the data. They have played a role in the design of our procedures.

Gordon (1980) has described the procedure for smoothing and interpolating the raw position data. On the average, raw position data were taken every 4 hours. These data were then fitted by least squares polynomials ranging in degree from 3 to 7. These polynomials were then evaluated at hourly intervals. These smoothed and interpolated positions were subjected to a number of analyses as described below.

It has been our experience that polynomial fits, especially if the degree is low relative to the number of data points, is a satisfactory procedure for smoothing trajectory data. It should be noted that other techniques are available which, in our view, are superior. A discussion of other such options is outside the scope of this work.

There are, however, two characteristics of the data which have limited our ability to interprete quantatively physical processes in the ocean. One of these is that a separate parallel analysis was not made for trajectories and velocities. Problems arising from this characteristic were discussed in section 2.2. The other problem is that the interpolation procedure provided approximately 4 times more data points than were observed. This means that the data points have a built-in correlation with a lag of about 4 hours. This effect was minimized by running a special analysis utilizing every fourth point. This procedure also should reduce some-

what the effect of correlations of velocity and position imposed by the fitting procedure. This reduction can not be quantified at this time.

## 3.2 Discussion of trajectories

Trajectories of 5 drifters were analyzed. Drifters 9, 16 and 1 comprised what is called here the large-scale cluster. Drifters 1, 3 and 5 comprised a very small scale cluster on the western edge of the large-scale cluster. Because of their proximity to drifter 1, drifters 5 and 3 provided very little kinematic information for the large-scale cluster. Thus, two separate analysis were conducted, one on the large-scale cluster and one on the small-scale cluster.

Data from drifter 20 was also available for the last few hours of the experiment. Unfortunately, it provided little new kinematic information since it stayed in a line with drifters 9 and 16.



what the effect of correlations of velocity and position imposed by the fitting procedure. This reduction can not be quantified at this time.

## 3.2 Discussion of trajectories

Trajectories of 5 drifters were analyzed. Drifters 9, 16 and 1 comprised what is called here the large-scale cluster. Drifters 1, 3 and 5 comprised a very small scale cluster on the western edge of the large-scale cluster. Because of their proximity to drifter 1, drifters 5 and 3 provided very little kinematic information for the large-scale cluster. Thus, two separate analysis were conducted, one on the large-scale cluster and one on the small-scale cluster.

Data from drifter 20 was also available for the last few hours of the experiment. Unfortunately, it provided little new kinematic information since it stayed in a line with drifters 9 and 16.



## 4. Data Analysis

of flow of the cluster center of mass.

A number of analyses and tests were performed on the large- and small-scale clusters. These were designed both to assess the quality of the data as well as to obtain the DKP. The following sub-sections discuss pertinent aspects of these analyses and the results.

4.1 Shear and Normal Deformation Rates - Large-Scale Cluster
First we shall discuss calculations of the shear and normal
deformation rates for the large-scale cluster. These calculations were
made for both a geographic coordinate system (north and east) and then
for a natural coordinate system oriented along and normal to the direction

The purpose of the latter calculations was to see if there was a preference for shear or normal deformation in a natural coordinate system. Specifically, this test was designed to address the hypothesis that the dominant horizontal velocity gradient along frontal zones is shear. The test was accomplished by transforming both shear and normal deformation to a coordinate system in which the y axis is oriented along the instantaneous direction of motion of the cluster and the x axis points to high pressure.

If  $\Theta$  is the angle between north and the direction of motion of the cluster, then the normal and shear deformation in the natural coordinate system can be found from

$$\overline{N} = \left[ N(V^2 - U^2) - 2SUV \right] / (U^2 + V^2)$$

$$\overline{S} = \left[ 2NUV + S(V^2 - U^2) \right] / (U^2 + V^2)$$
(9)

## 4. Data Analysis

of flow of the cluster center of mass.

A number of analyses and tests were performed on the large- and small-scale clusters. These were designed both to assess the quality of the data as well as to obtain the DKP. The following sub-sections discuss pertinent aspects of these analyses and the results.

4.1 Shear and Normal Deformation Rates - Large-Scale Cluster
First we shall discuss calculations of the shear and normal
deformation rates for the large-scale cluster. These calculations were
made for both a geographic coordinate system (north and east) and then
for a natural coordinate system oriented along and normal to the direction

The purpose of the latter calculations was to see if there was a preference for shear or normal deformation in a natural coordinate system. Specifically, this test was designed to address the hypothesis that the dominant horizontal velocity gradient along frontal zones is shear. The test was accomplished by transforming both shear and normal deformation to a coordinate system in which the y axis is oriented along the instantaneous direction of motion of the cluster and the x axis points to high pressure.

If  $\Theta$  is the angle between north and the direction of motion of the cluster, then the normal and shear deformation in the natural coordinate system can be found from

$$\overline{N} = \left[ N(V^2 - U^2) - 2SUV \right] / (U^2 + V^2)$$

$$\overline{S} = \left[ 2NUV + S(V^2 - U^2) \right] / (U^2 + V^2)$$
(9)

Here ⊖ is given by

$$\Theta = \tan^{-1} (U/V) + \pi/2$$
 (10)

In (9), the double angle, 20, trigonometric functions are expressed in terms of the velocity components (U,V) of the center of mass by use of (10).

The time histories of the shear and normal deformation rates are shown in Figs. la and 2a, respectively. Figs. lb and 2b give the deformation rates with respect to the natural coordinate system.

Since an estimate of the rms position error was provided by NRL, we were able to correct the deformation rates for this factor as suggested by Kirwan and Chang (1979). These corrected deformation rates are given in Figs. 3a and 4a, respectively. Figs. 3b and 4b give the corrected deformation rates with respect to a natural coordinate system.

4.2 Shear and Normal Deformation Rates - Small-Scale Cluster.

The shear and normal deformation rates were calculated for the small-scale cluster for a geographic coordinate system only. Figs. 5 and 6 show that the results of the calculations are quite noisy. This indication was supported by calculations of the deformation rates after the correction for the position error (Figs. 7 and 8). These latter two figures show that the correction has altered substantially the time histories of the deformation rates.

4.3 Vorticity Balance - Large-Scale Cluster

The vorticity and divergence were calculated for the largescale cluster, and a test was conducted to investigate the extent to which the vorticity equation, given below, is satisfied

$$\frac{d}{dt}$$
 ( $\zeta+f$ ) + ( $\zeta+f$ ) D = R



Here ⊖ is given by

$$\Theta = \tan^{-1} (U/V) + \pi/2$$
 (10)

In (9), the double angle, 20, trigonometric functions are expressed in terms of the velocity components (U,V) of the center of mass by use of (10).

The time histories of the shear and normal deformation rates are shown in Figs. la and 2a, respectively. Figs. lb and 2b give the deformation rates with respect to the natural coordinate system.

Since an estimate of the rms position error was provided by NRL, we were able to correct the deformation rates for this factor as suggested by Kirwan and Chang (1979). These corrected deformation rates are given in Figs. 3a and 4a, respectively. Figs. 3b and 4b give the corrected deformation rates with respect to a natural coordinate system.

4.2 Shear and Normal Deformation Rates - Small-Scale Cluster.

The shear and normal deformation rates were calculated for the small-scale cluster for a geographic coordinate system only. Figs. 5 and 6 show that the results of the calculations are quite noisy. This indication was supported by calculations of the deformation rates after the correction for the position error (Figs. 7 and 8). These latter two figures show that the correction has altered substantially the time histories of the deformation rates.

4.3 Vorticity Balance - Large-Scale Cluster

The vorticity and divergence were calculated for the largescale cluster, and a test was conducted to investigate the extent to which the vorticity equation, given below, is satisfied

$$\frac{d}{dt}$$
 ( $\zeta+f$ ) + ( $\zeta+f$ ) D = R



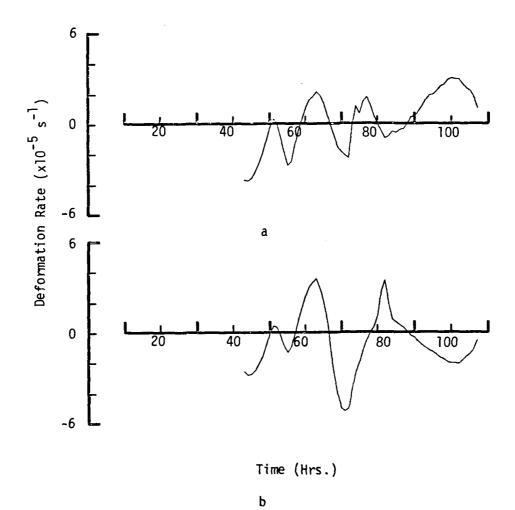


Fig. 1 Shear deformation rates for the large-scale cluster (without corrections for position errors). a is for a geographic coordinate system, and b is for a natural coordinate system.

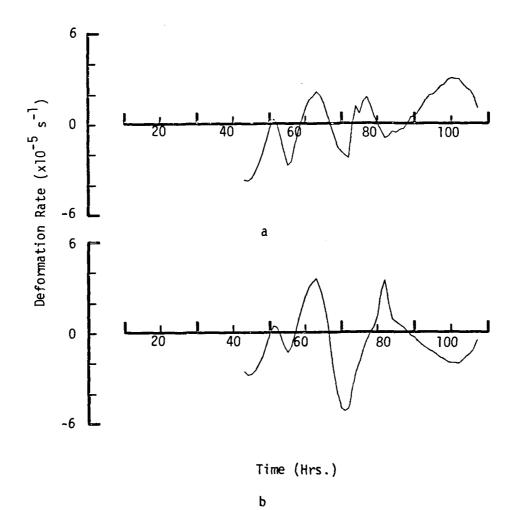


Fig. 1 Shear deformation rates for the large-scale cluster (without corrections for position errors). a is for a geographic coordinate system, and b is for a natural coordinate system.

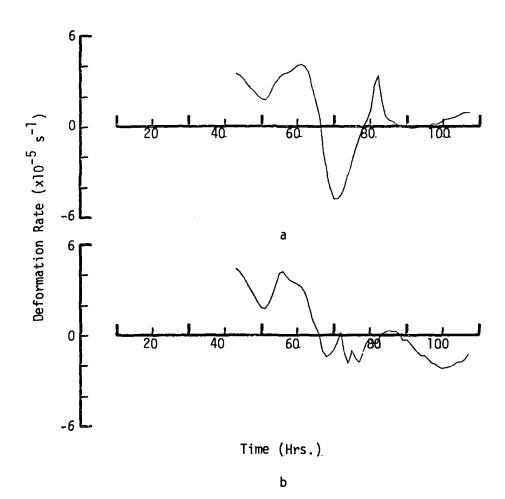


Fig. 2 Normal deformation rates for the large-scale cluster (without corrections for position errors). a is for a geographic coordinate system, and b is for a natural coordinate system.

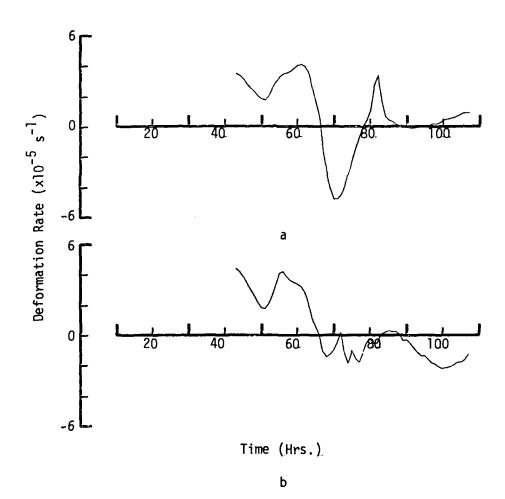


Fig. 2 Normal deformation rates for the large-scale cluster (without corrections for position errors). a is for a geographic coordinate system, and b is for a natural coordinate system.

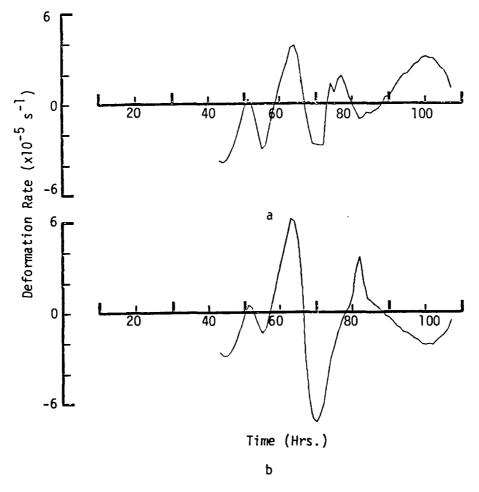


Fig. 3 Shear deformation rates for the large-scale cluster (with corrections for position errors). a is for a geographic coordinate system, and b is for a natural coordinate system.

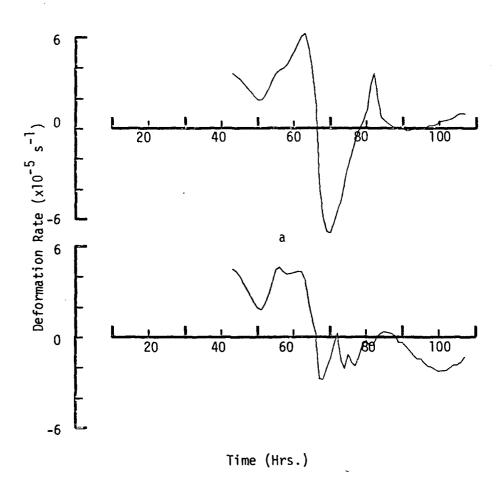
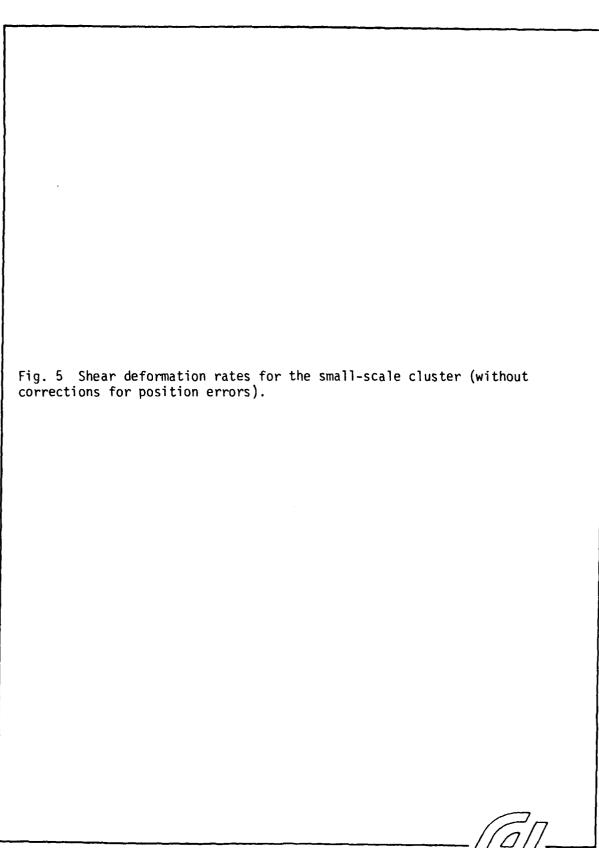


Fig. 4 Normal deformation rates for the large-scale cluster (with corrections for position errors). a is for a geographic coordinate system, and b is for a natural coordinate system.

b



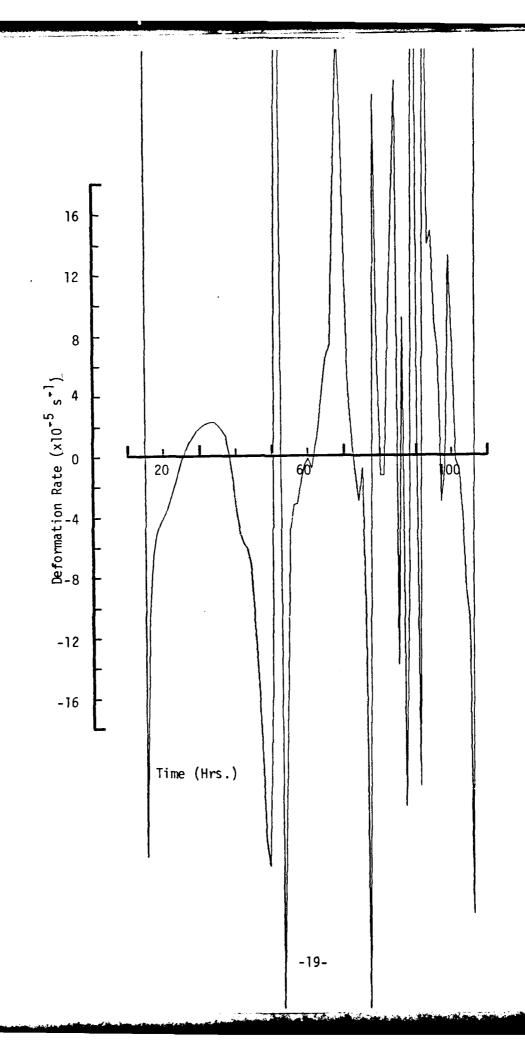
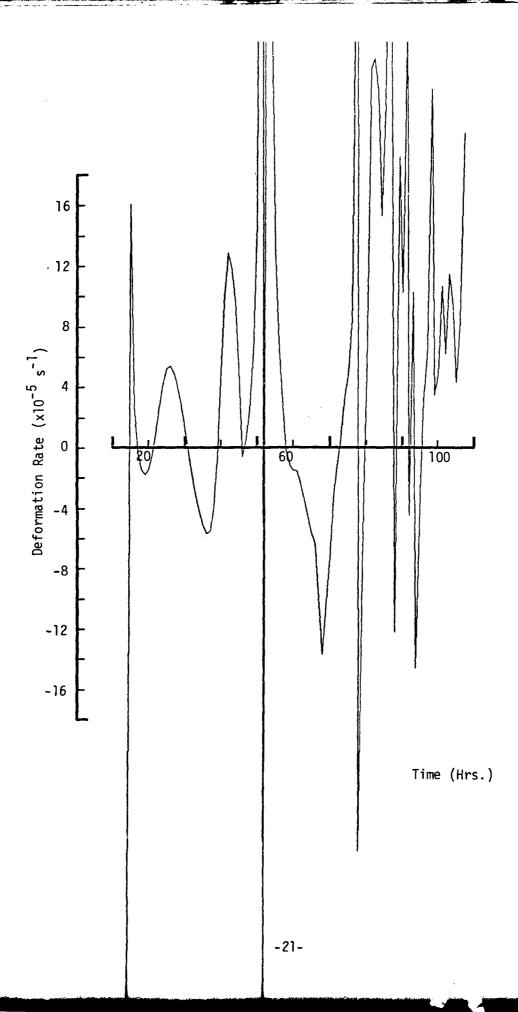
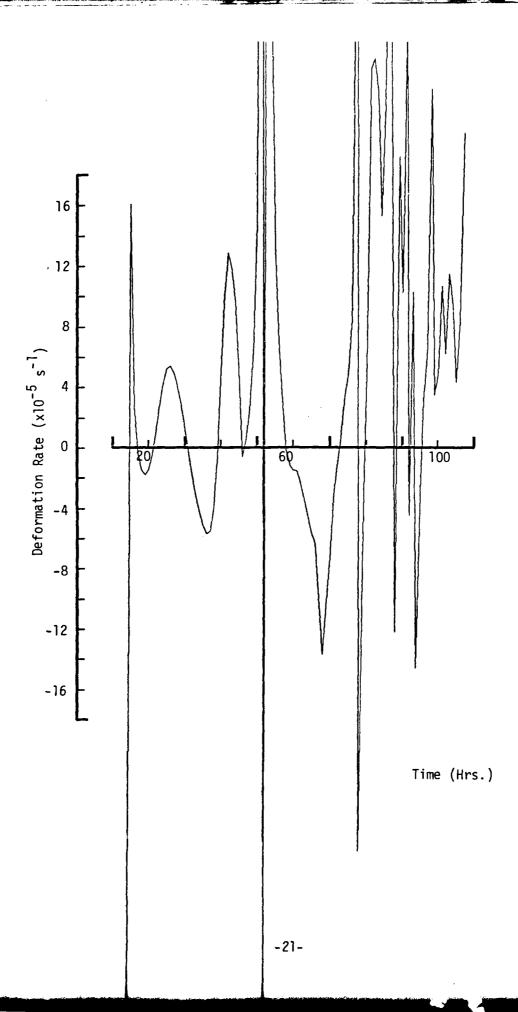
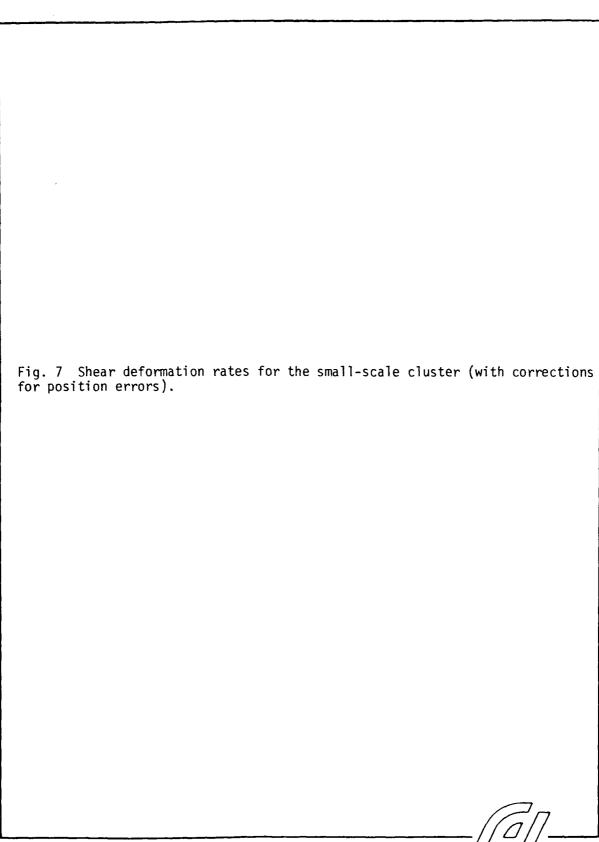


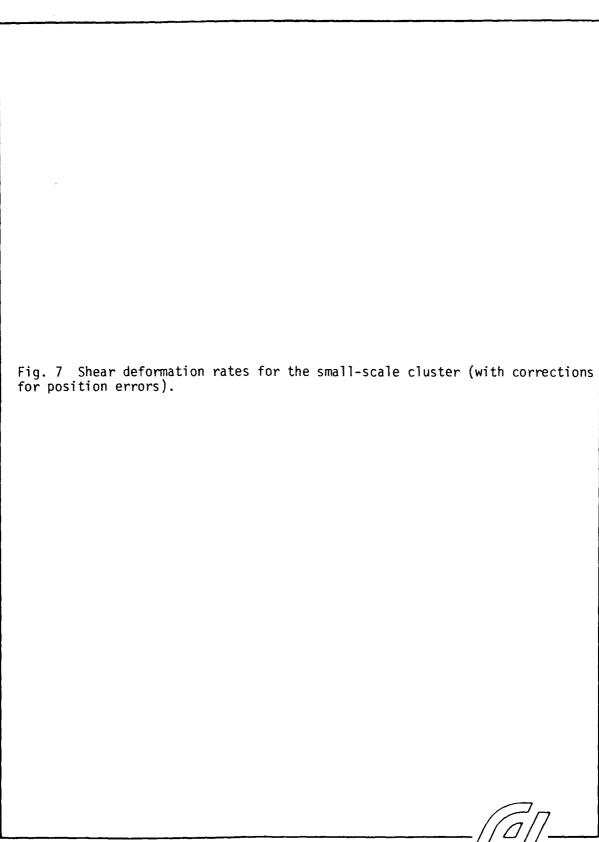
Fig. 6 Normal deformation rates for the small-scale cluster (without corrections for position errors).

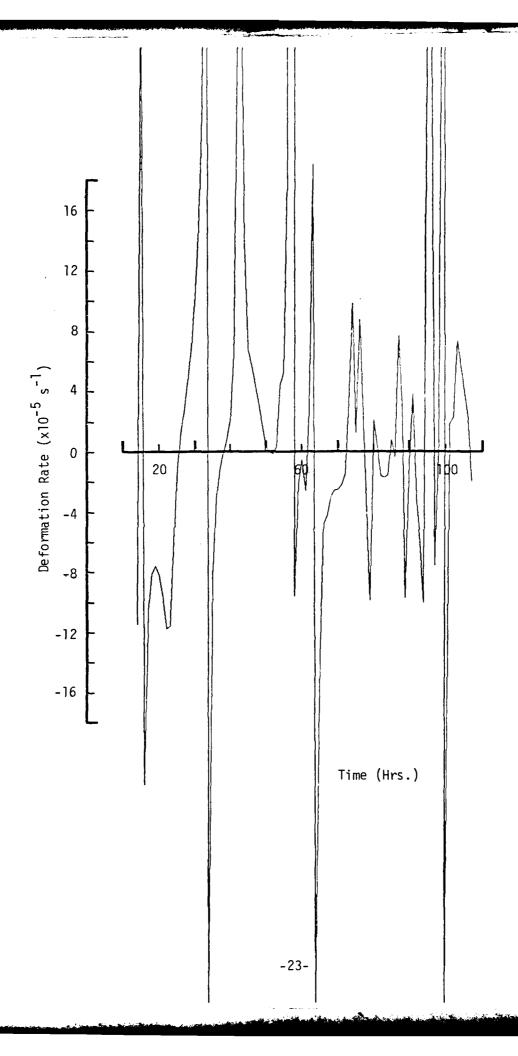
-20-

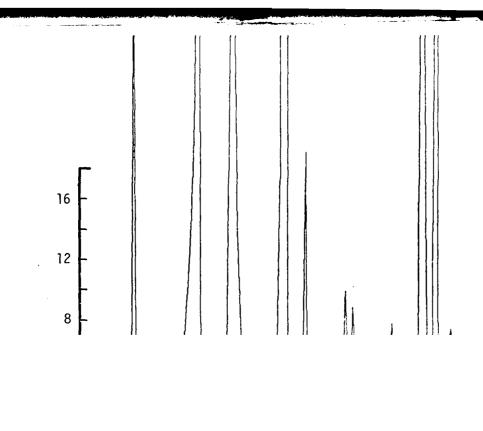


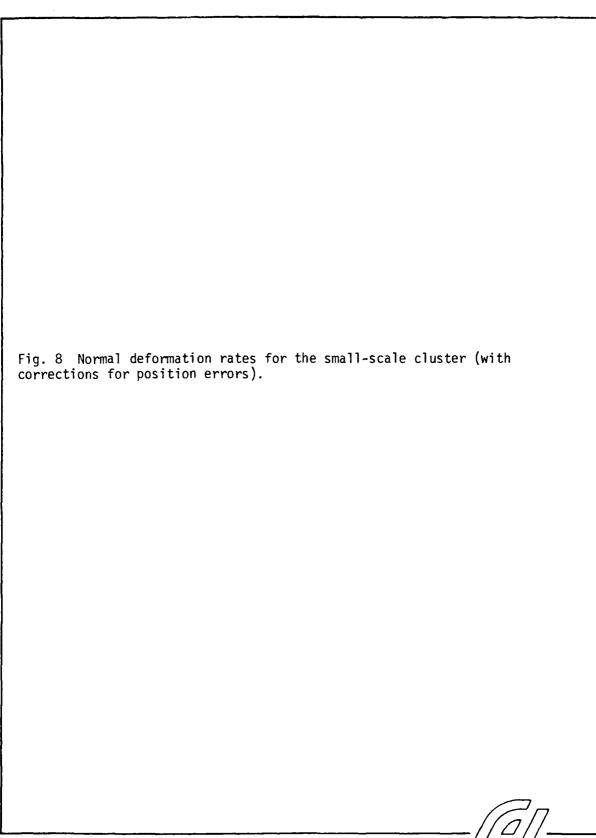


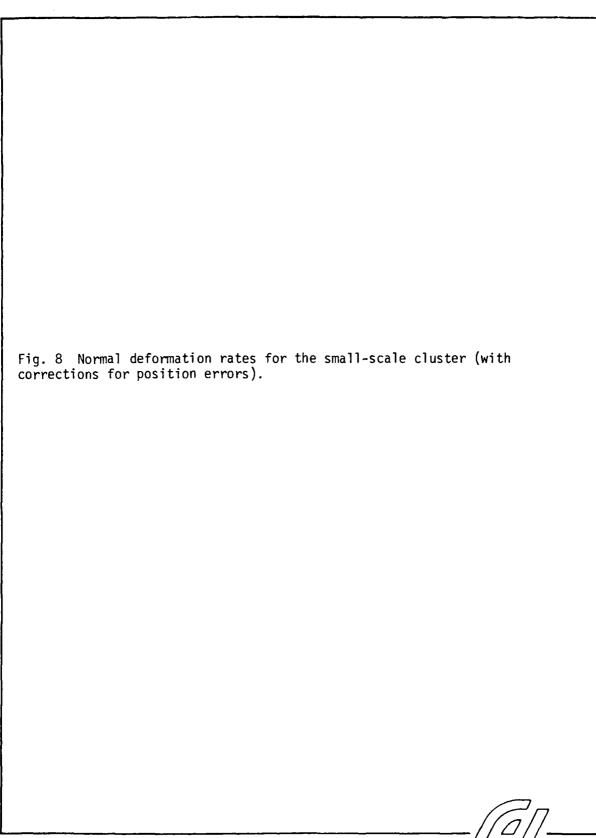


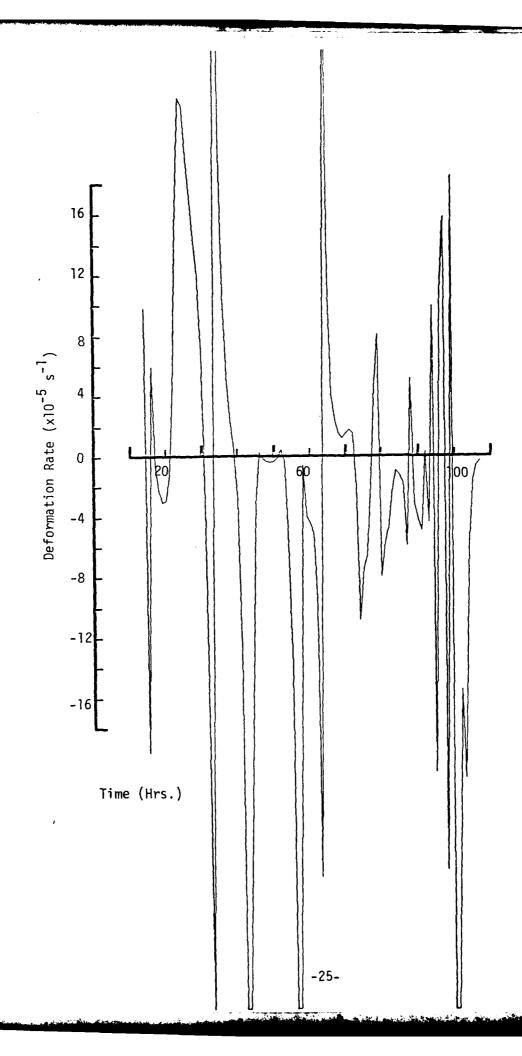


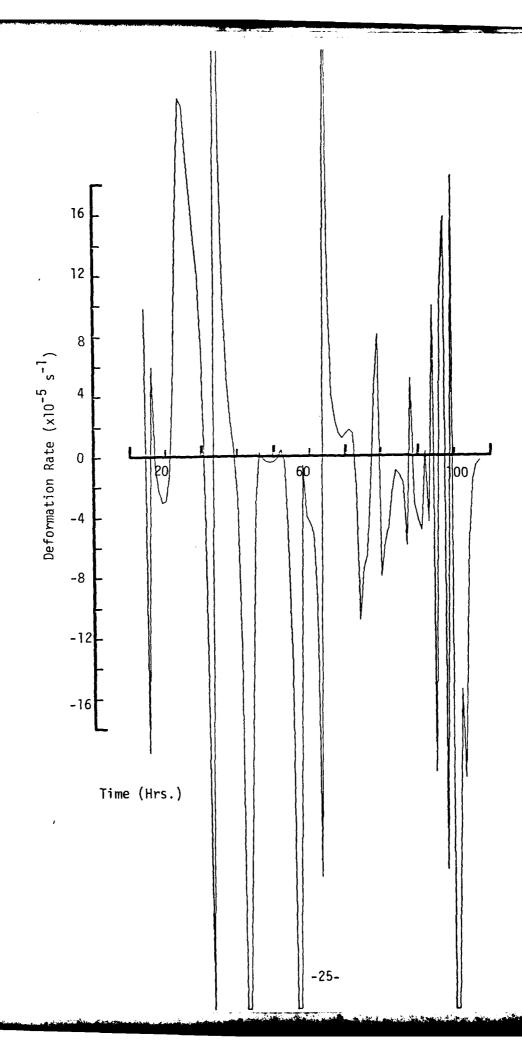












Here f is Coriolis, R represents friction, baroclinic torque and measurement errors. If the right hand side of (11) is smaller than the terms on the left hand side and often changes sign, then we conclude that the mixed layer exhibits a barotropic vorticity balance. This condition provides additional confidence in the data, but the non-existance of this condition is not sufficient evidence that the data is of poor quality.

Fig. 9 shows the time variations of divergence, vorticity, and the three components of the potential vorticity equation. The time derivative term in (11) is the lightest line in Fig. 9c while the second term on the left hand side is the next darker line. The R term in (11) is represented by the darkest line in Fig. 9c.

The time histories of vorticity, divergence, and the potential vorticity components also were calculated with the corrections for position errors. These corrected time histories are shown in Fig. 10.

4.4 Vorticity and Divergence Rates - Small-Scale Cluster

The vorticity and divergence rates were calculated for the small-scale cluster, and the results are shown in Figs. 11 and 12, respectively. The time histories that were corrected for position errors are shown in Figs. 13 (vorticity) and 14 (divergence). As with the shear and normal deformation rates, the values are quite noisy. Also, the position error corrections substantially alter the results.

4.5 Assessment of Interpolation Procedure

Since the interpolation procedure produced approximately

4 times more data than was observed, tests were conducted to determine

what effect the interpolation had on the character of the DKP. This was

done by repeating the calculations described in sections 4.1 through 4.4

but taking only every fourth data point.

Here f is Coriolis, R represents friction, baroclinic torque and measurement errors. If the right hand side of (11) is smaller than the terms on the left hand side and often changes sign, then we conclude that the mixed layer exhibits a barotropic vorticity balance. This condition provides additional confidence in the data, but the non-existance of this condition is not sufficient evidence that the data is of poor quality.

Fig. 9 shows the time variations of divergence, vorticity, and the three components of the potential vorticity equation. The time derivative term in (11) is the lightest line in Fig. 9c while the second term on the left hand side is the next darker line. The R term in (11) is represented by the darkest line in Fig. 9c.

The time histories of vorticity, divergence, and the potential vorticity components also were calculated with the corrections for position errors. These corrected time histories are shown in Fig. 10.

4.4 Vorticity and Divergence Rates - Small-Scale Cluster

The vorticity and divergence rates were calculated for the small-scale cluster, and the results are shown in Figs. 11 and 12, respectively. The time histories that were corrected for position errors are shown in Figs. 13 (vorticity) and 14 (divergence). As with the shear and normal deformation rates, the values are quite noisy. Also, the position error corrections substantially alter the results.

4.5 Assessment of Interpolation Procedure

Since the interpolation procedure produced approximately

4 times more data than was observed, tests were conducted to determine

what effect the interpolation had on the character of the DKP. This was

done by repeating the calculations described in sections 4.1 through 4.4

but taking only every fourth data point.

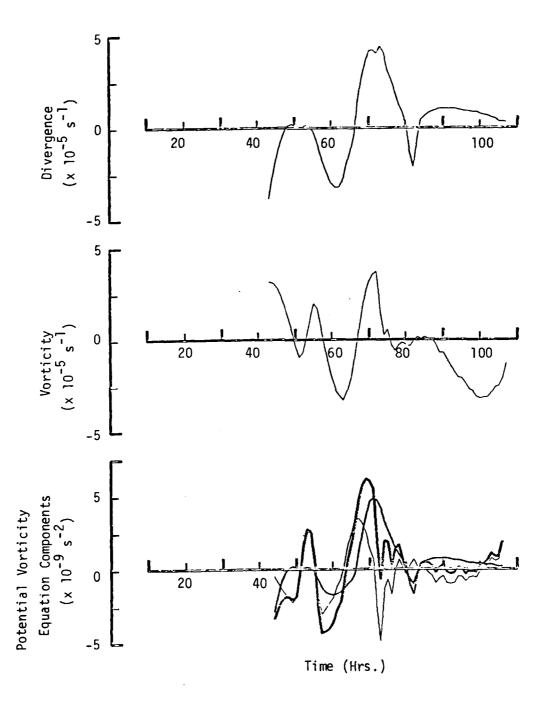


Fig. 9 Divergence, vorticity, and the potential vorticity equation components for the large-scale cluster (without corrections for position errors). For the equation components, the lightest line is the time derivative term, the medium line is the divergence-vorticity term, and the darkest line is the residual term.

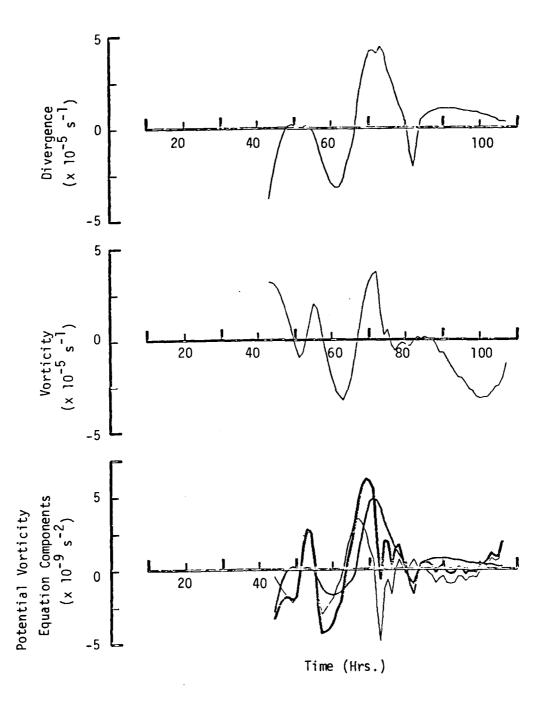


Fig. 9 Divergence, vorticity, and the potential vorticity equation components for the large-scale cluster (without corrections for position errors). For the equation components, the lightest line is the time derivative term, the medium line is the divergence-vorticity term, and the darkest line is the residual term.

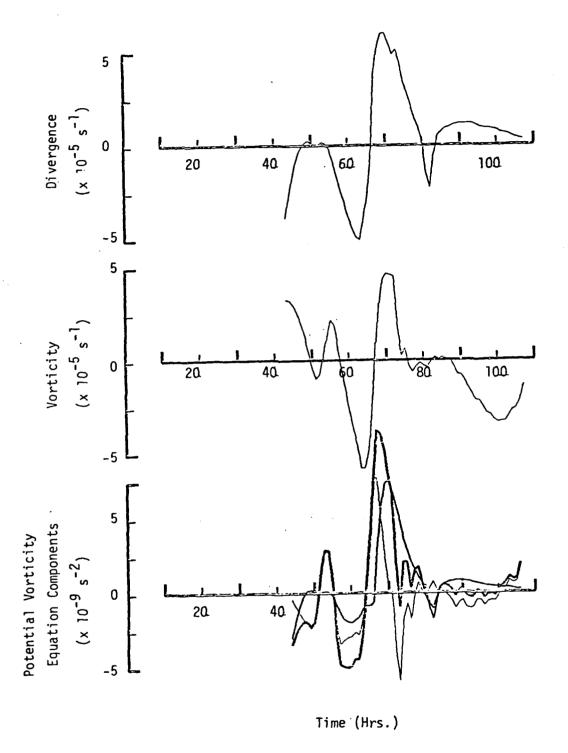


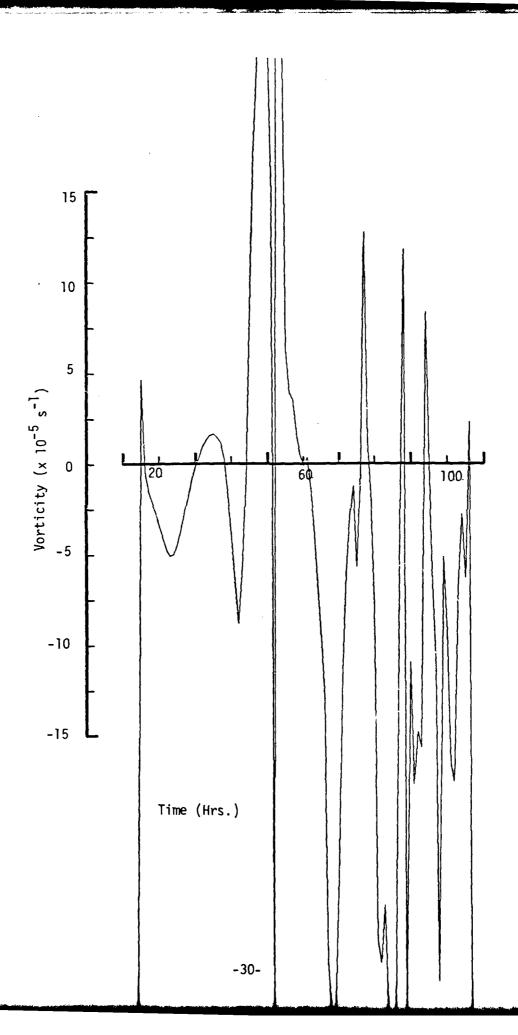
Fig. 10 Divergence, vorticity, and the potential vorticity equation components for the large-scale cluster (with corrections for position errors). For the equation components, the lightest line is the time derivative term, the medium line is the divergence-vorticity term, and the darkest line is the residual term.

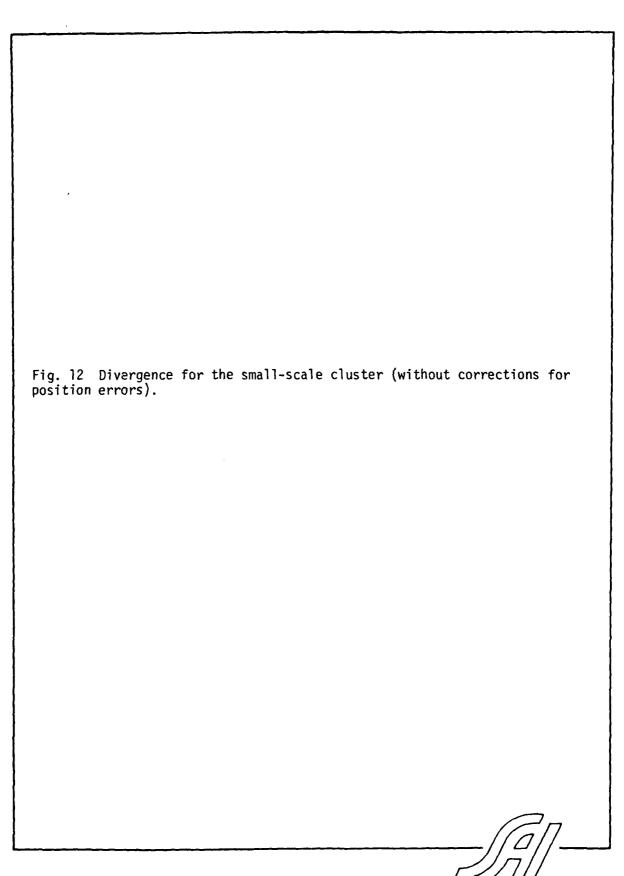
Fig. 11 Vorticity for the small-scale cluster (without corrections for position errors).

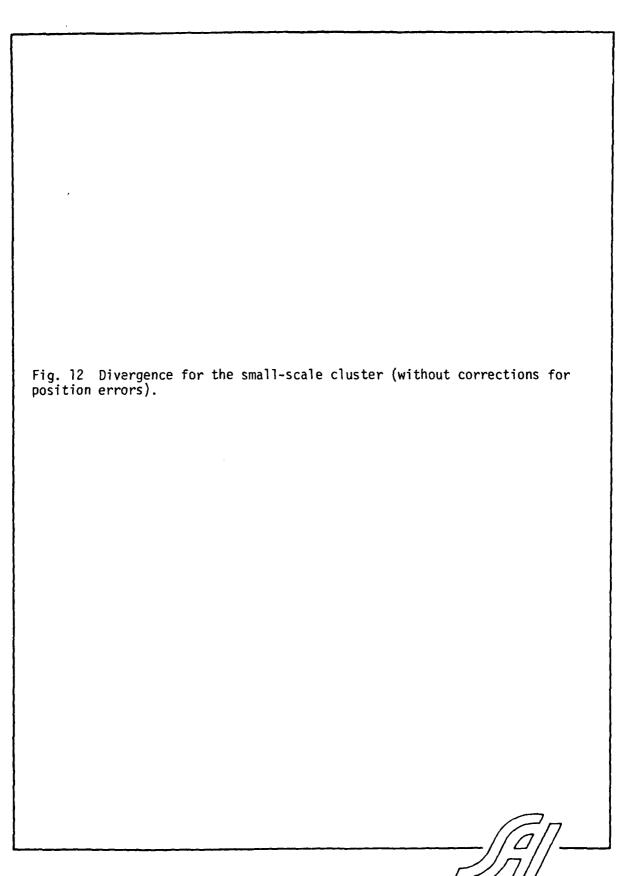
-29-

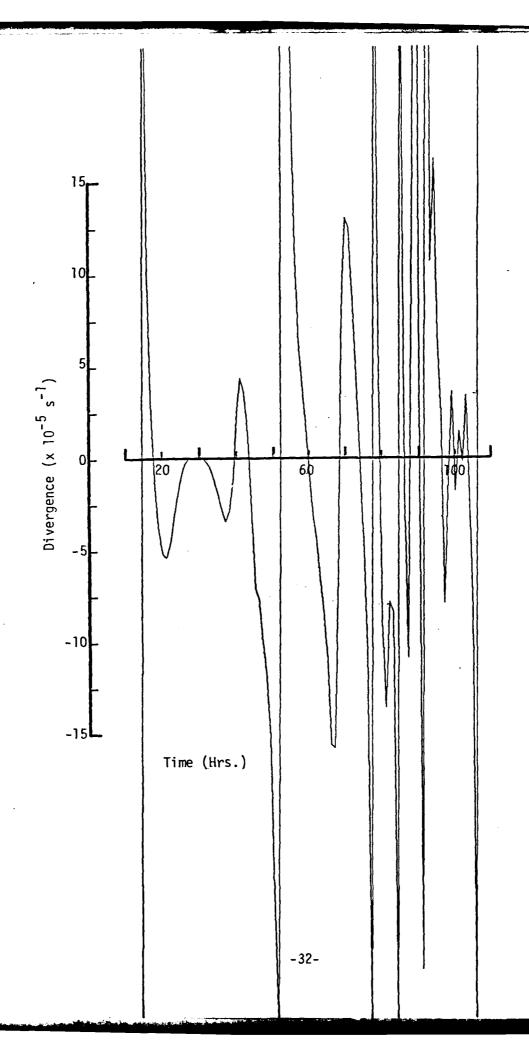
Fig. 11 Vorticity for the small-scale cluster (without corrections for position errors).

-29-









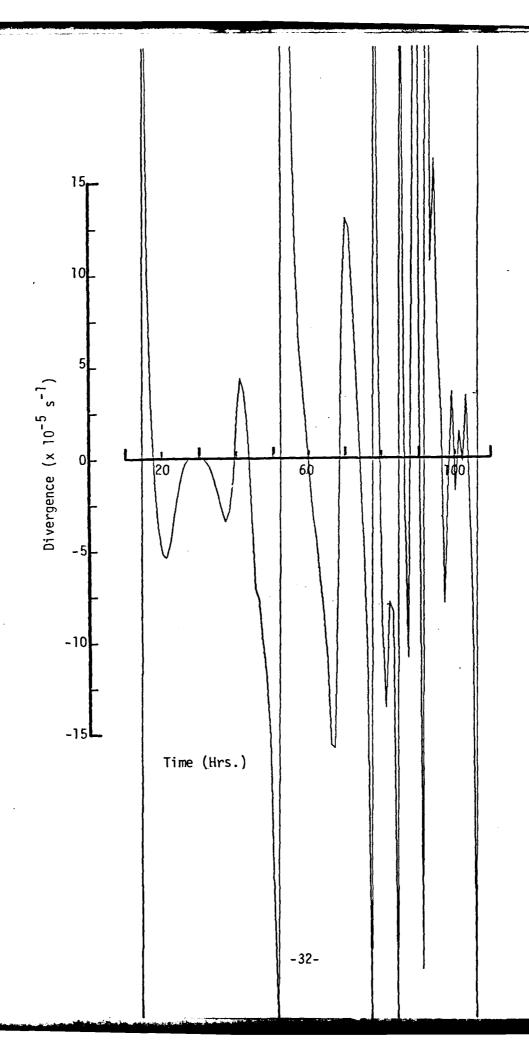
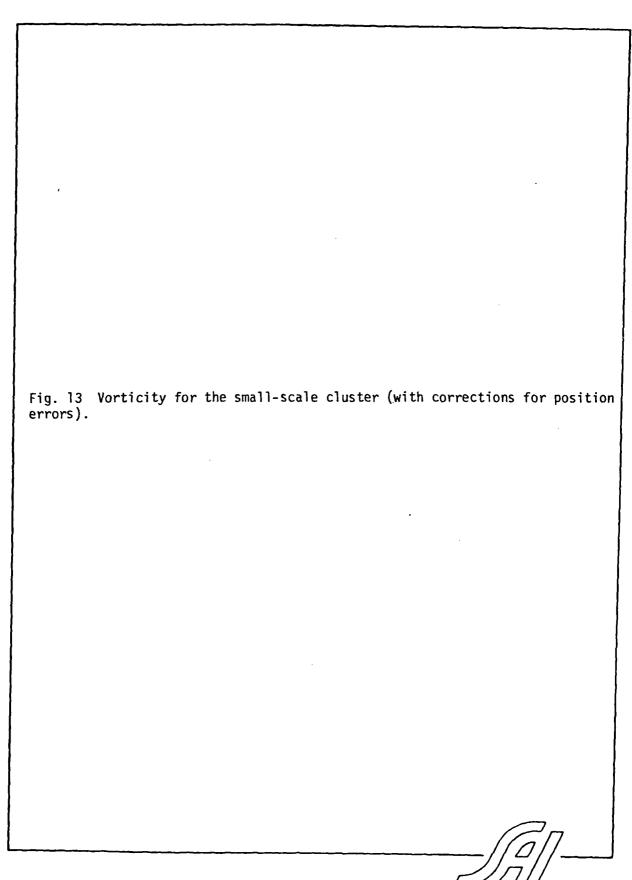
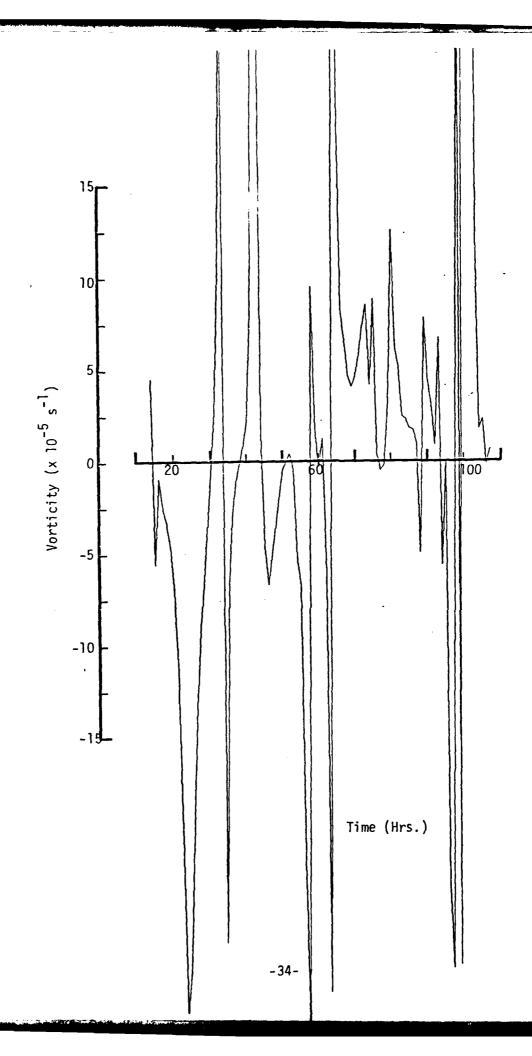
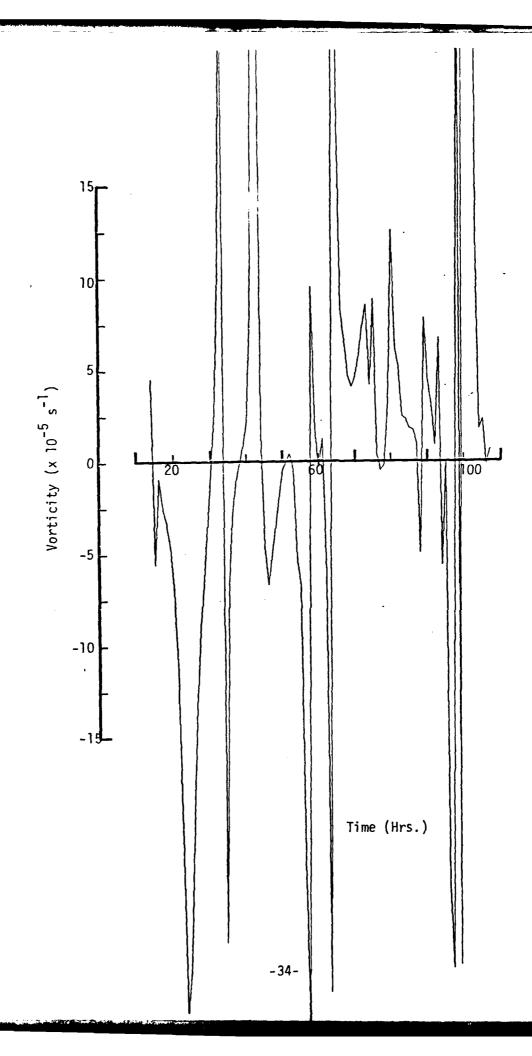
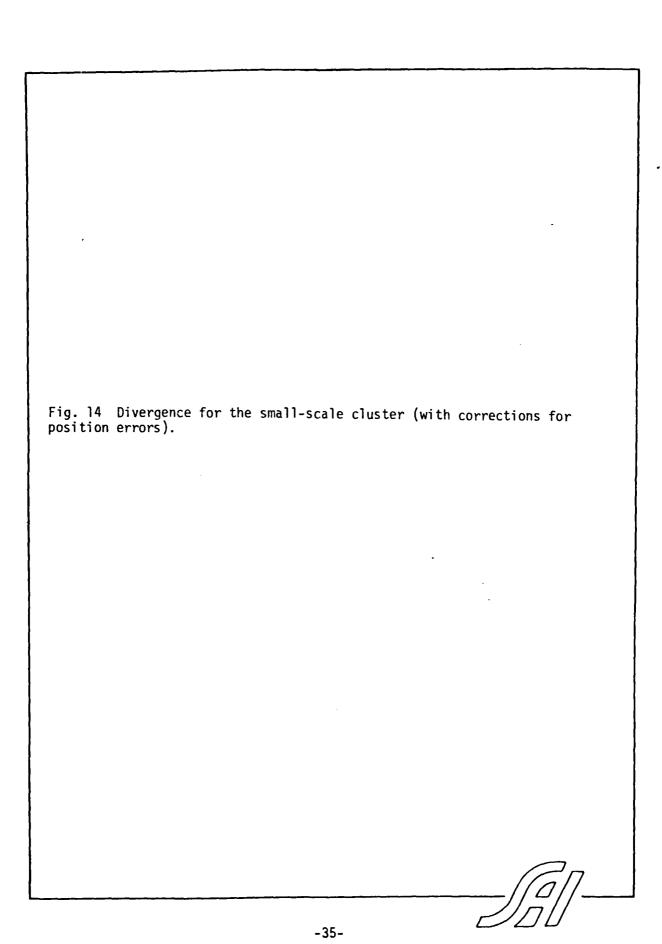


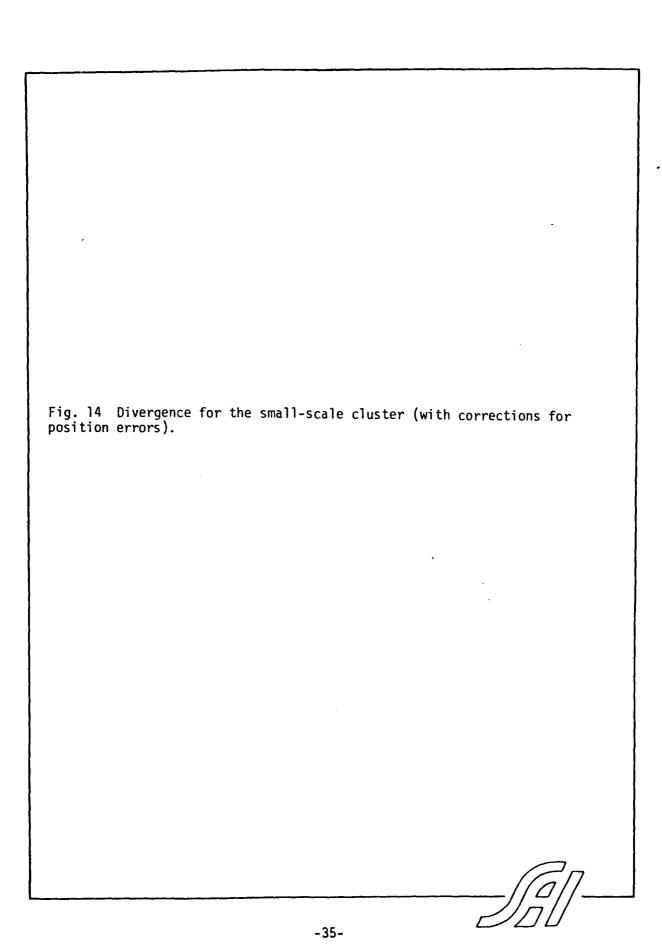
Fig. 13 Vorticity for the small-scale cluster (with corrections for position errors).

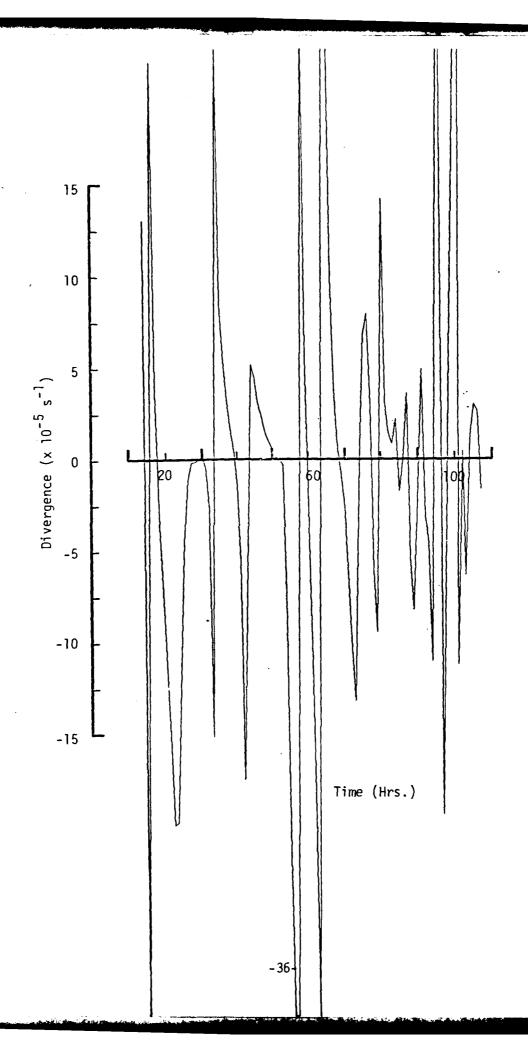


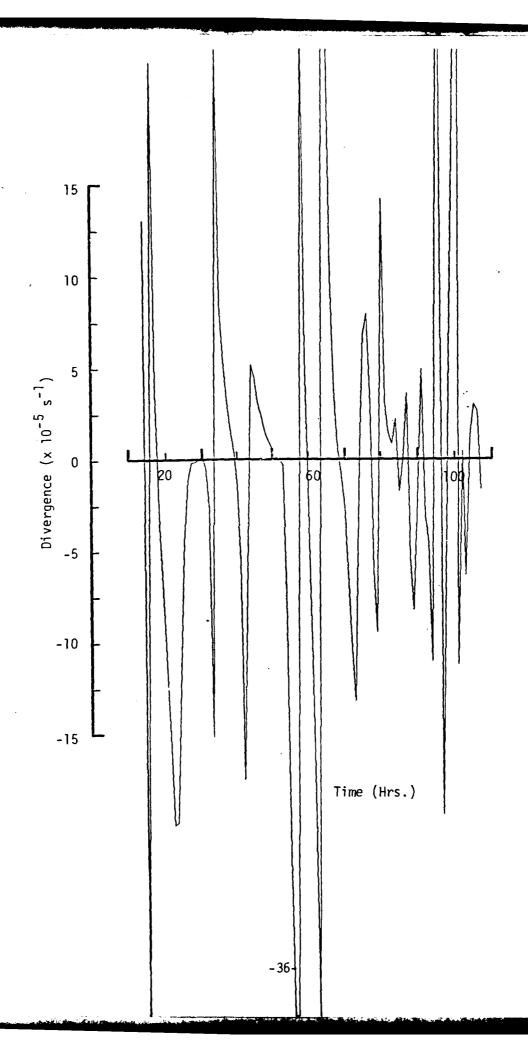












The shear and normal deformation rates for the large-scale cluster were recalculated for both coordinate systems. These time histories are shown in Figs. 15 and 16, respectively. The time histories that were corrected for position errors are shown in Figs. 17 and 18.

The shear and normal deformation rates were recalculated for the small-scale cluster, and these time histories are shown in Figs. 19 and 20, respectively. The time histories corrected for position error are shown in Figs. 21 and 22.

The vorticity and divergence rates for the large-scale cluster were recalculated, and these time histories are shown in Fig. 23. Also shown in Fig. 23 are the components of the vorticity equation. Fig. 24 shows the same time histories but with the position error correction.

The vorticity and divergence rates for the small-scale cluster were recalculated using every 4th point, and these time histories are shown in Figs. 25 and 26, respectively. These time histories after being corrected for position error are shown in Figs. 27 and 28.



The shear and normal deformation rates for the large-scale cluster were recalculated for both coordinate systems. These time histories are shown in Figs. 15 and 16, respectively. The time histories that were corrected for position errors are shown in Figs. 17 and 18.

The shear and normal deformation rates were recalculated for the small-scale cluster, and these time histories are shown in Figs. 19 and 20, respectively. The time histories corrected for position error are shown in Figs. 21 and 22.

The vorticity and divergence rates for the large-scale cluster were recalculated, and these time histories are shown in Fig. 23. Also shown in Fig. 23 are the components of the vorticity equation. Fig. 24 shows the same time histories but with the position error correction.

The vorticity and divergence rates for the small-scale cluster were recalculated using every 4th point, and these time histories are shown in Figs. 25 and 26, respectively. These time histories after being corrected for position error are shown in Figs. 27 and 28.



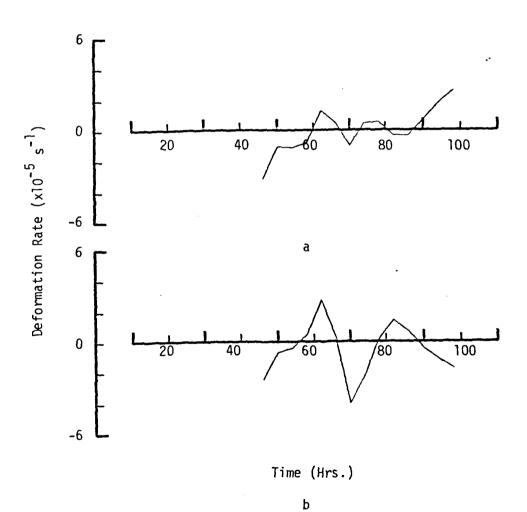


Fig. 15 Shear deformation rates for the large-scale cluster using every 4th data point (without corrections for position errors). a is for a geographic coordinate system, and b is for a natural coordinate system.

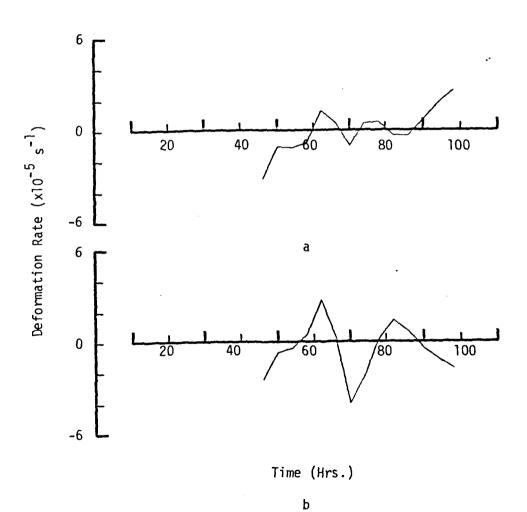


Fig. 15 Shear deformation rates for the large-scale cluster using every 4th data point (without corrections for position errors). a is for a geographic coordinate system, and b is for a natural coordinate system.

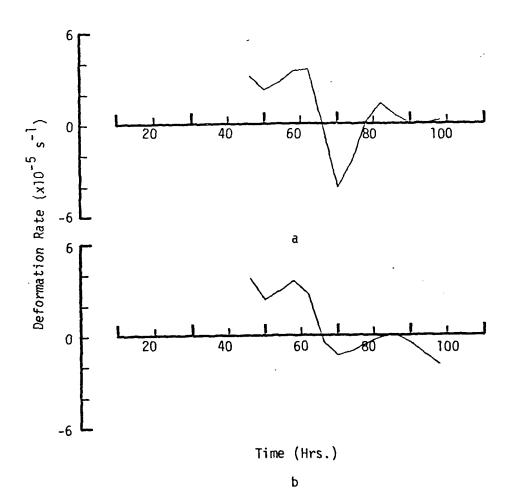


Fig. 16 Normal deformation rates for the large-scale cluster using every 4th data point (without corrections for position errors). a is for a geographic coordinate system, and b is for a natural coordinate system.

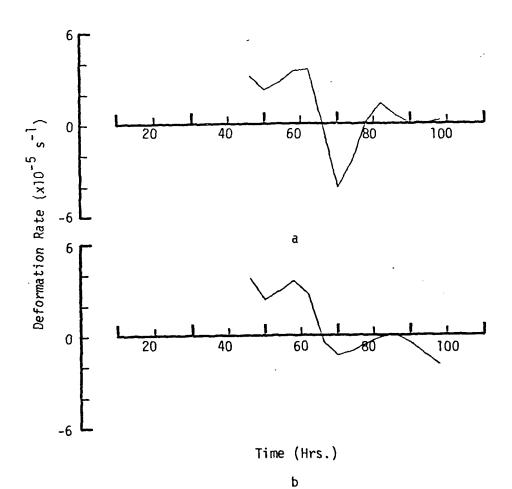


Fig. 16 Normal deformation rates for the large-scale cluster using every 4th data point (without corrections for position errors). a is for a geographic coordinate system, and b is for a natural coordinate system.

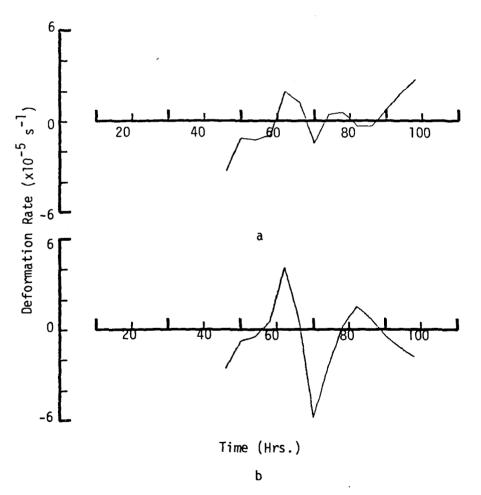


Fig. 17 Shear deformation rates for the large-scale cluster using every 4th data point (with corrections for position errors). a is for a geographic coordinate system, and b is for a natural coordinate system.

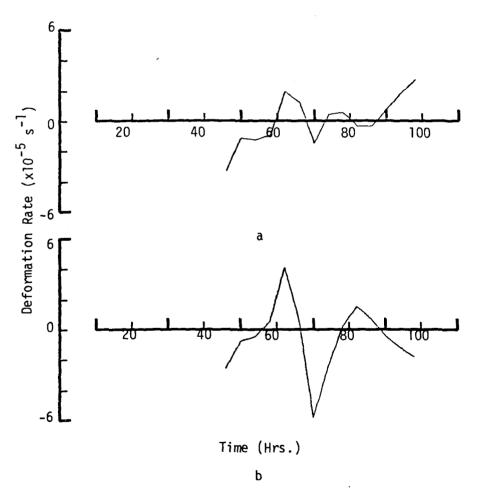


Fig. 17 Shear deformation rates for the large-scale cluster using every 4th data point (with corrections for position errors). a is for a geographic coordinate system, and b is for a natural coordinate system.

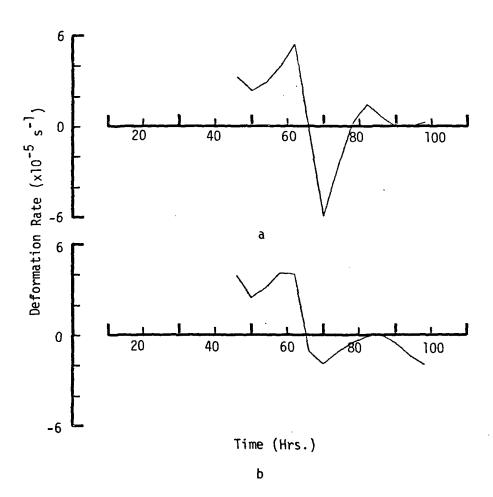
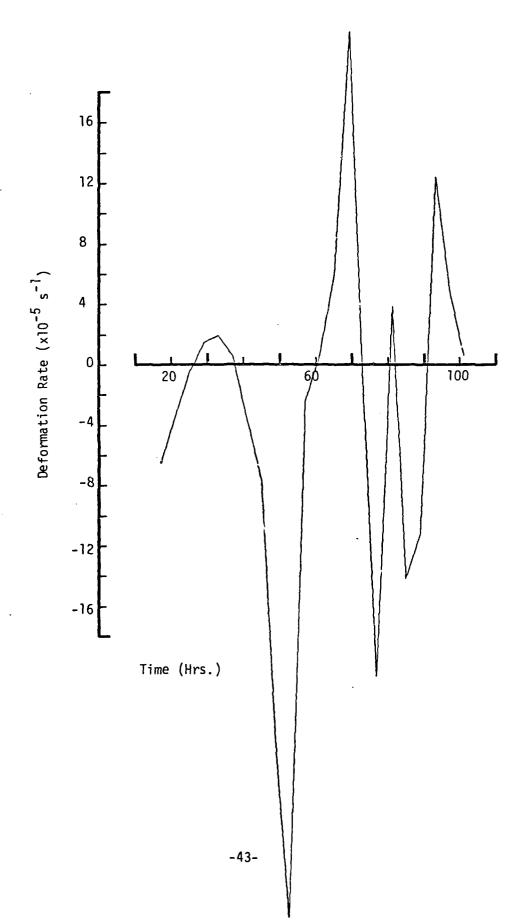


Fig. 18 Normal deformation rates for the large-scale cluster using every 4th data point (with corrections for position errors). a is for a geographic coordinate system, and b is for a natural coordinate system.

Fig. 19 Shear deformation rates for the small-scale cluster using every 4th data point (without corrections for position errors).

-42-



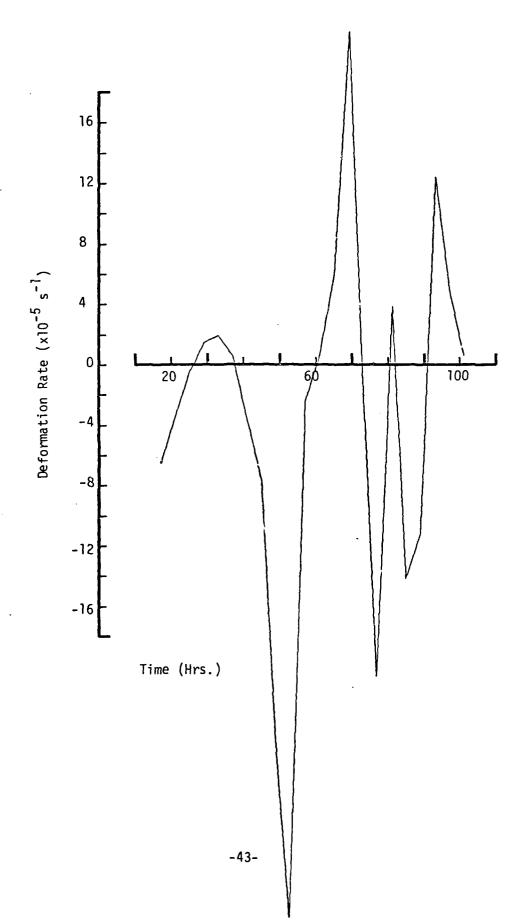
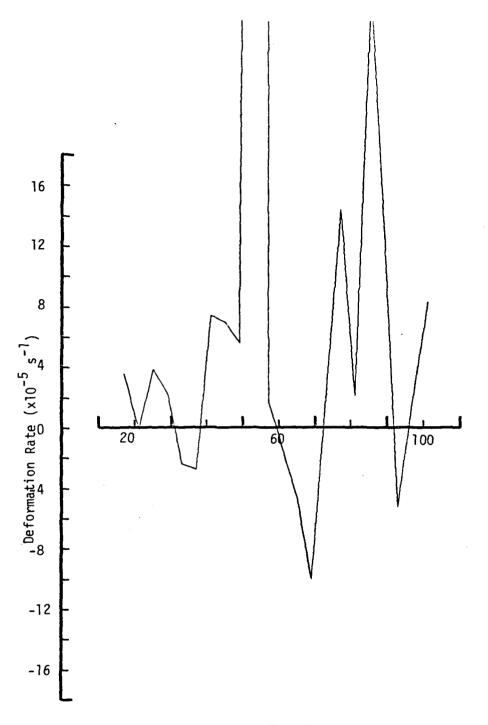


Fig. 20 Normal deformation rates for the small-scale cluster using every 4th data point (without corrections for position errors).

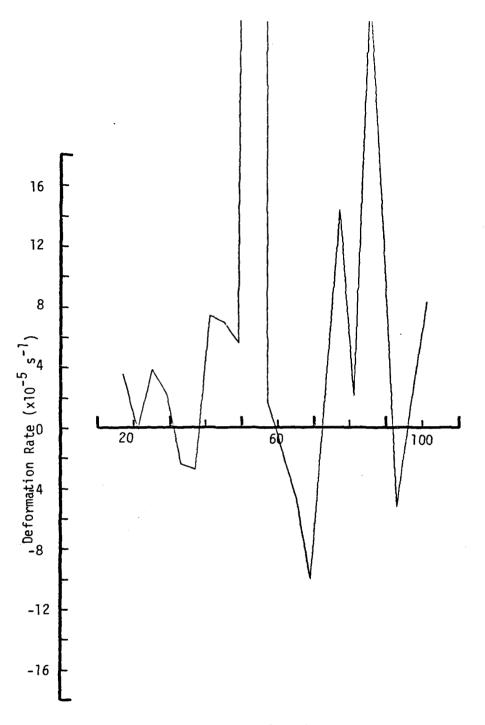
-44-

Fig. 20 Normal deformation rates for the small-scale cluster using every 4th data point (without corrections for position errors).

-44-



Time (Hrs.)



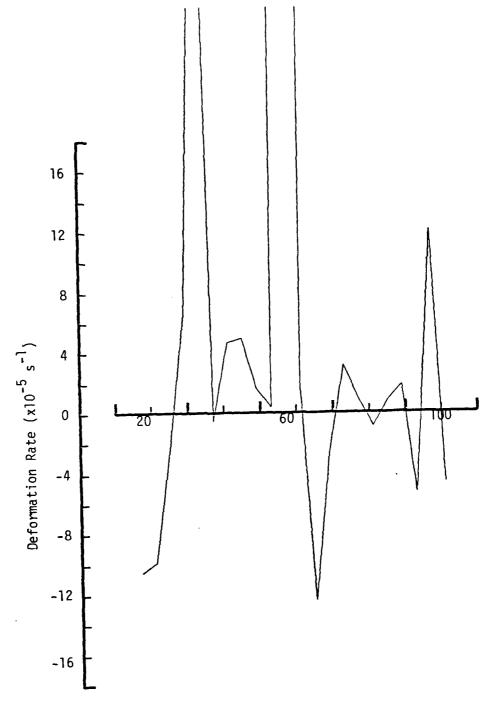
Time (Hrs.)

Fig. 21 Shear deformation rates for the small-scale cluster using every 4th data point (with corrections for position errors).

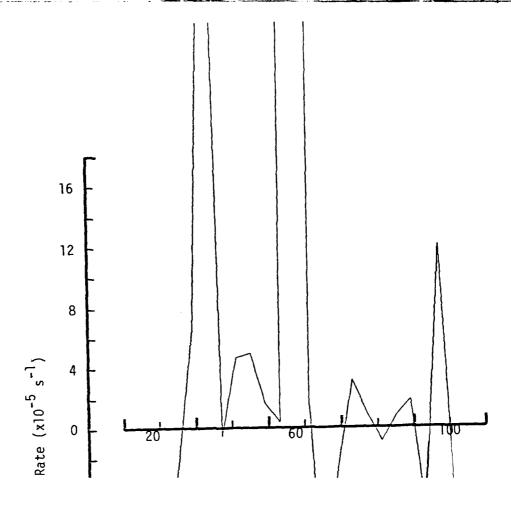
-46-

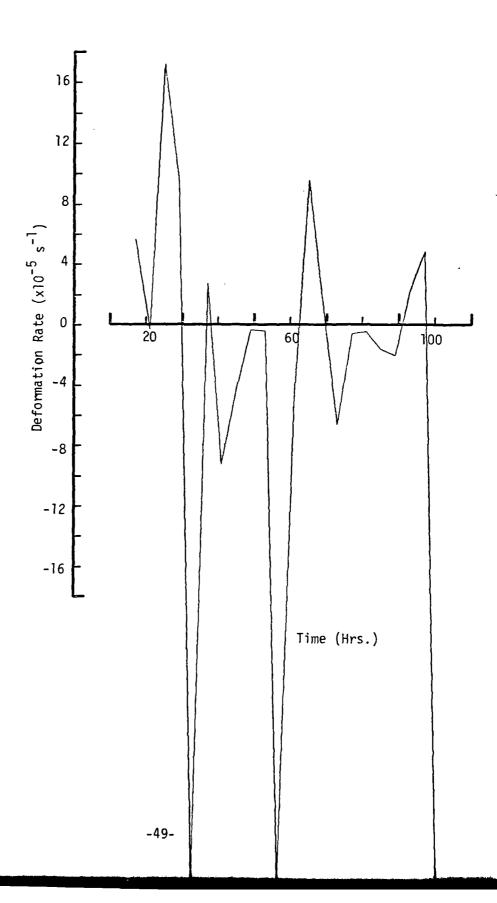
Fig. 21 Shear deformation rates for the small-scale cluster using every 4th data point (with corrections for position errors).

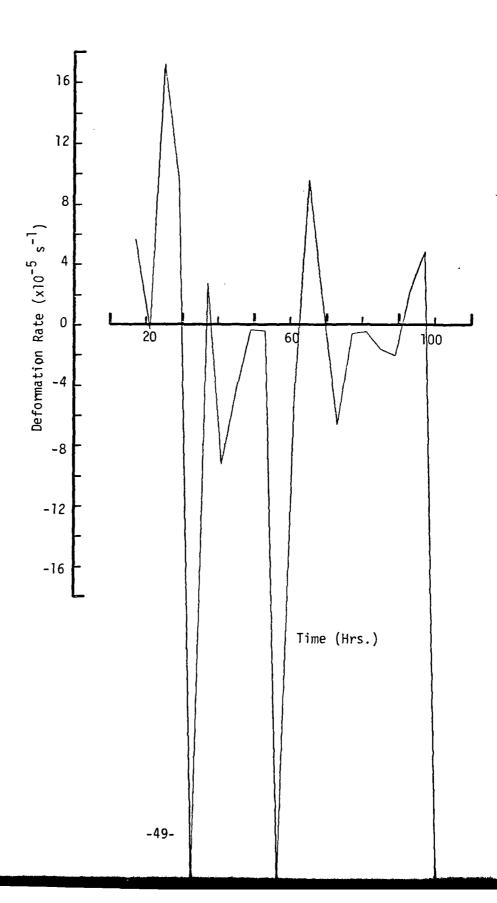
-46-



Time (Hrs.)







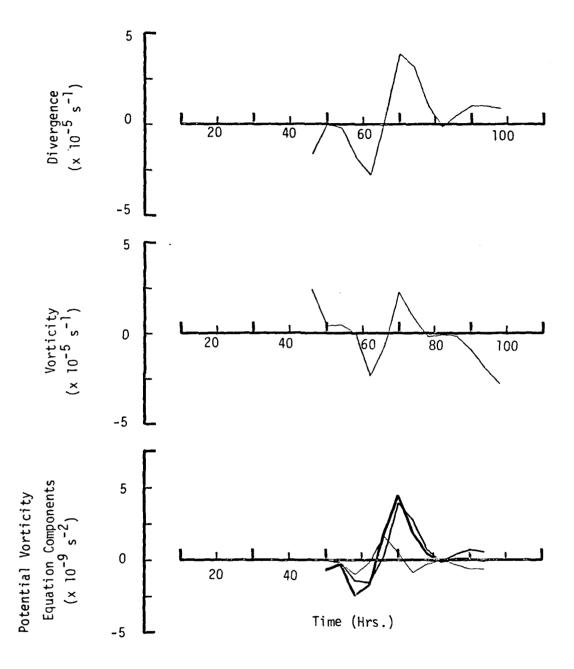


Fig. 23 Divergence, vorticity, and potential vorticity equation components for the large-scale cluster using every 4th data point (without corrections for position errors). For the equation components, the lightest line is the time derivative term, the medium line is the divergence-vorticity term, and the darkest line is the residual term.

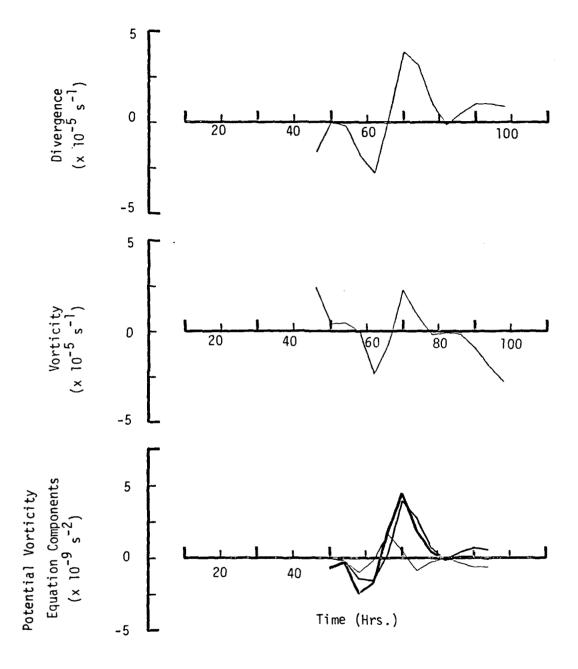


Fig. 23 Divergence, vorticity, and potential vorticity equation components for the large-scale cluster using every 4th data point (without corrections for position errors). For the equation components, the lightest line is the time derivative term, the medium line is the divergence-vorticity term, and the darkest line is the residual term.

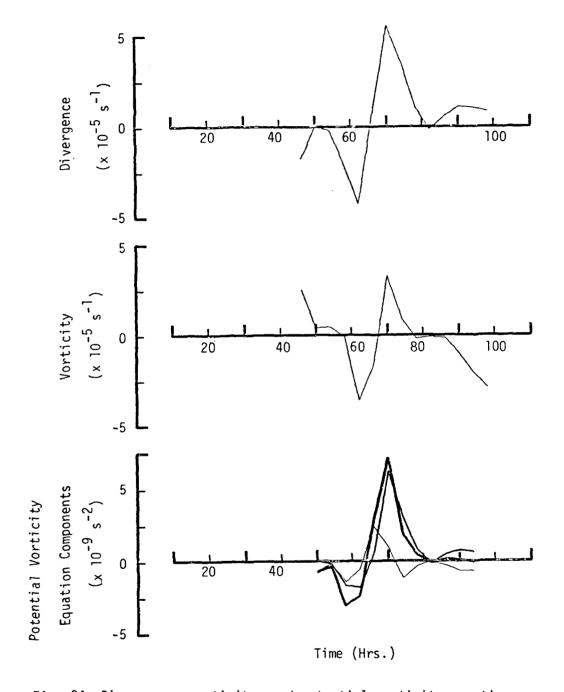


Fig. 24 Divergence, vorticity, and potential vorticity equation components for the large-scale cluster using every 4th data point (with corrections for position errors). For the equation components, the lightest line is the time derivative term, the medium line is the divergence-vorticity term, and the darkest line is the residual term.

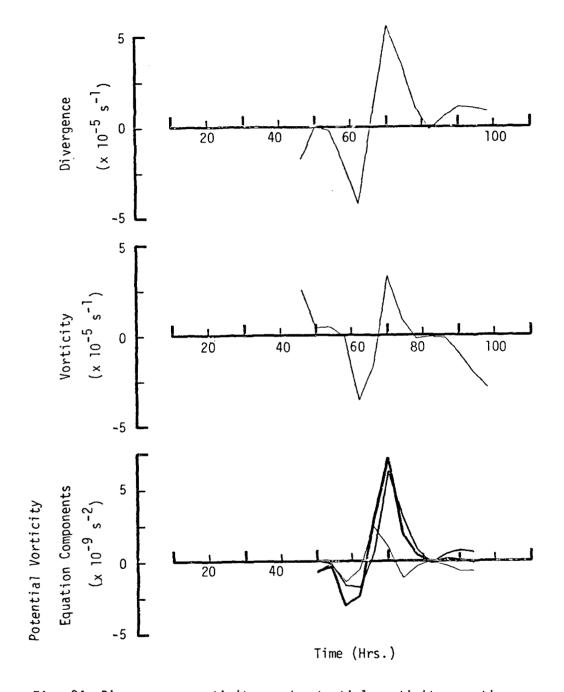
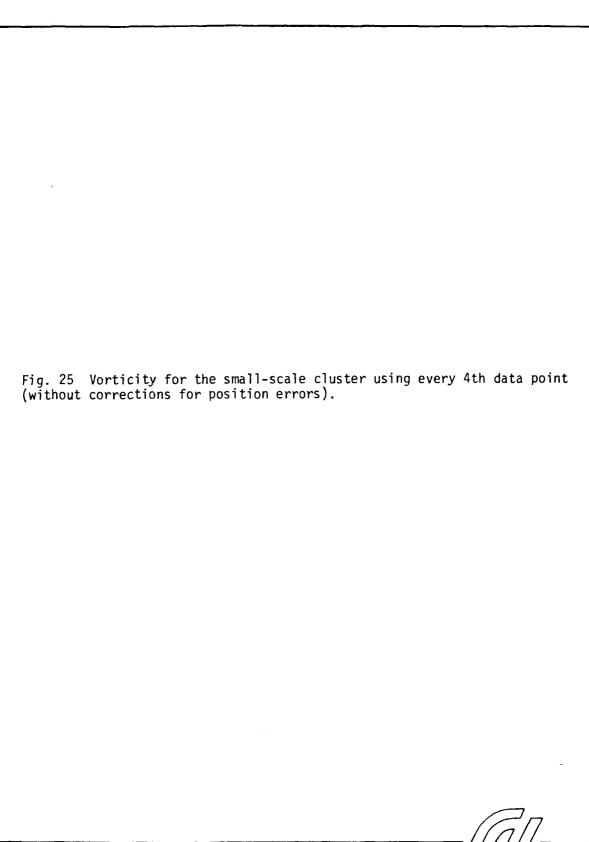
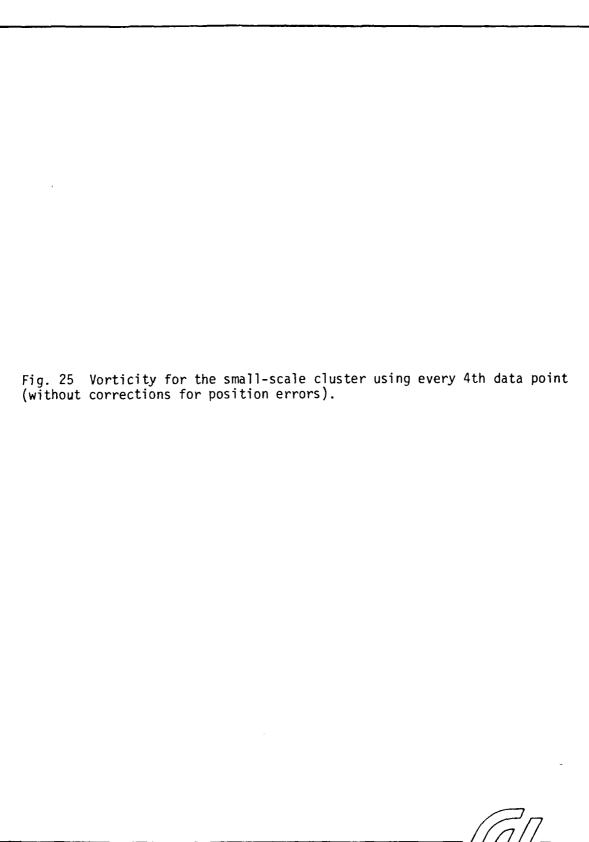
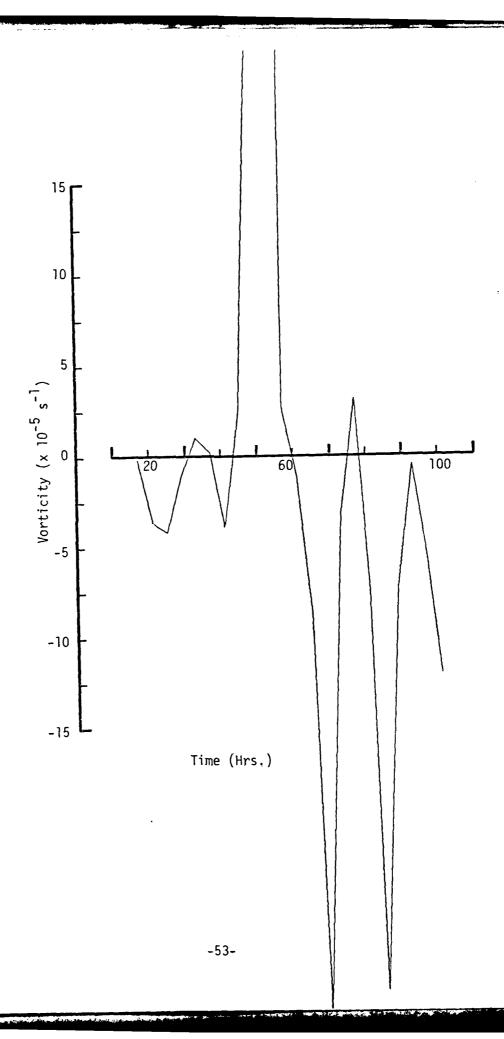


Fig. 24 Divergence, vorticity, and potential vorticity equation components for the large-scale cluster using every 4th data point (with corrections for position errors). For the equation components, the lightest line is the time derivative term, the medium line is the divergence-vorticity term, and the darkest line is the residual term.







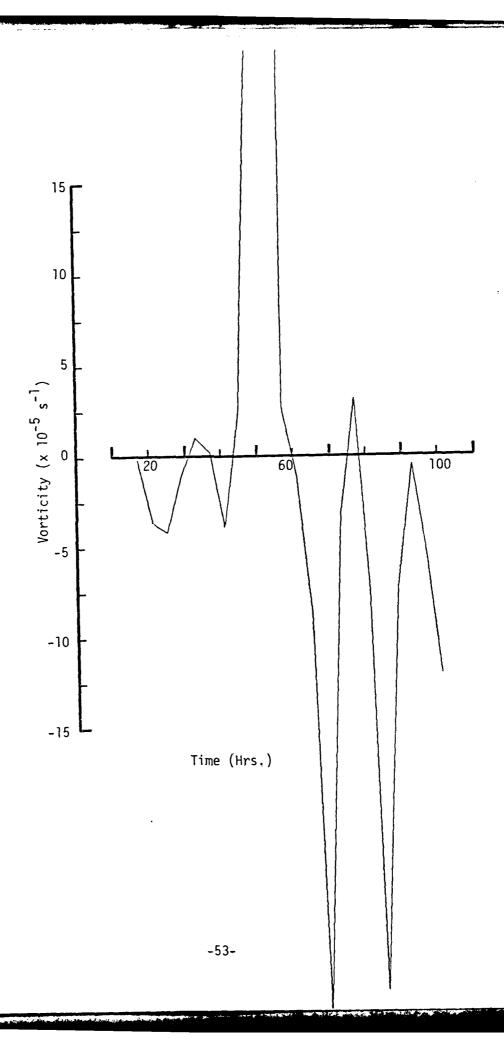
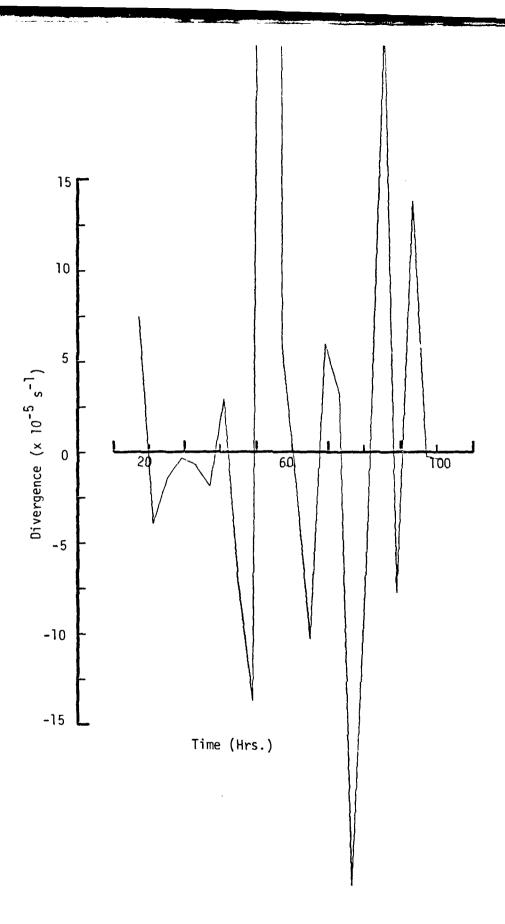


Fig. 26 Divergence for the small-scale cluster using every 4th data point (without corrections for position errors).

-54-

Fig. 26 Divergence for the small-scale cluster using every 4th data point (without corrections for position errors).

-54-



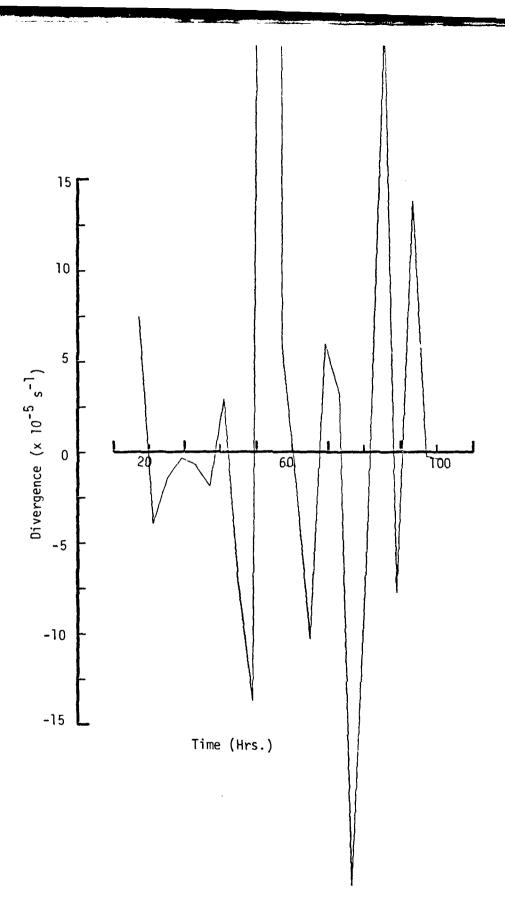
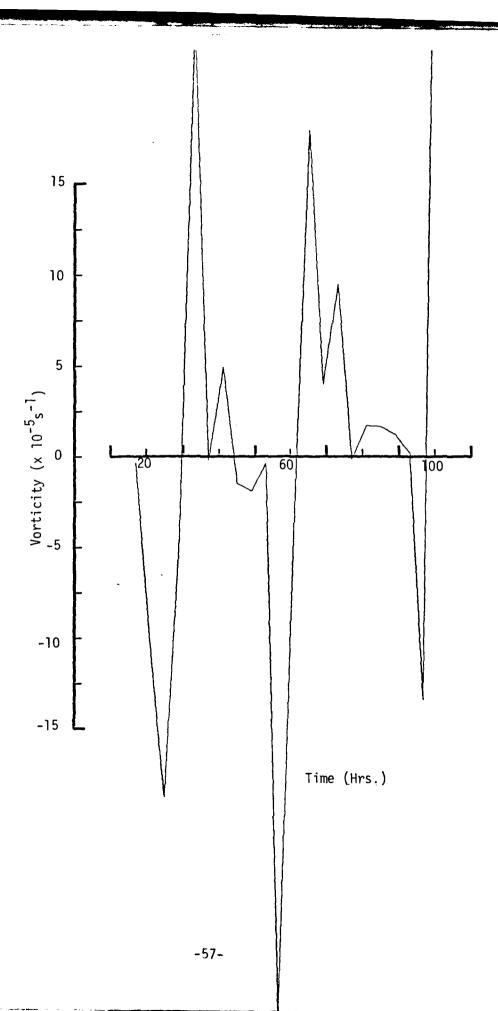


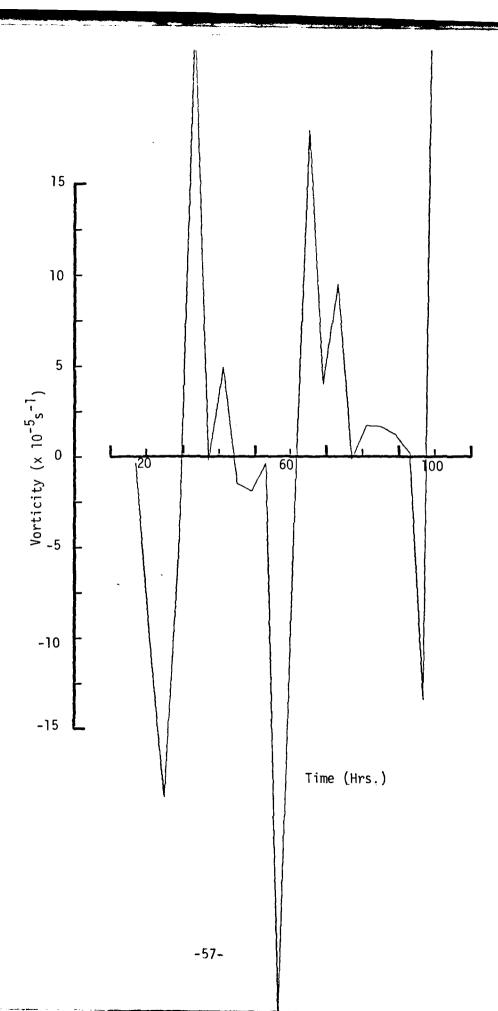
Fig. 27 Vorticity for the small-scale cluster using every 4th data point (with corrections for position errors).

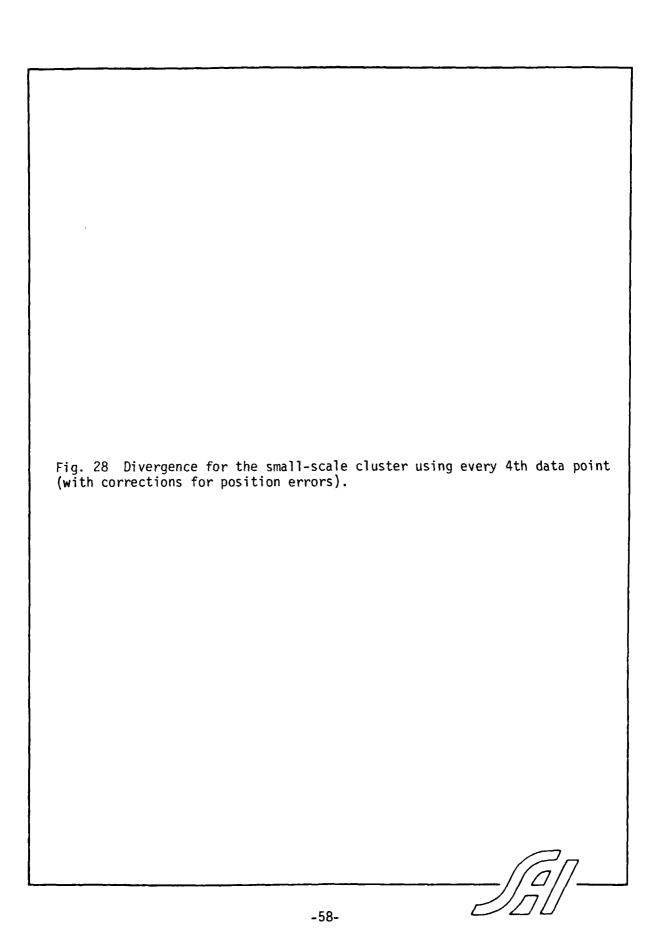
-56~

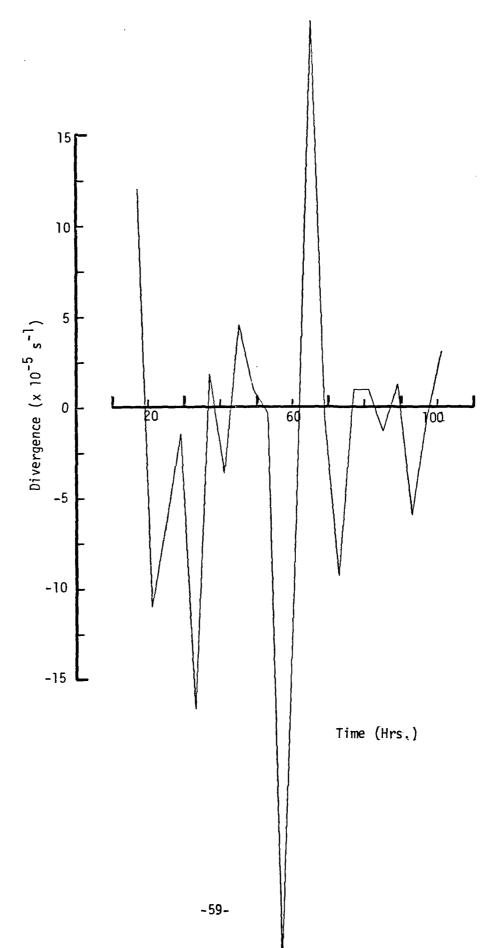
Fig. 27 Vorticity for the small-scale cluster using every 4th data point (with corrections for position errors).

-56~









### 5. Conclusions and Recommendations

There are several conclusions and recommendations which emerge from this study. These are discussed delow.

a. Perhaps the most important fact to emerge from this study is that the orders of magnitude for the DKP from the large-scale cluster are completely consistent with other studies. This strongly suggests that the data have provided useful qualitative information on horizontal shears.

# Recommendation

In order to perform quantitative mechanisms in which horizontal shears are important, it will be necessary to use the original unsmoothed data to construct parallel estimates of the trajectories and velocities. Then, from this, the DKP and vorticity balance should be recalculated.

b. Tests of the interpolation routine and position error effect for the large-scale cluster suggested that neither played a significant role in the qualitative aspects of the results.

### Recommendation

In any future calculations with this data, it would not be necessary to apply position error corrections. Any problems arising from the interpolation procedure would be overcome by following recommendation a.

c. Two quantative tests of the data were performed. They were the transformation to the natural coordinate system and the vorticity balance. There tests failed to provide quantitative information on horizontal shear mechanisms.

## Recommendation

If Recommendation a is carried out, these calculations should be repeated.

d. The smoothed data from the small-scale cluster were not useful for determining small-scale processes. The DKP records were quite noisey with frequent changes of sign. Also, corrections for position errors substantially altered the character of the DKP. From this it appears that the problems are intrinsic to the smoothed data and not related to external sources of error.

# Recommendation

In order to determine whether there is any useful information in this data, it will be necessary to use the original, unsmoothed data and perform parallel analysis for the trajectories and velocities, and then repeat the calculations.

e. All four DKP for the large-scale cluster as well as the residual in the vorticity balance showed a dramatic change of sign around hour 66. From the data supplied to us, we have been unable to isolate a likely cause.

### Recommendation

The original position data, meteorological data and experimental log should be examined to determine if anything unusual occurred during that time period.

The recommendations given above apply to the data set on hand. These suggest, however, some recommendations for future experiments.

- 1. Parallel processing of the raw position data is essential.
- 2. It would have been better to have had one cluster with five drifters rather than separate large and small-scale clusters. One cluster with a large number of drifters should provide the same basic information as separate clusters but with added statistical reliability.

3. Hydrographic data taken along the trajectory of the center of mass of the cluster could have provided very important information on the residual of the vorticity equation. In the natural coordinate system, the baroclinic torque term is very nearly  $\frac{\partial \alpha}{\partial T} \frac{\partial p}{\partial N}$  where T and N are in the tangential and normal directions of the trajectory. The hydrographic data (even XBT data) can supply a sense of  $\frac{\partial \alpha}{\partial T}$ . Since the flow is very nearly quasi-geostrophic, the sense of  $\frac{\partial P}{\partial N}$  is known by inspection.



# 6. References

- 1. Gordon, C.M., 1980: Ltr. of 13 Nov. 1980, Serial 4345-153:CMG:M1.
- Kirwan, A.D., G.J. McNally, M.-S. Chang, and R. Molinari, 1975:
   "The effect of wind and surface currents on drifters." J. Phys. Oceanogr., 5, 361-368.
- 3. Kirwan, A.D., and M.-S. Chang, 1979: "Effect of Sampling Rate and Random Position Error on Analysis of Drifter Data." J. Phys. Oceanogr., 9.2, 382-387.
- 4. Kirwan, A.D., 1975: "Oceanic Velocity Gradients." J. Phys. Oceanogr., 5.4, 729-735.
- 5. Molinari, R., and A.D. Kirwan, 1975: "Calculation of differential kinematic properties of the Yucatan Current from Lagrangian observations." J. Phys. Oceanogr., 5, 483-491.
- Okubo, A., and C.C. Ebbesmeyer, 1976: "Determination of vorticity, divergence, and deformation rates from analysis of drogue observations." Deep Sea Research, 23, 349-352.



# 6. References

- 1. Gordon, C.M., 1980: Ltr. of 13 Nov. 1980, Serial 4345-153:CMG:M1.
- Kirwan, A.D., G.J. McNally, M.-S. Chang, and R. Molinari, 1975:
   "The effect of wind and surface currents on drifters." J. Phys. Oceanogr., 5, 361-368.
- 3. Kirwan, A.D., and M.-S. Chang, 1979: "Effect of Sampling Rate and Random Position Error on Analysis of Drifter Data." J. Phys. Oceanogr., 9.2, 382-387.
- 4. Kirwan, A.D., 1975: "Oceanic Velocity Gradients." J. Phys. Oceanogr., 5.4, 729-735.
- 5. Molinari, R., and A.D. Kirwan, 1975: "Calculation of differential kinematic properties of the Yucatan Current from Lagrangian observations." J. Phys. Oceanogr., 5, 483-491.
- Okubo, A., and C.C. Ebbesmeyer, 1976: "Determination of vorticity, divergence, and deformation rates from analysis of drogue observations." Deep Sea Research, 23, 349-352.



# Appendix A The following is a listing of the computer program used to make the calculations for this study.



```
//DKP JOB (A043.01A.01,50.JL) - J.K.LEWIS*
                      /*JUE PARM
                                                          R=128
                     // EXEC FTNXVTEC.GUREGN=128K
//FORT:SYSIN DO *
    4.
   5.
                                    REAL N(100).IA(100)
                                    DMENSION \times (100.3).Y(100.3).X(100.3).Y(100.3).D(160).
   0.
    7.
                                  1 VDR(160),5(160),XC(160),YC(160),VXC(160),VYC(160),
                              "2 NI (3) .PA(160)
    8.
                                    CALL PLUTS(U.U.U)
   y.
 10.
                                    READ IN TIME SPAN REQUIRED.
 11.
                     Č
                                   READ(5.10) NS.NF
 12.
 13.
                                    FORMAT(16 15)
 14.
 15.
                                    NP=NF-NS+1
16.
                                    READ IN DRIFTER NUM. AND ITS START AND END TIMES.
 17.
 16.
                             DU 20 I=1.3
READ(5.10) NI(1).IS.IF
 19.
20.
21.
                     C
22.
                     C
                                    READ IN THE DATA FOR THE NI(1) DRIFTER.
 23.
                                    READ(5,40) (X(J+K-1,1),K=1,10)
                            DO 30 J=IS.IF.10
24.
25.
                                    DO 32 K=1.10
 26.
                                    X(J+K-1,I)=-X(J+K-1,I)
 27.
                        J2
                              CONTINUE
20.
                        30
 24.
                                   FURMAT(10 F8-2)
 30.
                                    DO 50 J=15.1F.10
                                   DO 50 J=15+1F+10
READ(5,40) (Y(J+K-1,1)+K=1,10)
 31.
                       20 CONTINUE
ISP=15+1
32.
                                                                                   ......
33.
34.
                                    IFM=NF-1
35.
                            CALC. SPEED COMPONENTS.
36.
37.
3೮∙
                                   .000F**2=MUN3G
34.
                                    TIME=3600.
                            DU 31 J=1.3
DU 31 K=15P.1FM
40.
                                                                                                                                   in a service of the s
41-
42-
                                    VX(K_{\bullet}J)=(X(K+1_{\bullet}J)-X(K-1_{\bullet}J)) VDENOM
                        31
                                    VY(K+J)=(Y(K+1+J)-Y(K-1+J)) \setminus DENOM
43.
44.
                                 "CALC. POSITIONS AND VELL OF CENTRUID.
45.
40.
47.
                                   DO 41 1=15P+1FM
                                   5X=0.
48.
45.
                                    5Y=0.
50-
                                   SVX=0.
51.
                                   5VY=0.
52.
                                   DO 42 J=1,3
                                   5x=5x+x(1,J)
5.3.
                                      5Y=5Y+Y(1,J)
54.
55.
                                   SVX=SVX+VX(I,J)
56.
                                   SVY=SVY+VY(1.J)
57.
                                   XC(1)=5x/3.
                                    YC(1)=SY/3.
50.
                                   VXC(1)=SVX/3.
54.
60.
                                   VYC(1)=SVY/3.
```

```
61.
                                        CUNVERT PUSITIONS AND VELOCITIES RELATIVE TO CENTROID.
  62.
  63.
                               E. I=L 18 DD

WAI: ASI=I 15 DD

WAI: ASI=I 15 DD

WAI: ASI=I 15 DD

WAI: ASI=I NO

WAI: ASI=I NO
  64.
  65.
  60.
  67.
                                        (I) 0 x (I+J) x x (I)
  60.
                           51 - VY(1, J) = VY(1, J) - VYC(1)
  69.
  70.
                                        CALC. DKP DF SYSTEM.
  71.
                        C
  72.
                             DO 61 I=ISP+IFM
SXX=0+
  73.
  74.
  75.
                                        5XY=0 .
                                        SYY=0.
  76.
                                 ## "SVXX=0.
  77-
                              5VXY=0.
   78.
  79.
                                        SVYY=0.
                                        SVYX=0.
  80.
                             " DO 62 J=1.3
  81.
                               " A1=X(I+J)
  82.
                                        A2=Y([,J)
  83.
                                        B1=VX(I,J)
  84.
                                82=VY(I,J)
  85.
                                        SXX=SXX+A1 *A1
  80.
                                        SXY=SXY+A1#A2
  87.
                                         SYY=SYY+A2*A2
  600
                                 """ SVXX=SVXX+B1*A1
  89.
                                        SVXY=SVXY+H1*AZ
  90.
                                        SVYY=SVYY+82*A2
  91.
                                        SVYX=5VYX+B2*A1
  92.
                                                                                                             . . . .
  93.
                                    "FURM SPACIAL DERIVATIVES OF VELOCITIES.
  94.
  95.
                        C
                                 DENOM=SXY*SXY-SXX#SYY+350.**2*(SXX+SYY)+350.***4
  90.
  97.
                                  THE FOLLOWING ARE FOR A 350 METER AVERAGE POSITION ERROR. THE TERMS HAVE BEEN MODIFIED TO ELIMINATE
   90.
  99.
                                        BIASING DUE TO THIS ERRUR.
100.
101.
                                 DVXDY=(5VXX*5XY-5VXY*5XX+350.*(5VXX+SVXY))/DENUM
DVXDX=(5VXX*5YY-5VXY*5XY-350.*(5VXX+SVXY))/(-DENOM)
102.
103.
                                        DVYDY=(SVYX+SXY-SVYY+SXX+350.*(SVYX+SVYY))/DENOM
104.
                                        DVYDX=(SVYX+SYY-SVYY*SXY-350.*(SVYX+SVYY))/(-DENOM)
105.
100.
                        č
10/.
                                        FURM DKP.
108.
                                  D(I)=DVXDX+DVYDY
109.
                                        VOR (1)=UVYDX-UVXDY
110.
111.
                                        N(I)=DVXDX-DVYDY
                           61 S(I)=DVXDY+DVYDX
112.
113.
                                WRITE OUT RESULTS.
114-
115.
116.
                                        WRITE (6.6)
                            DO 100 I=ISP.IFM
100 WRITE(6-101) 1.0(1).VUR(1).H(1).S(1).XC(1).YC(1)
117-
                                                                                       DIVER VORTY N DEF S DEF
                                                                                                                                                                                                  X CENTER
                                        FORMAT( * HOUR
114.
                                      1 Y CENTER .//)
120.
                                        FORMAT(1X-16-E10-3-5 (E9-2-1X))
                            101
121.
```

```
122.
 123.
                                    NOW MAKE CALC.S FUR A NATURAL COURDINATE SYSTEM.
  124.
 125.
                                    DO 1000 I=ISP.IFM
 126.
                                 X(I.1)=ATAN2(VYC(I),VXC(I))*180./3.14159-90.
                                    X(1,2)=S(1)/(VYC(1)**2-VXC(1)**2)
 127.
                                    X(1.3)=N(1)-X(1.2)*2.*VXC(1)*VYC(1)
 120.
                                    Y(1,1)=SQRT(VXC(1)##2+VYC(1)##2)
 129.
                                Y(1,2)=(N(1)*(VYC(1)**2-VXC(1)**2)-2.*S(1)*VXC(1)*
 130.
                                                   VYC(1))/Y(1,1)**2
 131.
                         1000 Y(1,3)=(S(1)*(VYC(1)**2-VXC(1)**2)+2.*N(1)*VXC(1)*
 132-
 133.
                                                  VYC(1))/Y(1+1)**2
                         1020 FORMAT(*1THE FOLLOWING ARE PARAMETERS OF THE NATURAL SYSTEM*.
 134.
 135.
                                                                                  EQ 19 EQ 18
                                                                                                                            SPEED N DEF
 136.
                                                                                                                                                                        S DEF.
                                  2//)
 137.
                          DO 1010 I=ISP.IFM
 138-
                                   WHITE (0.101) 1, (X(1,K),X=1.3).(Y(1,K),K=1.3)
 139.
 140.
                         1010 CUNTINUE
 141.
                      C TEMPLOT
                                                                         The state of the s
 142-
 143.
 144.
                                    DO 3000 I=ISP,IFM
 145.
                                    1A(1-15P+1)=1
                         3000 PA(I-ISP+1)=Y(I,3)
 146.
                                    CALL SET(3.,7.,2.8,4.8,10.,110.,-0.00000,+.00000,1)
CALL HALFAX(5,2,1,0,0.,0.,0)
 147-
 146.
                            CALL CURVE(IA.PA.IFM-ISP+1)
CALL SET(3..7..5.1.7.1.10..110..-0.00000..00006.1)
 149.
 150.
                                    CALL HALFAX(5,2,1,0,0,0,0,0,0)
 151.
                        DO 3010 I=15P.IFM
5010 PA(I-15P+1)=5(1)
 152.
 153.
                       CALL CURVE (IA.PA.IFM-ISPFI)
154.
 155.
                                   CALL HLOT(0.0.-999)
                                   CALL SET(3.,7.,2.8,4.8,10.,110.,-0.00006,+0.00006,1)
 150.
                        CALL HALFAX (5.2.1.6.0..0..0)
DO 3030 I=ISP.IFM

J030 PA([-ISP+1)=Y(I.2]
 157.
158.
 159.
                                   CALL CURVE(IA.PA.IFM-ISP+1)
 100.
                         CALL SET(3..7..5.1.7.1.10...110...-U.00000.+0.00000.1)

CALL HALFAX(5.2.1.0.00..0.0)

DU 3040 I=1SP.1FM
161.
162.
163.
                        3040 PA(I-15P+1)=N(I)
 164.
                          CALL CURVE(IA-PA-IFM-ISP+1)
CALL PLUT(0.0.-999)
165.
160-
167.
168.
                                   CALC. PUT. VURT. EQN. COMP. 15.
169.
                            WRITE (6+2001)
170.
                        2001 FURMAT( 1POT. VURT. EUR. CUMP. 5".// HOUR
171.
                                                                                                                                            TIME DER DIV*VUR
                                 IRES 1//
172.
173.
                                   DEN(M=2.*3600.
                              ___ ISS=NS+2
174.
                                   IFF=NF-2
175-
175.5
                                  F=1.458E-04#51N(32.#2.#3.14159/360.)
                                  DO 2000 I=155.IFF
FO=F+YC(I-1)*1.941E-11
176.
178.
179.
                                  FN=F+YC(1+1)*1.941E-11
                                  FR=F+YC(1)*1.941E-11
180.
                                   x(1+1)=(VOR(1+1)+FN-VOR(1-1)-FO)/DENOM
181.
182.
                                   X(I,2)=0(I)*(VUR(I)+FR)
```

```
122.
 123.
                                    NOW MAKE CALC.S FUR A NATURAL COURDINATE SYSTEM.
  124.
 125.
                                    DO 1000 I=ISP.IFM
 126.
                                 X(I.1)=ATAN2(VYC(I),VXC(I))*180./3.14159-90.
                                    X(1,2)=S(1)/(VYC(1)**2-VXC(1)**2)
 127.
                                    X(1.3)=N(1)-X(1.2)*2.*VXC(1)*VYC(1)
 120.
                                    Y(1,1)=SQRT(VXC(1)##2+VYC(1)##2)
 129.
                                Y(1,2)=(N(1)*(VYC(1)**2-VXC(1)**2)-2.*S(1)*VXC(1)*
 130.
                                                   VYC(1))/Y(1,1)**2
 131.
                         1000 Y(1,3)=(S(1)*(VYC(1)**2-VXC(1)**2)+2.*N(1)*VXC(1)*
 132-
 133.
                                                  VYC(1))/Y(1+1)**2
                         1020 FORMAT(*1THE FOLLOWING ARE PARAMETERS OF THE NATURAL SYSTEM*.
 134.
 135.
                                                                                  EQ 19 EQ 18
                                                                                                                            SPEED N DEF
 136.
                                                                                                                                                                        S DEF.
                                  2//)
 137.
                          DO 1010 I=ISP.IFM
 138-
                                   WHITE (0.101) 1, (X(1,K),X=1.3).(Y(1,K),K=1.3)
 139.
 140.
                         1010 CUNTINUE
 141.
                      C TEMPLOT
                                                                         The state of the s
 142-
 143.
 144.
                                    DO 3000 I=ISP,IFM
 145.
                                    1A(1-15P+1)=1
                         3000 PA(I-ISP+1)=Y(I,3)
 146.
                                    CALL SET(3.,7.,2.8,4.8,10.,110.,-0.00000,+.00000,1)
CALL HALFAX(5,2,1,0,0.,0.,0)
 147-
 146.
                            CALL CURVE(IA.PA.IFM-ISP+1)
CALL SET(3..7..5.1.7.1.10..110..-0.00000..00006.1)
 149.
 150.
                                    CALL HALFAX(5,2,1,0,0,0,0,0,0)
 151.
                        DO 3010 I=15P.IFM
5010 PA(I-15P+1)=5(1)
 152.
 153.
                       CALL CURVE (IA.PA.IFM-ISPFI)
154.
 155.
                                   CALL HLOT(0.0.-999)
                                   CALL SET(3.,7.,2.8,4.8,10.,110.,-0.00006,+0.00006,1)
 150.
                        CALL HALFAX (5.2.1.6.0..0..0)
DO 3030 I=ISP.IFM

J030 PA([-ISP+1)=Y(I.2]
 157.
158.
 159.
                                   CALL CURVE(IA.PA.IFM-ISP+1)
 100.
                         CALL SET(3..7..5.1.7.1.10...110...-U.00000.+0.00000.1)

CALL HALFAX(5.2.1.0.00..0.0)

DU 3040 I=1SP.1FM
161.
162.
163.
                        3040 PA(I-15P+1)=N(I)
 164.
                          CALL CURVE(IA-PA-IFM-ISP+1)
CALL PLUT(0.0.-999)
165.
160-
167.
168.
                                   CALC. PUT. VURT. EQN. COMP. 15.
169.
                            WRITE (6+2001)
170.
                        2001 FURMAT( 1POT. VURT. EUR. CUMP. 5".// HOUR
171.
                                                                                                                                            TIME DER DIV*VUR
                                 IRES 1//
172.
173.
                                   DEN(M=2.*3600.
                              ___ ISS=NS+2
174.
                                   IFF=NF-2
175-
175.5
                                  F=1.458E-04#51N(32.#2.#3.14159/360.)
                                  DO 2000 I=155.IFF
FO=F+YC(I-1)*1.941E-11
176.
178.
179.
                                  FN=F+YC(1+1)*1.941E-11
                                  FR=F+YC(1)*1.941E-11
180.
                                   x(1+1)=(VOR(1+1)+FN-VOR(1-1)-FO)/DENOM
181.
182.
                                   X(I,2)=0(I)*(VUR(I)+FR)
```

```
X(1.3)=X(1.1)+X(1.2)
183.
            2000 BRITE(6,101) I.X(1,1),X(1,2),X(1,3)
184.
185.
                  PLOT
180-
187.
             CALL SET(3..7..5.1.7.1.10..110..-0.00005.+0.00005.1)
 188.
                  CALL HALFAX(5,2,1,4,0,0,0,0)
 189-
                 DO 2040 1=15P.1FM
TIA(1-15P+1)=1
190.
191.
           2040"PA(I-15P+1)=VUR(1)
192-
          CALL CURVE(IA-PA-IFM-ISIM-I)
CALL SET(3-.7-.7-4-9-4-10-.110-.-U-00005-+0-00005-1)
CALL HALFAX(5-2-1-4-0--0-0-0-0)
DU 2050 I=15P-IFM
193.
194.
195.
190.
          " 2050 PA(I-ISP+1)=D(I)
197.
          CALL CURVE(IA.PA.1FM-ISP+1)
DD 2010 I=ISS.IFF
198-
199.
                  "IA(1-155+1)=I
20 J.
201.
                  PA(I-ISS+1)=X(I-1)
            2010 CONTINUE
202.
            CALL SET(3-,7-,2-8,4-8,10-,110-,-0-000000005,+0-0000000005,1)
CALL HALFAX(5,2,1-5,0-,0,0)
CALL NEWPEN(1)
203.
204.
205.
200.
                  CALL CURVE(IA.PA.IFF-ISS+1)
           CALL NEWPEN(3)
DU 2020 1=155,1FF
207-
200.
            2020 PA(I-ISS+1)=X(1.2)
CALL CURVE(IA.PA.IFF-ISS+1)
CALL NEWPEN(5)
209.
210.
                VALL NEWPEN(5)
DU 2030 1=155-1FF
211.
212-
            2030 PA(1-155+1)=X(1.3)
213.
                 CALL CURVE(1A.PA.IFF-ISS+1)
214.
              CALL PLOT(0.0.-999)
CALL PLOT(0.0.+999)
215.
210.
                 STOP
217-
                 END
218.
           //LKED:PLOTLIB DD DSN=USER:OCN:GUINASSO.JOBL18;DISP=SHR
219.
           //LKED-SYSIN DD *
220.
            INCLUDE PLOTLIB(PLOTVTEC.PERIM.PARX)
221.
           //GD-SYSIN-DD DSN=WYL-JL-ABH-LARG -DISP=SHR
221-
223.
           /*END
                                                                  المرابة الشيبين مساهدات ماما
```

A-5

The second secon

```
X(1.3)=X(1.1)+X(1.2)
183.
            2000 BRITE(6,101) I.X(1,1),X(1,2),X(1,3)
184.
185.
                  PLOT
180-
187.
             CALL SET(3..7..5.1.7.1.10..110..-0.00005.+0.00005.1)
 188.
                  CALL HALFAX(5,2,1,4,0,0,0,0)
 189-
                 DO 2040 1=15P.1FM
TIA(1-15P+1)=1
190.
191.
           2040"PA(I-15P+1)=VUR(1)
192-
          CALL CURVE(IA-PA-IFM-ISIM-I)
CALL SET(3-.7-.7-4-9-4-10-.110-.-U-00005-+0-00005-1)
CALL HALFAX(5-2-1-4-0--0-0-0-0)
DU 2050 I=15P-IFM
193.
194.
195.
190.
          " 2050 PA(I-ISP+1)=D(I)
197.
          CALL CURVE(IA.PA.1FM-ISP+1)
DD 2010 I=ISS.IFF
198-
199.
                  "IA(1-155+1)=I
20 J.
201.
                  PA(I-ISS+1)=X(I-1)
            2010 CONTINUE
202.
            CALL SET(3-,7-,2-8,4-8,10-,110-,-0-000000005,+0-0000000005,1)
CALL HALFAX(5,2,1-5,0-,0,0)
CALL NEWPEN(1)
203.
204.
205.
200.
                  CALL CURVE(IA.PA.IFF-ISS+1)
           CALL NEWPEN(3)
DU 2020 1=155,1FF
207-
200.
            2020 PA(I-ISS+1)=X(1.2)
CALL CURVE(IA.PA.IFF-ISS+1)
CALL NEWPEN(5)
209.
210.
                VALL NEWPEN(5)
DU 2030 1=155-1FF
211.
212-
            2030 PA(1-155+1)=X(1.3)
213.
                 CALL CURVE(1A.PA.IFF-ISS+1)
214.
              CALL PLOT(0.0.-999)
CALL PLOT(0.0.+999)
215.
210.
                 STOP
217-
                 END
218.
           //LKED:PLOTLIB DD DSN=USER:OCN:GUINASSO.JOBL18;DISP=SHR
219.
           //LKED-SYSIN DD *
220.
            INCLUDE PLOTLIB(PLOTVTEC.PERIM.PARX)
221.
           //GD-SYSIN-DD DSN=WYL-JL-ABH-LARG -DISP=SHR
221-
223.
           /*END
                                                                  المرابة الشيبين مساهدات ماما
```

A-5

The second secon

Арр	endix B									
	The follow	ing are	tables	of	the	output	from	the	production	runs.
	•									
									/	G1

B-1

Арр	endix B									
	The follow	ing are	tables	of	the	output	from	the	production	runs.
	•									
									/	G1

B-1

Table B-1 DKP and the location of the center of mass for the large-scale cluster (without corrections for position errors). This data is for a geographic coordinate system.

Table B-1 DKP and the location of the center of mass for the large-scale cluster (without corrections for position errors). This data is for a geographic coordinate system.

```
VIX TY
                                                       SUEF
                                                                 X CENTER
                                                                                Y CENTER
                DIVER
                                          N DEF
    MOUR
                                       0.35E-04 -0.37E-04 0.11E+00
0.34E-04 -0.38E-04 0.11E+00
     #43-0.378E-04*0.32E-04
44-0.262E-04*0.31E-04
                                                                               0.15E+06
                                                                               0-14E+00
                                                   -0.36E-04
         45-0.162E-04 0.28E-04
                                        0.31E-04
                                                                  0.1UE+06
                                                                               0-14E+06
                                       0-28E-04
                                                   -0.32E-04
         40-0.804E-05 0.24E-04
                                                                 0-10F+0p
                                                                               0-14E+00
                                                  -0.20E-04
      47-0-226E-0570-19L-04
                                                                               0.14E+06
                                        0-25E-04
                                                                 0-10E+00
         48 0.101E-05 0.12E-04
49 0.222E-05 0.45E-05
                                        U-23E-04
                                                                 0 • 1 JE+00
                                                                               6 -14E+00
                                        0.2UE-04 -0.12E-04
                                                                               0-13E+06
                                                                 0.10E+06
^}
     50 0.125E-05-0.41E-05
51 0.285E-06-0.95E-05
                                                                               0 -1 3E+00
                                        0.18E-04
                                                   -0.27E-05
                                                                 0 - 1 OF +0 o
                                        0-18E-04
                                                  0.27E-05
                                                                               0-13E+06
                                                                 0-10E+00
   52 0.602E-06-0.70E-05
                                                    0-65E-07
                                                                               C -13E+06
                                        0-20E-04
                                                                 0.10E+06
         53 0.154E-05 0.16E-05
54 0.804E-06 0.11E-04
                                        0.25E-04
                                                   -0.87E-05
                                                                  0.105+06
                                                                               0.13E+06
                                                   -0.19E-04
                                       0-29E-04
                                                                 0.10E+0n
                                                                               0-1 £+00
                                       0-33E-04
0-35E-04
     55-0.182E-05-0.20E-04
50-0.737E-05-0.17E-04
                                                   =0.27E=04
-0.25E=04
                                                                 D:10E+06
                                                                               0-12E+06
                                                                 0.1 ÚE+06
                                                                               0.12E+06
                                                                               0-12E+06
         57-0.145E-04 0.58E-05
                                        0.35E-04 -0.15E-04
                                                                 0-10E+06
`)
                                       0.37E-04 -0.46E-05
0.38E-04 0.31E-05
         58-0.207E-04-0.49E-05
                                                                 0.1UE+00
                                                                               0-12E+00
    59-0.259E-04-0.14E-04
                                        0-38E-04
                                                                 0-10E+06
                                                                               0.12E+06
                                                                 0.1 JE+00
                                                                               0 -1 2E +06
                                       U-40E-04
                                                    ひっしりと つしゅ
                                                    0.15E-04
0.15E-04
0.21E-04
0.19E-04
         61-0.320E-04-0.27E-04
                                                                 0.1 以に+0 6
                                                                               U-12E+06
                                        0-411-04
                                       0-40E-04
                                                                 0-13E+00
         62-0.3225-04-0.305-04
                                                                               U-11L+00
   63-0.287E-04-0.33E-04
                                       0.36E-04
                                                                 0-10E+06
                                                                               0.11E+00
                                       0.25E-04
                                                                 0.1 JE+00
                                                                               U-11E+00
         05-0.124E-04-0.21E-04
                                        0-16E-04
                                                    0-14E-04
                                                                 0-10E+06
                                                                               0-11E+06
     00-0.431E-05-0.10E-04
67'0.151E-04'0.33E-05
08 0.207c-04'0.15E-04
                                       0.58E-05
                                                    0.56E-05
                                                                 0.10E+06
                                                                               0-11E+06
                                                  -0-12E-05
                                      -0-16E-04
                                                                               0 -1 1E +06
                                                                 0"+99E+05
                                      -0-30E-04
-0-41E-04
                                                   -0.82E-05
                                                                 0.94E+05
                                                                               0.11E+00
                                                  -0.15E-04
                                                                 0.98E+05
                                                                               0-10E+06
         69 0.352E-04 0.26E-04
   70 0.417E-04 0.32E-04
71 0.420E-04 0.35E-04
72 0.402E-04 0.37E-04
                                      -0.48E-04 -0.19E-04
-0.48E-04 -0.21E-04
-0.45E-04 -0.23E-04
                                                                 0.97E+05
                                                                               0-105+06
                                                                 0-97E+05
                                                                               0:10E+06
                                                               -0.90E+05
                                                                               0.10E+00
         73 U.441E-U4 U.15E-04
                                                   -0.21E-06
0.12E-04
                                      -U-40E-04
                                                                 0.95E+05
                                                                               0.99E+05
   74 0.4032-04 0.23E-05
75 0.308E-04-0.57E-05
76 0.260E-04-0.28E-05
77 0.200E-04-0.62E-05
                                      -0.31E-04
                                                                               0.97E+05
                                                                 0.94E+05
                                      -0.31E-04 0.15E-05
-0.22E-04 0.65E-05
-0.14E-04 0.14E-04
-0.64E-05 0.13E-04
                                                                              0.96E+05
                                                                 10-93E+05
                                                                 0-92E+05
                                                                               U-95E+05
                                      -U.64E-US
                                                                 0.91E+05
                                                                               U-93E+05
    78 0.1316-04-0.32E-05
79 0.837E-05-0.14E-05
                                                    0.12E-04
0.48E-05
                                                                 0.89E+05
                                                                               0 .92E +05
                                      -0.18E-00
                                        0-39E-05
                                                                 0-88E+05
                                                                               0.91E+05
                                                   -0.55E-06
         30 U.199E-US-0.28E-05
                                        0-11E-04
                                                                 0.87E+05
                                                                               0.9HE+05
         81-0.13/E-04-0.36E-05
82-0.211E-04-0.49E-06
                                       0.27E-04
0.33E-04
                                                   -0.50E-05
                                                                 0.85E+05
                                                                               0.898+05
                                                   -0.96E-05
                                                                 0.84E+05
                                                                               0 -88E +05
         83-0.549E-05"0.14E-05
84 0.457E-05 0.41E-06
                                                  -0.85E-05
   0-17E-04
                                                                 0382E+05
                                                                              0.87E+05
                                                                               0 -86E+05
                                       0-66E-05
                                                                 0-81E+05
         85 0.643E-05 0.14E-05
                                                   -0.59E-U5
                                       0.43E-05
                                                                 0.79E+05
                                                                               0.85E+05
       86 0.809E-05 0.47E-06
87 0.886E-05-0.12E-06
                                                   -0.45E-05
                                                                 0.78E+05
                                                                               0 -84E +05
                                       0.28E-05
                                                                               0-83E+05
                                       0-11E-05
                                                                 0.76E+05
   -0.52E-06
         86 0.907E-05-0-27E-05
                                       0-11E-00
                                                                 0.75E+05
                                                                              0.82E+05
                                                    0.40E-05
                                       0-22E-07
         a9 0.103E-04-0.70E-05
                                                                 0.73E+05
                                                                               0.81E+05
         90 0.106E-04-0.72E-05
                                      -0.83E-00
                                                                 0.71E+05
                                                                               0.81E+05
                                                    0.79E-05
0.12E-04
         91 0.107E-04-0.10E-04
92 0.107E-04-0.14E-04
                                                                 0170E+05
                                                                              0 -80F +05
                                      -0-14E-05
                                      -0 . 1 JE -05
                                                                 0•08E+05
                                                                              0-79E+05
                                                    0.15E-04
0.18E-04
0.19E-04
                                      -U.54E-Uo
                                                                               U.78E+05
         93 0.107E-04-0.17E-04
                                                                 0.67E+05
       94 0.102E-04-0.20E-04
95 0.962E-05-0.21E-04
                                      —0 •40E −0ი
                                                                 0.65E+05
                                                                               0-775+05
                                      -0.45E-06
                                                                 0.63E+05
                                                                               0.77E+05
         96 U-908E-05-0-24E-04
                                       0-53F-00
                                                                               U . 70E +05
                                                    0-22E-04
                                                                 0.62E+05
         97 0.875E-05-0.27E-04
98 0.837E-05-0.28E-04
                                       0.10E-05
0.19E-05
                                                    0.25E-04
0.25E-04
                                                                 0.60E+05
0.58E+05
                                                                              U -75E+05
                                                                              U .75E +05
                                                    0.29E-04
         59 0.832E-05-0.31E-04
                                       0-24E-05
                                                                 0.57E+05
                                                                              0.74E+05
        100 0.766E-05-0.32E-04
                                       0.396-05
                                                    0.30E-04
                                                                 0.55E+05
                                                                              U-73E+05
                                                                              0-73E+05
                                       0-4/E-U5
                                                                 U.5 JE+05
        101 0.640E-05-0.32E-04
                                                    0-295-04
                                       0.51E-05
0.61E-05
        102 0.635E-05-0.32E-04
                                                    0.29E-04
                                                                 0.52E+05
                                                                              0.72E+05
                                                    0-27E-04
        103 0.573と-05-0.29た-04
                                                                 0.50E+05
                                                                               0.72E+05
        104 0.505E-05-0.26E-04
                                                    0.23E-04
                                       0.70E-05
                                                                 0.48E+05
                                                                               0.71E+05
                                                    0.215-04
0.18E-04
                                                                 0.47E+05
0.45E+05
        105 U.304L-05-0.25E-04
106 0.356E-05-U.21E-04
                                       0.87E-05
                                                                              0.716+05
                                       0.90E-05
                                                                              0.70E+05
                                                    0.99E-05
                                                                              0.70E+05
                                                                 0.43E+05
             0-296L-05-0-13E-04
                                       0-93L-05
```

``

```
VIX TY
                                                       SUEF
                                                                 X CENTER
                                                                                Y CENTER
                DIVER
                                          N DEF
    MOUR
                                       0.35E-04 -0.37E-04 0.11E+00
0.34E-04 -0.38E-04 0.11E+00
     #43-0.378E-04*0.32E-04
44-0.262E-04*0.31E-04
                                                                               0.15E+06
                                                                               0-14E+00
                                                   -0.36E-04
         45-0.162E-04 0.28E-04
                                        0.31E-04
                                                                  0.1UE+06
                                                                               0-14E+06
                                       0-28E-04
                                                   -0.32E-04
         40-0.804E-05 0.24E-04
                                                                 0-10F+0p
                                                                               0-14E+00
                                                  -0.20E-04
      47-0-226E-0570-19L-04
                                                                               0.14E+06
                                        0-25E-04
                                                                 0-10E+00
         48 0.101E-05 0.12E-04
49 0.222E-05 0.45E-05
                                        U-23E-04
                                                                 0 • 1 JE+00
                                                                               6 -14E+00
                                        0.2UE-04 -0.12E-04
                                                                               0-13E+06
                                                                 0.10E+06
^}
     50 0.125E-05-0.41E-05
51 0.285E-06-0.95E-05
                                                                               0 -1 3E+00
                                        0.18E-04
                                                   -0.27E-05
                                                                 0 - 1 OF +0 o
                                        0-18E-04
                                                  0.27E-05
                                                                               0-13E+06
                                                                 0-10E+00
   52 0.602E-06-0.70E-05
                                                    0-65E-07
                                                                               C -13E+06
                                        0-20E-04
                                                                 0.10E+06
         53 0.154E-05 0.16E-05
54 0.804E-06 0.11E-04
                                        0.25E-04
                                                   -0.87E-05
                                                                  0.105+06
                                                                               0.13E+06
                                                   -0.19E-04
                                       0-29E-04
                                                                 0.10E+0n
                                                                               0-1 £+00
                                       0-33E-04
0-35E-04
     55-0.182E-05-0.20E-04
50-0.737E-05-0.17E-04
                                                   =0.27E=04
-0.25E=04
                                                                 D:10E+06
                                                                               0-12E+06
                                                                 0.1 ÚE+06
                                                                               0.12E+06
                                                                               0-12E+06
         57-0.145E-04 0.58E-05
                                        0.35E-04 -0.15E-04
                                                                 0-10E+06
`)
                                       0.37E-04 -0.46E-05
0.38E-04 0.31E-05
         58-0.207E-04-0.49E-05
                                                                 0.1UE+00
                                                                               0-12E+00
    59-0.259E-04-0.14E-04
                                        0-38E-04
                                                                 0-10E+06
                                                                               0.12E+06
                                                                 0.1 JE+00
                                                                               0 -1 2E +06
                                       U-40E-04
                                                    ひっしりと つしゅ
                                                    0.15E-04
0.15E-04
0.21E-04
0.19E-04
         61-0.320E-04-0.27E-04
                                                                 0.1 以に+0 6
                                                                               U-12E+06
                                        0-411-04
                                       0-40E-04
                                                                 0-13E+00
         62-0.3225-04-0.305-04
                                                                               U-11L+00
   63-0.287E-04-0.33E-04
                                       0.36E-04
                                                                 0-10E+06
                                                                               0.11E+00
                                       0.25E-04
                                                                 0.1 JE+00
                                                                               U-11E+00
         05-0.124E-04-0.21E-04
                                        0-16E-04
                                                    0-14E-04
                                                                 0-10E+06
                                                                               0-11E+06
     00-0.431E-05-0.10E-04
67'0.151E-04'0.33E-05
08 0.207c-04'0.15E-04
                                       0.58E-05
                                                    0.56E-05
                                                                 0.10E+06
                                                                               0-11E+06
                                                  -0-12E-05
                                      -0-16E-04
                                                                               0 -1 1E +06
                                                                 0"+99E+05
                                      -0-30E-04
-0-41E-04
                                                   -0.82E-05
                                                                 0.94E+05
                                                                               0.11E+00
                                                  -0.15E-04
                                                                 0.98E+05
                                                                               0-10E+06
         69 0.352E-04 0.26E-04
   70 0.417£-04 0.32£-04
71 0.420£-04 0.35£-04
72 0.402£-04 0.37£-04
                                      -0.48E-04 -0.19E-04
-0.48E-04 -0.21E-04
-0.45E-04 -0.23E-04
                                                                 0.97E+05
                                                                               0-105+06
                                                                 0-97E+05
                                                                               0:10E+06
                                                               -0.90E+05
                                                                               0.10E+00
         73 U.441E-U4 U.15E-04
                                                   -0.21E-06
0.12E-04
                                      -U-40E-04
                                                                 0.95E+05
                                                                               0.99E+05
   74 0.4032-04 0.23E-05
75 0.308E-04-0.57E-05
76 0.260E-04-0.28E-05
77 0.200E-04-0.62E-05
                                      -0.31E-04
                                                                               0.97E+05
                                                                 0.94E+05
                                      -0.31E-04 0.15E-05
-0.22E-04 0.65E-05
-0.14E-04 0.14E-04
-0.64E-05 0.13E-04
                                                                              0.96E+05
                                                                 10-93E+05
                                                                 0-92E+05
                                                                               U-95E+05
                                      -U.64E-US
                                                                 0.91E+05
                                                                               U-93E+05
    78 0.1316-04-0.32E-05
79 0.837E-05-0.14E-05
                                                    0.12E-04
0.48E-05
                                                                 0.89E+05
                                                                               0 .92E +05
                                      -0.18E-00
                                        0-39E-05
                                                                 0-88E+05
                                                                               0.91E+05
                                                   -0.55E-06
         30 U.199E-US-0.28E-05
                                        0-11E-04
                                                                 0.87E+05
                                                                               0.9HE+05
         81-0.13/E-04-0.36E-05
82-0.211E-04-0.49E-06
                                       0.27E-04
0.33E-04
                                                   -0.50E-05
                                                                 0.85E+05
                                                                               0.898+05
                                                   -0.96E-05
                                                                 0.84E+05
                                                                               0 -88E +05
         83-0.549E-05"0.14E-05
84 0.457E-05 0.41E-06
                                                  -0.85E-05
   0-17E-04
                                                                 0382E+05
                                                                              0.87E+05
                                                                               0 -86E+05
                                       0-66E-05
                                                                 0-81E+05
         85 0.643E-05 0.14E-05
                                                   -0.59E-U5
                                       0.43E-05
                                                                 0.79E+05
                                                                               0.85E+05
       86 0.809E-05 0.47E-06
87 0.886E-05-0.12E-06
                                                   -0.45E-05
                                                                 0.78E+05
                                                                               0 -84E +05
                                       0.28E-05
                                                                               0-83E+05
                                       0-11E-05
                                                                 0.76E+05
   -0.52E-06
         86 0.907E-05-0-27E-05
                                       0-11E-00
                                                                 0.75E+05
                                                                              0.82E+05
                                                    0.40E-05
                                       0-22E-07
         a9 0.103E-04-0.70E-05
                                                                 0.73E+05
                                                                               0.81E+05
         90 0.106E-04-0.72E-05
                                      -0.83E-00
                                                                 0.71E+05
                                                                               0.81E+05
                                                    0.79E-05
0.12E-04
         91 0.107E-04-0.10E-04
92 0.107E-04-0.14E-04
                                                                 0170E+05
                                                                              0 -80F +05
                                      -0-14E-05
                                      -0 . 1 JE -05
                                                                 0•08E+05
                                                                              0-79E+05
                                                    0.15E-04
0.18E-04
0.19E-04
                                      -U.54E-Uo
                                                                               U.78E+05
         93 0.107E-04-0.17E-04
                                                                 0.67E+05
       94 0.102E-04-0.20E-04
95 0.962E-05-0.21E-04
                                      —0 •40E −0ი
                                                                 0.65E+05
                                                                               0-775+05
                                      -0.45E-06
                                                                 0.63E+05
                                                                               0.77E+05
         96 U-908E-05-0-24E-04
                                       0-53F-00
                                                                               U . 70E +05
                                                    0-22E-04
                                                                 0.62E+05
         97 0.875E-05-0.27E-04
98 0.837E-05-0.28E-04
                                       0.10E-05
0.19E-05
                                                    0.25E-04
0.25E-04
                                                                 0.60E+05
0.58E+05
                                                                              U -75E+05
                                                                              U .75E +05
                                                    0.29E-04
         59 0.832E-05-0.31E-04
                                       0-24E-05
                                                                 0.57E+05
                                                                              0.74E+05
        100 0.766E-05-0.32E-04
                                       0.396-05
                                                    0.30E-04
                                                                 0.55E+05
                                                                              U-73E+05
                                                                              0-73E+05
                                       0-4/E-U5
                                                                 U.5 JE+05
        101 0.640E-05-0.32E-04
                                                    0-295-04
                                       0.51E-05
0.61E-05
        102 0.635E-05-0.32E-04
                                                    0.29E-04
                                                                 0.52E+05
                                                                              0.72E+05
                                                    0-27E-04
        103 0.573と-05-0.29た-04
                                                                 0.50E+05
                                                                               0.72E+05
        104 0.505E-05-0.26E-04
                                                    0.23E-04
                                       0.70E-05
                                                                 0.48E+05
                                                                               0.71E+05
                                                    0.215-04
0.18E-04
                                                                 0.47E+05
0.45E+05
        105 U.304L-05-0.25E-04
106 0.356E-05-U.21E-04
                                       0.87E-05
                                                                              0.716+05
                                       0.90E-05
                                                                              0.70E+05
                                                    0.99E-05
                                                                              0.70E+05
                                                                 0.43E+05
             0-296L-05-0-13E-04
                                       0-93L-05
```

``

Table B-2 DKP for the large-scale cluster (without corrections for position errors). This data is for a natural coordinate system.

Table B-2 DKP for the large-scale cluster (without corrections for position errors). This data is for a natural coordinate system.

# "THE FOLLOWING ARE PARAMETERS OF THE NATURAL SYSTEM"

```
SPIZED
                                                                 N DEF
                                                                              S DEF
אטטא 🛉
            ALPHA
                                                                       0.44E-04 -0.26E-04
0.42E-04 -0.23E-04
0.34E-04 -0.25E-04
0.34E-04 -0.25E-04
        43-0.1881+03
                                                        0.505+00
                                                        0.51E+U0
        44-0.167E+03
                                                        0.51E+00
0.51E+00
        45-0.187£+03
      ~46-0.186E+03
                                                      47-0 . 185E+03
        48-0-1855+03
        49-0-164 0+03
     50-0.183E+03
                                                                                      0-43E-U5
                                                                       0.17E-04
0.20E-04
                                                        0.4 bE+00
        51-0.1835+03
                                                                                   0-28E-05
                                                        0.475 +00
        52-0 · 1n4t+03
                                                      0.47E+00 0.26E-04 -0.32E-05
-0.46E+00 0.34E-04 -0.13E-04
0.45E+00 0.41E-04 -0.13E-04
        53-0.1606+03
    54-0.189E+03
                                                                       0.42E-04 -0.96E-05
0.33E-04 -0.66E-06
                                                        0.45E+00
        50-0-1925+03
        57-0.191 E+03
                                                        0.44E+00
 58-0-190E+03
                                                       "0.43E+00" 0.36E-04 '0.84E-05
                                                                                    0-10E-04
0-26
                                                        0.421+00
0.41E+00
                                                                       0.35E-04
0.34E-04
        59-0-1906+03
        60-0.1916+03
                                                                      0.32E-04 0.30E-04
0.32E-04 0.33E-04
0.28E-04 0.35E-04
        61-0-191E+03
                                                        0.41E+00
                                                      0.40E+00
    ~~~~62-0 • 193E+03
                                                        0-40E+00 -
        CO+3 461.0-50
                                                      0.40E+00 0.12E-04 0.29E-04
0.40E+00 0.53E-05 0.21E-04
0.40E+00 0.53E-05 0.21E-04
0.40E+00 0.90E-06 0.80E-05
0.40E+00 -0.11E-04 -0.12E-04
0.41E+00 -0.14E-04 -0.28E-04
        04-0.190E+03
        65-0-198E+03
       ·66-0。200E+03
        67-0 - 202E+03
        08-0.204E+03
                                                       0.41E+00 ~0.1:E-04 ~0.42E-04
0.42E+00"=0.10E-04 ~0.50E-04
        69-0.200E+03
       70-0.208E+03
                                                        U.43E+00 -U.46E-05 -U.52E-04
        71-0.211 =+03
                                                        0.44E+00 0.18E-05 -0.50E-04
0.45E+00 -0.13E-04 -0.38E-04
0.47E+00 -0.19E-04 -0.27E-04
0.48E+00 -0.10E-04 -0.20E-04
        72-0.213E+03
        73-0.215E+03
        74-0.218E+03
        75-0-220E+03
                                                        0.49E+00 -0.16E-04 -0.12E-04
0.50E+00 -0.18E-04 -0.53E-05
        70-0 -222E+03
        77-0.223E+03
                                                                     -0.12E-04 -0.26E-06
-0.52E-05 0.33E-05
                                                        0.50E+00 -0.12E-04
0.49E+00 -0.52E-05
78-0.225E+03
        79-0-229E+03
                                                        0.48E+00 -0.23E-05
0.47E+00 -0.52E-05
0.48E+00-0.52E-05
                                                                                     U-11E-04
       80-0.232E+03
                                                                                      0-27E-04
        61-0.236E+03
                                                                                   0.34E-04
 82-0-237E+03
                                                                       0.615-06 0.19E-04
                                                        U-49L+00
        83-0-237L+03
                                                       0.49E+00 0.21E-05 0.83E-05
0.50E+00 0.33E-05 0.66E-05
0.50E+00 0.25E-05 0.46E-05
0.50E+00 0.24E-05 0.27E-05
        84-0.238E+03
        b5-0.239E+03
  86-0.240E+03
       87-0-24UL+U3
                                                       08-0-241E+03
        69-0.2422+03
    90-0-243E+03
       91-0-243E+03
                                                        0.50E+00 -0.84E-05 -0.82E-05
0.50E+00 -0.12E-04 -0.10E-04
        92-0-244E+0J
        43-0.245E+03
                                                        0.50E+00 -0.14E-04
0.50E+00 -0.14E-04
                                                                                   -0-12E-04
     " 94-0.245E+03
                                                                                   -0.13E-04
       95-0.240E+03
                                                        0.50E+00 -0.16E-04 -0.15E-04
       90-0.247E+03
                                                        0.49E+00 -0.19E-04 -0.17E-04
0.49E+00 -0.19E-04 -0.18E-04
       97-0-248L+03
 -----98-0-249E+03
                                                            . . .
                                                        0.49E+00 -0.21E-04 -0.20E-04
0.49E+00 -0.22E-04 -0.21E-04
       ~99-0.249E+03
      100-0.2505+03
                                                        0.49E+00 -0.22E-04 -0.20E-04
0.49E+00 -0.21E-04 -0.21E-04
      101-0-251E+03
      102-0-252E+03
                                                        0.50E+00 -0.20E-04 -0.19E-04
      103-0.253E+03
                                                        0.50E+00 -0.18E-04 -0.16E-04
0.51E+00 -0.18E-04 -0.14E-04
 104-0.254E+03
      105-0.255E+03
                                                        0.51E+00 -0.14E-04 -0.12E-04
0.53E+00 -0.13E-04 -0.52E-05
      106-0.250E+03
   ---107-0.258E+03
```

# "THE FOLLOWING ARE PARAMETERS OF THE NATURAL SYSTEM"

```
SPIZED
                                                                 N DEF
                                                                              S DEF
אטטא 🛉
            ALPHA
                                                                       0.44E-04 -0.26E-04
0.42E-04 -0.23E-04
0.34E-04 -0.25E-04
0.34E-04 -0.25E-04
        43-0.1881+03
                                                        0.505+00
                                                        0.51E+U0
        44-0.167E+03
                                                        0.51E+00
0.51E+00
        45-0.187£+03
      ~46-0.186E+03
                                                      47-0 . 185E+03
        48-0-1855+03
        49-0-164 0+03
     50-0.183E+03
                                                                                      0-43E-U5
                                                                       0.17E-04
0.20E-04
                                                        0.4 bE+00
        51-0.1835+03
                                                                                   0-28E-05
                                                        0.475 +00
        52-0 · 184E+03
                                                      0.47E+00 0.26E-04 -0.32E-05
-0.46E+00 0.34E-04 -0.13E-04
0.45E+00 0.41E-04 -0.13E-04
        53-0.1606+03
    54-0.189E+03
                                                                       0.42E-04 -0.96E-05
0.33E-04 -0.66E-06
                                                        0.45E+00
        50-0-1925+03
        57-0.191 E+03
                                                        0.44E+00
 58-0-190E+03
                                                       "0.43E+00" 0.36E-04 '0.84E-05
                                                                                    0-10E-04
0-26
                                                        0.421+00
0.41E+00
                                                                       0.35E-04
0.34E-04
        59-0-1906+03
        60-0.1916+03
                                                                      0.32E-04 0.30E-04
0.32E-04 0.33E-04
0.28E-04 0.35E-04
        61-0-191E+03
                                                        0.41E+00
                                                      0.40E+00
    ~~~~62-0 • 193E+03
                                                        0-40E+00 -
        CO+3 461.0-50
                                                      0.40E+00 0.12E-04 0.29E-04
0.40E+00 0.53E-05 0.21E-04
0.40E+00 0.53E-05 0.21E-04
0.40E+00 0.90E-06 0.80E-05
0.40E+00 -0.11E-04 -0.12E-04
0.41E+00 -0.14E-04 -0.28E-04
        04-0.190E+03
        65-0-198E+03
       ·66-0。200E+03
        67-0 - 202E+03
        08-0.204E+03
                                                       0.41E+00 ~0.1:E-04 ~0.42E-04
0.42E+00"=0.10E-04 ~0.50E-04
        69-0.200E+03
       70-0.208E+03
                                                        U.43E+00 -U.46E-05 -U.52E-04
        71-0.211 =+03
                                                        0.44E+00 0.18E-05 -0.50E-04
0.45E+00 -0.13E-04 -0.38E-04
0.47E+00 -0.19E-04 -0.27E-04
0.48E+00 -0.10E-04 -0.20E-04
        72-0.213E+03
        73-0.215E+03
        74-0.218E+03
        75-0-220E+03
                                                        0.49E+00 -0.16E-04 -0.12E-04
0.50E+00 -0.18E-04 -0.53E-05
        70-0 -222E+03
        77-0.223E+03
                                                                     -0.12E-04 -0.26E-06
-0.52E-05 0.33E-05
                                                        0.50E+00 -0.12E-04
0.49E+00 -0.52E-05
78-0.225E+03
        79-0-229E+03
                                                        0.48E+00 -0.23E-05
0.47E+00 -0.52E-05
0.48E+00-0.52E-05
                                                                                     U-11E-04
       80-0.232E+03
                                                                                      0-27E-04
        61-0.236E+03
                                                                                   0.34E-04
 82-0-237E+03
                                                                       0.615-06 0.19E-04
                                                        U-49L+00
        83-0-237L+03
                                                       0.49E+00 0.21E-05 0.83E-05
0.50E+00 0.33E-05 0.66E-05
0.50E+00 0.25E-05 0.46E-05
0.50E+00 0.24E-05 0.27E-05
        84-0.238E+03
        b5-0.239E+03
  86-0.240E+03
       87-0-24UL+U3
                                                       08-0-241E+03
        69-0.2422+03
    90-0-243E+03
       91-0-243E+03
                                                        0.50E+00 -0.84E-05 -0.82E-05
0.50E+00 -0.12E-04 -0.10E-04
        92-0-244E+0J
        43-0.245E+03
                                                        0.50E+00 -0.14E-04
0.50E+00 -0.14E-04
                                                                                   -0-12E-04
     " 94-0.245E+03
                                                                                   -0.13E-04
       95-0.240E+03
                                                        0.50E+00 -0.16E-04 -0.15E-04
       90-0.247E+03
                                                        0.49E+00 -0.19E-04 -0.17E-04
0.49E+00 -0.19E-04 -0.18E-04
       97-0-248L+03
 -----98-0-249E+03
                                                            . . .
                                                        0.49E+00 -0.21E-04 -0.20E-04
0.49E+00 -0.22E-04 -0.21E-04
       ~99-0.249E+03
      100-0.2505+03
                                                        0.49E+00 -0.22E-04 -0.20E-04
0.49E+00 -0.21E-04 -0.21E-04
      101-0-251E+03
      102-0-252E+03
                                                        0.50E+00 -0.20E-04 -0.19E-04
      103-0.253E+03
                                                        0.50E+00 -0.18E-04 -0.16E-04
0.51E+00 -0.18E-04 -0.14E-04
 104-0.254E+03
      105-0.255E+03
                                                        0.51E+00 -0.14E-04 -0.12E-04
0.53E+00 -0.13E-04 -0.52E-05
      106-0.250E+03
   ---107-0.258E+03
```

Table B-3 Potential vorticity equation components for the large-scale cluster (without corrections for position errors).

B-6

Table B-4 DKP and the location of the center of mass for the large-scale cluster (with corrections for position errors). This data is for a geographic coordinate system.

```
A HUUR
                TIME DER DIVAVOR
                                                      RE 5
          44-0.469r-09-0.24.-03 -0.34E-08
45-0.940E-09-0.18E-08 -0.27E-08
40-0.136E-08-0.84E-09 -0.22E-08
   47-0.168E-08-0.22E-09 -0.19E-08 48-0.19E-08 0.93E-10 -0.19E-08
    49-0.227E-08 0.19E-09 -0.21E-08
50-0.196E-08 0.95E-10 -0.19E-08
51-0.417E-09*0.20E-10 -0.40E-09
                                                                     The second se
           52 U.153E-UB U.44E-10
                                                     0.106-09
           53 0.255E-08 0.12E-09
                                                     0-27E-08
   54 0.251E-06 0.73E-10 0.20E-04

55 0.786E-09-0.18E-09 0.61E-09

50-0.195E-08-0.71E-09 -0.27E-08
  57-0.308E-08-0.12E-08 -0.43E-08
58-0.209E-08-0.15E-08 -0.42E-08
59-0.233E-08-0.17E-08 -0.40E-08
          60-0.194E-08-0.17E-06 -0.37E-08
61-0.122E-08-0.17E-08 -0.29E-08
   62-0.775E-09-0.16E-05 -0.24E-00
63 0.309E-09-0.13E-08 -0.10E-08
64 0.105E-00-0.10E-08 0.65E-09
          65 0.249E-08-0.72E-09
66 0.337E-08-0.30E-09
                                                     0-18E-08
                                                     0-31E-08:
    67 0.345E-08 0.12E-08 08 0.312E-08 0.25E-08 0.37E-08 0.37E-08
                                                     0-47E-08
                                                     0.50E-06
    70 0.134E-08 0.40E-08 0.00E-08 0.00E-08 0.55E-08 0.240E-08 0.47E-08 0.55E-08 0.55E-08 0.42E-08 0.60E-09 74-0.134E-08 0.33E-08 0.19E-08 0.19E-08 75-0.215E-08 0.33E-08 0.19E-08
                                                    0-0UE-0H
0-55E-08
    74-0.1342-08 0.332-08 0.19E-08
          70-0.100E-00 0.20E-08
77-0.500E-10 0.15E-08
                                                     0.32E-09
                                                    0-14E-08
0-17E-08
0-70E-09
          78 0.660E-09 0.10E-08 0.17E-08
79 0.456E-10 0.65E-09 0.70E-09
80-0.300E-09 0.15E-09 -0.15E-09
          81 0.317E-09-0.10E-08 -0.72E-09
82 0.682E-09-0.17E-08 -0.97E-09
 63 0.120E-09=0.44E-09 -0.32E-09
84 0.229E-11 0.36E-09 0.37E-09
85 0.406E-11 0.52E-09 0.52E-09
 65-0.223E-09 0.64E-09 0.42E-09
67-0.443E-09 0.70E-09 0.25E-09
68-0.964E-09 0.74E-09 -0.23E-09
                                                  0-25E-09
    09-0.636E-09 0.74E-09 0.10E-09
90-0.456E-09 0.76E-09 0.30E-09
91-0.929E-09 0.74E-09 -0.19E-09
      92-0.100E-08 0.69E-09 -0.31E-09
          93-0.912E-09 0.66E-09 -0.26E-09
         94-0.493E-09 0.60E-09
95-0.487E-09 0.56E-09
96-0.641E-09 0.50E-09
                                                     0.10E-09
                                                   0.08E-10
                                                  -0.34E-09
         97-0.593E-09 0.45E-09 -0.14E-09
98-0.523E-09 0.42E-09 -0.10E-09
99-0.570E-09*0.40E-09 -0.17E-09
                          ----
     100-0.125E-0910.36E-09
                                                    0-23E-09
                                                                                           0-41E-09
        102 0.336E-09 0.30E-09
103 0.765E-09 0.26E-09
                                                    U-64E-09
                                                    0 - 1 0F - 0N
        104 0.580E-09 0.27E-09
105 0.709E-09 0.20E-09
100 0.165E-08 0.21E-09
                                                    0-85E-09
                                                     0.906-09
                                                    U-19E-UH
```

HUUR	DIVER	· VURTY	N DLF	SDEF	X CENTER	Y CENTER	
•							
1,	3-0.387E-04	. 0 - 32F - 04	0.365-04	-0.38E-04	0.115+06	0.15E+06	
	44-0.270E-04			-0.392-04	0-115+06	U-14E+06	
	5-0-168E-04		0.32E-04	-U-37E-04	0-10E+00	0-14E+06	
** ***	10-0.836E-05	0-25E-04	0-29E-04	-0.33E-04	0-10E+00	0-14E+00	
	7-0.237E-05			-0-27E-04"		0 14E+06	
	18 0.100E-05 19 0.233E-05			-0.20E-04 -0.12E-04	0 - 1 0E + 0 o	0-14E+00 0-13E+00	
	0 0.132E-05			-0.29E-05	0.10E+06	0-13E+06	
	51 0.301 E-06		0-19E-04		0-10E+06	0.13E+06	• • •
	2 0.638E-UC		0-22E-04		0-105+00	U -1 3E+06	
	53 0.164E-05 54 0.862E-06			-0.93E-05	0.10E+00	0 • 1 3E +06 0 • 1 3E +06	
	5-0.198E-05			-0.30E-04		U-12E+06	•
	CU-36136-U5			-0.28E-04	0 • 1 UE+Oo	0-12E+00	
	7-0-163E-04			-U-10E-04	0 - 1 0E + 0 6	0-12E+0b	•
	ンB-0・2J9L-04 ンB-0・310E-04		0.42F04 0.46E-04	-0.53E-05	0.10E+06 0.10E+06	0 •1 2E +06 0 •12E +06	
	79-0-310E-04 70-0-3/8E-04		0.51E-04	0-13E-04	0.10E+06	U-12E+06	
	1-0.438E-04		0.56E-04	0-21E-04	0-10E+00	0-12E+0b	
	2-0-4691-04		0-61E-04		0-10E+06	0-11E+00	
T	3-0.503L-04		0.62E-04 0.51E-04		"0.10E+06 0.10E+06	0-11E+06 0-11E+06	
	54-0•400E-04 5-0•282E-04		0.37E-04	0.39E-04	0.10E+06	0-11E+00	
t	6-0-111E-04	-0-26E-04	0-15E-04	0-14E-04	0.10E+06	0 -11E+06	
	7 0.374E-04				0.99E+05	0.11E+06	
	0.529E-04		-0.60E-04		0.99E+05	0-11E+06	
	0 0 595E-04				0.98E+05 0.97E+05	0.10E+06	
	1 0.545E-04	0 40E-04	-0.62E-04	-0.27E-04			market and contract to the second
7	12 0.485E-U4	U-45L-04	-0.54E-04	~0.27E~04	0.90E+05	0-10E+06	
	3 0.509E-04				0.95E+05	0.99E+05	
	/4 0.440L-04 /5 0.334E-04			0-13E-04 0-71E-05	0.94E+05 0.93E+05	0 •97E+05 0 •96E+05`	
	0 0.279E-04			U-15E-04	0.92E+05	U.95E+05	
	7 0.212E-04			U-19E-04	0.91E+05	0.93E+05	
	8 0.139E-04		-0.19E-06	0-13E-04	0.89E+05	0-92E+05	
	9 0.882E-05		0-41E-05	0.50E-05 -0.58E-06	`0.88E+05 0.87E+05	0.91E+05 0.90E+05	
	10 0.209E-05 11-0.145E-04			-0.53E-05	0.85E+05	0.89E+05	
	2-0-227E-04			-0.10E-04	0.84E+05	0.88E+05	
	3-0.597E-05			-0.93E-05	0.82E+05	0.87E+05	
	4 0.448E-05			-0.59E-05	0.81E+05 0.79E+05	0 -86E+05 0 -85E+05	
	5 0.700E-05 6 0.880E-05			-0.65E-05	0.75E+05	0 -84E+05	
	7 0.962E-05			-0.37E-05		0.83E+05	•
· 6	8 U-105E-04	-0 •29E-05	0.12E-00	-0.50E-00	0.75E+U5	0 -82E+05	
	9 0.111E-04		0.23E-07		0.73E+05	0	
-	0 0.114E-04: 01 0.115E-04:		-0.90E-05	0 •49E~05 0 •85E~05		0.80E+05	
-	2 0.1141-04			0-12E-04	0.08E+05	U.79E+05	
	3 0.114L-U4			0.10E-04	0.67E+05	U.7EE+U5	
	4 0-108E-04		-0.42E-06	0+19E-04	0.65E+05	0.77E+05	
	5 0.102E-04 6 0.957E-05		-0.47E-06 0.55E-06	0-20E~04 0-23E~04	0.63E+05	0.77E+05 0.76E+05	
	7 0.9191-05		0.17E-05	U-20E-04	0.60E+05	U.75E+05	
Ý	8 0.877E-05	-0.29E-04	0+20E-05	0-27E-04	0 - 5 ხE+05	0.75E+05	
, ,	9 0.869E-05	-0.32E-04	0.26E-05	0.30E-04	0.57E+05	0.74E+05	
	•			***	•	, the same of the same	
1 (	0 U.79HE-05-	-1) - 3u+ -1)e	0.41E-05	0-31E-04	0.55E+05	0 -73E+05	İ
	1 0.717E-05		0.49E-05	0.30E-04	0.53E+05	0.73E+05	
1 0	2 0.6591-05-	-0 •33E -04	0.53E-05	0.30E-U4	0.52E+05	0.72E+05	
	J 0.5936-05-		0.63E-05	0.27E-04	0 -50E+05	0.72E+05	
	4 0.523E-05. 5 0.376E-05.		0.72E-05 0.89E-05	0 • 24E <del>- 0</del> 4 0 • 22E <del>- 0</del> 4	0.48E+05 0.47E+05	0.71E+05 0.71E+05	
	0 0.307E-05		0.93E-05	U-18E-04	0-45E+05	0.70E+05	Fi
	7 0.3066-05-		0.906-05	0-10E-04	0 • 4 JE+05	U .7UE +05	1.
			P	L_Q .			

ز.

Table B-4 DKP and the location of the center of mass for the large-scale cluster (with corrections for position errors). This data is for a geographic coordinate system.

Table B-5 DKP for the large-scale cluster (with corrections for position errors). This data is for a natural coordinate system.

HUUR	DIVER	· VURTY	N DLF	SDEF	X CENTER	Y CENTER	
•							
1,	3-0.387E-04	. 0 - 32F - 04	0.365-04	-0.38E-04	0.115+06	0.15E+06	
	44-0.270E-04			-0.392-04	0-115+06	U-14E+06	
	5-0-168E-04		0.32E-04	-U-37E-04	0-10E+00	0-14E+06	
** ***	10-0.836E-05	0-25E-04	0-29E-04	-0.33E-04	0-10E+00	0-14E+00	
	7-0.237E-05			-0-27E-04"		0 14E+06	
	18 0.100E-05 19 0.233E-05			-0.20E-04 -0.12E-04	0 - 1 0E + 0 o	0-14E+00 0-13E+00	
	0 0.132E-05			-0.29E-05	0.10E+06	0-13E+06	
	51 0.301 E-06		0-19E-04		0-10E+06	0.13E+06	• • •
	2 0.638E-UC		0-22E-04		0-105+00	U -1 3E+06	
	53 0.164E-05 54 0.862E-06			-0.93E-05	0.10E+00	0 • 1 3E +06 0 • 1 3E +06	
	5-0.198E-05			-0.30E-04		U-12E+06	•
	CU-36136-U5			-0.28E-04	0 • 1 UE+Qo	0-12E+00	
	7-0-163E-04			-U-10E-04	0 - 1 0E + 0 6	0-12E+0b	•
	ンB-0・2J9L-04 ンB-0・310E-04		0.42F04 0.46E-04	-0.53E-05	0.10E+06 0.10E+06	0 •1 2E +06 0 •12E +06	
	79-0-310E-04 70-0-3/8E-04		0.51E-04	0-13E-04	0.10E+06	U-12E+06	
	1-0.438E-04		0.56E-04	0-21E-04	0-10E+00	0-12E+0b	
	2-0-4691-04		0-61E-04		0-10E+06	0-11E+00	
T	3-0.503L-04		0.62E-04 0.51E-04		"0.10E+06 0.10E+06	0-11E+06 0-11E+06	
	54-0•400E-04 5-0•282E-04		0.37E-04	0.39E-04	0.10E+06	0-11E+00	
t	6-0-111E-04	-0-26E-04	0-15E-04	0-14E-04	0.10E+06	0 -11E+06	
	7 0.374E-04				0.99E+05	0.11E+06	
	0.529E-04		-0.60E-04		0.99E+05	0-11E+06	
	0 0 595E-04				0.98E+05 0.97E+05	0.10E+06	
	1 0.545E-04	0 40E-04	-0.62E-04	-0.27E-04			market and contract to the second
7	12 0.485E-U4	U-45L-04	-0.54E-04	~0.27E~04	0.90E+05	0-10E+06	
	3 0.509E-04				0.95E+05	0.99E+05	
	/4 0.440L-04 /5 0.334E-04			0-13E-04 0-71E-05	0.94E+05 0.93E+05	0 •97E+05 0 •96E+05`	
	0 0.279E-04			U-15E-04	0.92E+05	U.95E+05	
	7 0.212E-04			U-19E-04	0.91E+05	0.93E+05	
	8 0.139E-04		-0.19E-06	0-13E-04	0.89E+05	0-92E+05	
	9 0.882E-05		0-41E-05	0.50E-05 -0.58E-06	`0.88E+05 0.87E+05	0.91E+05 0.90E+05	
	10 0.209E-05 11-0.145E-04			-0.53E-05	0.85E+05	0.89E+05	
	2-0-227E-04			-0.10E-04	0.84E+05	0.88E+05	
	3-0.597E-05			-0.93E-05	0.82E+05	0.87E+05	
	4 0.498E-05			-0.59E-05	0.81E+05 0.79E+05	0 -86E+05 0 -85E+05	
	5 0.700E-05 6 0.880E-05			-0.65E-05	0.75E+05	0 -84E+05	
	7 0.962E-05			-0.37E-05		0.83E+05	•
· 6	8 U-105E-04	-0 •29E-05	0.12E-00	-0.50E-00	0.75E+U5	0 -82E+05	
	9 0.111E-04		0.23E-07		0.73E+05	0	
-	0 0.114E-04: 01 0.115E-04:		-0.90E-05	0 •49E~05 0 •85E~05		0.80E+05	
-	2 0.1141-04			0-12E-04	0.08E+05	U.79E+05	
	3 0.114L-U4			0.10E-04	0.67E+05	U.7EE+U5	
	4 0-108E-04		-0.42E-06	0+19E-04	0.65E+05	0.77E+05	
	5 0.102E-04 6 0.957E-05		-0.47E-06 0.55E-06	0 -20E-04 0 -23E-04	0.63E+05 0.62E+05	0.77E+05 0.76E+05	
	7 0.9191-05		0.17E-05	U-20E-04	0.60E+05	U.75E+05	
Ý	8 0.877E-05	-0.29E-04	0+20E-05	0-27E-04	0 - 5 ხE+05	0.75E+05	
, ,	9 0.869E-05	-0.32E-04	0.26E-05	0.30E-04	0.57E+05	0.74E+05	
	•			***	•	, the same of the same	
1 (	0 U.79HE-05-	-1) - 3u+ -1)e	0.41E-05	0-31E-04	0.55E+05	0 -73E+05	İ
	1 0.717E-05		0.49E-05	0.30E-04	0.53E+05	0.73E+05	
1 0	2 0.6591-05-	-0 •33E -04	0.53E-05	0.30E-U4	0.52E+05	0.72E+05	
	J 0.5936-05-		0.63E-05	0.27E-04	0 -50E+05	0.72E+05	
	4 0.523E-05. 5 0.376E-05.		0.72E-05 0.89E-05	0 • 24E <del>- 0</del> 4 0 • 22E <del>- 0</del> 4	0.48E+05 0.47E+05	0.71E+05 0.71E+05	
	0 0.307E-05		0.93E-05	U-18E-04	0-45E+05	0.70E+05	Fi
	7 0.3066-05-		0.906-05	0-10E-04	0 • 4 JE+05	U .7UE +05	1.
			P	L_Q .			

ز.

# "THE FOLLOWING ARE PARAMETERS OF THE MATURAL SYSTEM

A HOUR ALPHA 43-0.168E+03 44-0.187L+03 45-0.167E+03

SPEED

N DEF S DEF

0.50E+00 0.45E-04 -0.29E-04 0.51E+00 0.43E-04 -0.29E-04 0.51E+00 0.40E-04 -0.29E-04

Table B-6 Potential vorticity equation components for the large-scale cluster (with corrections for position errors).

### THE FOLLOWING ARE PARAMETERS OF THE MATURAL SYSTEM

```
SPEED
                                                           N DEF
                                                                        S DEF
4 HOUR
           AL PHA
       43-0-1685+03
                                                    0.5UE+UU
                                                                 0.45E-04 -0.26E-04
                                                                 0.43E-04 -0.29E-04
0.40E-04 -0.29E-04
       44-0-187L+03
                                                    0.51E+00
                                                    0-51E+00
       45-0-187E+03
 40-0.180E+03
                                                                 0.36E-04 -0.26E-04***
0.31E-04 -0.22E-04
                                                    0.51E+00
       4/-U-165E+03
                                                    0-518+03
                                                                 0.27E-04 -0.16E-04
0.23E-04 -0.91E-05
                                                    0-50E+00
       48-0-1856+03
       49-0-184L+03
                                                    0.50E+00
 ~ 50-0.183E+03
                                                                 0.19E-04 -0.91E-06
                                                    0-445+00
                                                    0.48E+00
                                                                 0.18E-04
       51-0.1631+03
                                                                               0-40C-US
                                                                 0-21E-04
                                                    0-47E+00
                                                                               0-296-05
       52-0.184L+03
                                                   0.47E+00 0.28E-04 -0.34E-05
0.46E+00 0.36E-04 -0.98E-05
0.45E+00 0.45E-04 -0.14E-04
0.45E+00 0.46E-04 -0.11E-04
       53-0-1 855+03
       54-0.109E+03
       55-0-191E+03
       56-0-1925+03
                                                                 0.43E-04 -0.75E-06
0.41E-04 0.97E-05
       57-0 - 191 E+03
                                                    0.44E+00
    -- '58-0-1906+03
                                                   0.43E+00
                                                                 0.43E-04
0.43E-04
0.43E-04
                                                    0.425+00
                                                                              0-19E-04
       39-0.190E+03
       60-U-191E+03
                                                    0.41L+00
                                                                              0.30E-04
                                                    0.415+00
                                                                               0-41E-04
       01-0-1416+03
                                                                 0.43E-04
0.38E-04
0.24E-04
0.12E-04
                                                    0-40E+00
                                                                              0.51E-04
0.62E-04
       02-0-193E+03
       03-0-194E+03
                                                   0-40E+00
                                                   0-406+00
                                                                               0.6DE-04
       04-0.196E+03
       65-0-198E+63
                                                    0.4UE+00
                                                                               0-47E-04
                                                               -0-23E-05 0-21E-04
     ~ 60-0-200E+03
                                                   0.40E+00
                                                   0.41E+00 -0.28E-04 -0.30E-04
0.41E+00 -0.28E-04 -0.56E-04
       67-0-202E+03
       D8-0-204E+03
                                                   U-41E+00 -0.2:E-04 -U.70E-04
U-42E+00 -0.15E-04 -0.72E-04
       69-0.206E+03
       70-0.208£+03
                                                   0.44E+00 -0.60E-05 -0.68E-04
0.44E+00 0.22E-05 -0.61E-04
       71-0-211E+03
       72-0-2135+03
                                                   0.45E+00 -0.15E-04 -0.44E-04

0.47E+00 -0.21E-04 -0.30E-04

0.45E+00 -0.11E-04 -0.22E-04

0.49E+00 -0.17E-04 -0.13E-04

0.50E+00 -0.19E-04 -0.56E-05
       73-0-2155+03
       74-0.21dE+03
       15-0.220E+03
       76-0.222E+03
       77-0.223E+03
                                                   0.50E+00 -0.13E-04 -0.27E-06
       76-0.225E+03
                                                                              0.35E-05
                                                   0.49E+00 -0.55E-05
       74-0.224E+03
                                                   0.48E+00 -0.24E-05
       80-0-232E+03
                                                                              0-11E-04
                                                   0.47E+00 -0.55E-05
       81-0.230E+03
                                                                              0.295-04
                                                   0.48E+00 -0.56E-05
                                                                              0.37E-04
       62-0.237c+03
                                                                 0.01E-00
                                                                              0-21E-04
                                                   0.49E+00
       63-0-23/L+03
                                                                 0-23E-05
                                                                              0.9Ut -05
       84-0-238E+03
                                                   0.45E+00
                                                   0.50E+00 0.36E-05
0.50E+00 0.27E-05
       65-0-234E+03
                                                                              0.72E-05
                                                                              0.50E-05
       80-0.240E+03
                                                   0.50E+00
                                                                 0.26E-05
0.41E-06
                                                                              0.296-05
       67-0-240E+03
                                                                              0.405-06
                                                   0-50E+00
       68-0.241E+03
                                                   0.50E+00 -0.36E-05 -0.24E-05
0.50E+00 -0.35E-05 -0.36E-05
       69-0.242L+03
       90-0-243E+03
                                                   0.50E+00 -0.59E-05 -0.63E-05
0.50E+00 -0.90E-05 -0.87E-05
       91-0-2435+03
       92-0.244E+05
                                                   0-50E+00 -0-12E-04 -0-11E-04
       43-0.245E+03
                                                   0.50E+00 -0.14E-04 -0.13E-04
0.50E+00 -0.14E-04 -0.14E-04
       44-0-245E+03
       45-0.240L+03
                                                   0.506+00 -0.17E-04 -0.16E-04
0.496+00 -0.19E-04 -0.17E-04
       90-0.247L+03
       97-0-248E+U3
       98-0-2496+03
                                                   0.49E+00 -0.20E-04 -0.19E-04
                                                   0-49E+00 -0-22E-04 -0-21E-
       99-0-249E+03
     100~0.250E+03
                                                   0-44L+00 -0.23E-04 -0.21E-04
                                                   0.49E+00 -0.22E-04 -0.21E-04
0.49E+00 -0.22E-04 -0.21E-04
     101-0-251E+03
     102-0.252E+03
                                                   0.50E+00 -0.20E-04 -0.19E-04
     103-0-253E+03
                                                   0.50E+00 -0.19E-04 -0.17E-04
     1 U4-U . 254 E+US
                                                   0.51E+00 -0.19E-04 -0.15E-04
0.51E+00 -0.17E-04 -0.12E-04
     105-0.255E+0J
     100-0.250L+03
     107-0.258E+03
                                                   0.53E+00 -0.13E-04 -0.53E-05
```

POT. VORT. EUN. COMP. S

HOUR TIME DER DIV\*VOR KL5

44-0.437E-09-0.30E-08 -0.35E-08 45-0.931E-09-0.18E-08 -0.28E-03 46-0.136E-08-0.88E-09 -0.23E-08 47-0.173E-08-0.24E-09 -0.20E-08 46-0.206E-08 0.98E-10 -0.20E-08

## 'POT. VORT. EUN. COMP. S

\* HOUR TIME DER DIV\*VOR KL5 44-0.437E-09-0.30E-08 -0.35E-08 45-0.931E-09-0.18E-08 -0.28E-09 46-0.138E-08-0.88E-09 -0.23E-08 47-0.173E-08-0.24E-09 -0.20E-08 45-0.200E-08 0.98E-10 -0.20E-08 49-0.238E-08 0.20E-09 -0.22E-08 50-0.207E-08 0.10E-09 51-0.447E-09 0.21E-10 52 0.102E-08 0.46E-10 -0.20E-03 -0.43E-09 0-17E-06 53 0-274E-08 0-13E-09 0-29L-06 54 0.273E-08 0.79E-10 55 0.911E-09-0.20E-09 J-286-06 0.71E-03 -0-24E-Un 56-0.208E-08-0.80E-09 57-0.343E-08-0.14E-08 -0.4&E-04 58-0.317E-08-0.18E-08 -0.44E-04 59-0.303E-08-0.20E-08 -0.50E-0B 00-0.296E-00-0.20E-08 ~U\_49L-08 01-0.201E-08-0.18E-08 -0.45E-08 63-0.163E-08-0.11E-08 -0.45E-08 -0.27E-08 64 0.134E-08-0.86E-09 0.486-09 65 0.442E-08-0.88E-09 0.35E-08 0.72E-08 0.11E-07 66 0.779E-08-0.59E-09 67 0.767E-08-0.33E-08 68 0.492E-08 0.57E-08 69 0.235E-08 0.73E-08 70 0.334E-09 0.75E-08 71-0.200E-09:0.68E-08 0.11E-07 0.97E-Uis 0.79E-08 0.66E-08 and a series of a second of the second of the second of the second of the second of the second of the second of 72-0.395E-08 0.60E-08 0.21E-08 -0.97E-09 73-0.589E-08 0.49E-08 74-0.100E-08 0.31E-08 75-0.777E-09 0.28E-08 0.20E-08 0.21E-08 0.34E-09 76-0-1/8c-68 0.21t -08 /7-0.559E-10 0.15E-08 0.15L-08 78 0.702E-09 0.11E-08 0.185-08 79 0.495E-10 0.68E-09 U.73E-09 00-0-317E-09 0-10E-09 -0-106-09 al 0.333E-09-0.11E-08 -0.76E-09 02 0.7281-09-0.18E-08 -0-11E-08 83 0.130E-09-0.4HE-09 -0.35E-09 84 0.333E-11 0.40E-09 85 0.481E-11 0.5nE-09 0-40E-09 0.57E-09 87-0.480E-09 0.70E-09 0.40E-09 0.28E-09 88-0.104E-08 0.80E-09 89-0.681E-09 0.79E-09 -0.24E-09 0.11E-09 0.33E-09 90-0-484E-09 0-81E-09 91-0-984E-09 0.78E-09 -0-20E-09 42-0-106E-08 0-73E-09 -0-33E-09 93-0.952E-09 0.68E-09 -0.27E-09 94-0.502E-09 0.62E-09 0.12E-09 95-0.493E-09 0.57E-09 0.62E-10 90-0.864E-U9 0.51E-09 ーひょうちとーひず 97-0.000E-09 0.46E-09 -0.14E-09 98-0.524E-09 0.43E-09 -0.92E-10 99-0.571E-09 0.40E-09 -0.17E-09 ز 100-0.109E-09 0.36E-09 0.25E-09 101 0-103E-09 0-33E-09 0.43E-09 0.07E-09 0.11E-06 102 0.365E-09 0.30E-09 103 0.804E-09 0.24E-09

0.88E-09

0.94E-09

0.19E-08

104 0.608E-09 0.27E-09 105 0.737E-09 0.20E-09

106 0.1/0E~08 0.21E-09

Table B-7 DKP and the location of the center of mass for the small-scale cluster (without corrections for position errors). This data is for a geographic coordinate system.

HOUR	DIVER	YTECV	N DEF	S DEF	X CENTER	Y CENTER
14 15 16 17 18 19 20 21 223 24 25 26 27 28 30 31 32 33	-0.106 = -02 - 0.347 = -04 - 0.234 = -04 - 0.234 = -04 - 0.519 = -04 - 0.549 = -04 - 0.29 = -04 - 0.29 = -04 - 0.314 = -05 - 0.537 = -06 - 0.517 = -05 - 0.5	0.36E -03 0.46E -04 0.46E -04 0.16E -04 0.27E -04 0.34E -04 0.41E -04 0.41E -04 0.50E -04 0.50E -04 0.50E -04 0.36E -04 0.36E -04 0.16E -05 0.12E -05 0.38E -05 0.13E -05 0.13E -04 0.15E -04 0.15E -04 0.15E -04 0.15E -04	-0.000-03 0.160-03 0.27E-04 -0.36E-04 -0.150-04 -0.14E-04 -0.14E-04 0.230-04 0.230-04 0.430-04 0.520-04 0.430-04 0.520-04 0.430-04 0.520-04 0.430-04 0.520-04	0.93E-03 -0.275-03 -0.10E-03 -0.10E-04 -0.52E-04 -0.45E-04 -0.35E-04 -0.28E-04 -0.28E-04 -0.25E-05 0.32E-05 0.82E-05 0.82E-05 0.82E-04 0.15E-04 0.15E-04 0.15E-04 0.22E-04 0.22E-04	0.94E+05 0.96E+05 0.96E+05 0.97E+05 0.99E+05 0.10E+06 0.10E+06 0.10E+06 0.10E+06 0.10E+06 0.10E+06 0.10E+06 0.10E+06 0.10E+06 0.10E+06 0.10E+06 0.10E+06 0.10E+06	0.22E+06 0.21E+06 0.21E+06 0.21E+06 0.20E+06 0.20E+06 0.19E+06 0.19E+06 0.19E+06 0.19E+06 0.18E+06 0.18E+06 0.18E+06 0.18E+06 0.17E+06 0.16E+76
36: 37: 38: 39: 40: 41: 42:	-0.286E-04 -0.343E-04 -0.283E-04 -0.103E-04- 0.250E-04-	0.15E-04 0.11E-04 0.15E-05 0.17E-04 0.39E-04 0.65E-04 0.33E-04	-0.57E-04 -0.55E-04 -0.39E-04 -0.60E-05 0.51E-04 0.10E-03 0.13E-03 0.12E-03	0.17F-04 0.13E-04 0.10E-05 -0.15E-04 -0.36E-04 -0.50E-04 -0.59E-04 -0.61E-04	0 - 1 0E + 06 0 - 1 0E + 06	0.16E+06 0.16E+06 0.16E+06 0.15E+06 0.15E+06 0.15E+06 0.15E+00

```
71 0.124E-03-0.11E-03
72 0.862E-04-0.61E-04
                           -0.34E-04
                                         0.450-04
                                                     0.88E+05
                                                                 0.10E+06
                                                                 0.10E+06
                            -0.122-04
                                         0.130-04
                                                     0.87E+05
                                        -0.117-04
-0.307-04
                             0.695-05
                                                     0.865+05
                                                                 0.10E+00
 73 0.456F-04-0.30E-04
                                                     0.855+05
                                                                 0.995+05
                             0.335-04
 74 0.660E-06-0.13E-04
                                                     0.835+05
                                        -0.84E-05
                                                                 0.98E+05
 75-0.441E-04-0.57E-04
                             0.49E-04
 76-0.102E-03-0.57E-05
77-0.745E-03 0.13E-03
                             0.845-04
                                        -0.11E-03
                                                     0.82E+05
                                                                 0.96E+05
                             0.495-03
                                        -0.03E-03
                                                                 0.95E+05
                                                     0.81E+05
                            -0.27E-03
                                         0.245-03
                                                                 0.94E+05
 78 0.362E-03 0.12E-04
79 0.651E-04-0.21E-04
                                                     0.79E+05
                                                                 0.93E+05
                                         0.68E-04
                            -0.56E-04
                                                     0.735+05
 80-0.890E-04-0.73E-04
                             0.50E-04
                                        -0.135-04
                                                     0.765+05
                                                                 0.92E+05
                                        -0.13E-04
                             0.255-03
                                                     0.75E+05
                                                                 0.90E+05
 81-0.1365-03-0.262-03
82-0.7876-04-0.295-03
83-0.8426-04-0.246-03
                             0.265-03
                                         0.892-04
                                                     0.735+05
                                                                 0.895+05
                                                                 0.89E+05
                                         0.175-03
                                                     0.72E+05
                             0.24E-03
                                                     0.70E+05
                             0.150-03
                                         0.250-03
                                                                 0.8SE+05
 84-0.355E-03-0.36E-03
                                        -0.147-03
0.915-04
-0.235-03
 85 0.317E-03-0.32E-03
86-0.172E-04-0.45E-03
                             0.230-03
                                                     0.68E+05
                                                                 0.87E+05
                                                     0.665+05
                                                                 0.835+05
                             0.475-03
                                                     0.65E+05
                                                                 0.85E+05
                             0.18E-03
 37-0.109E-03-0.30E-04
                            -0.12E-03
 88 0.127E-03 0.12E-03
                                        -0.74E-04
                                                     0.63E+05
                                                                 0.84E+05
 89 0.510E-03-0.48E-03
                             0.19E-03
                                         0.60E-03
                                                     0.61E+05
                                                                 0.83E+05
                             0.105-03
                                         0-175-04
                                                     0.59E+05
 90 0.358E-04-0.11E-03
                                                                 0.83E+05
                                        -0.225-03
                                                     0.58E+05
                             0.28E-03
                                                                 0.82E+05
 91-0.279E-03-0.18E-03
                            -0.45E-04
0.10E-03
 92 0.502E-03-0.15E-03
                                         0.50E-03
                                                     0.56E+05
                                                                 0.81E+05
 93 0.107E-03-0.16E-03
                                         0.145-03
                                                     0.545+05
                                                                 0.81E+05
                                                     0.535+05
 94 0.163F-03 0.345-04
                            -0.155-03
                                         0.155-03
                                                                 0.805+05
                            -0.398-04
                                         0.83E-04
                                                     0.51E+05
                                                                 0.79E+05
 95 0.670E-04 0.35E-07
                                                                 0.798+05
                             0.316-04
                                         0.65E-04
    0.239E-04-0.67E-04
                                                     0.49E+05
                             0.64E-04
 97-0.791E-04-0.113-03
                                        -0.31E-04
                                                     0.48E+05
                                                                 0.78E+05
                                        -0.69E-05
 98-0.116F-04-0.295-03
                             0.24E-03
                                                     0 -4 65 +05
                                                                 0.775+05
 99 0.359E-04-0.52E-04
                                                     0.44E+05
                                                                 0.77E+05
                             0.35E-04
                                         0.13E-03
100-0.178E-04-0.93E-04
                             0-49E-04
                                         0.71E-04
                                                     0.43E+05
                                                                 0.77E+05
101 0.1472-04-0.175-03
102-0.1922-05-0.135-03
103 0.3425-04-0.065-04
                             0.116-03
                                        -0.245-05
                                                     0.4 IE+05
                                                                 0.76E+05
                             0.621-04
0.11E-03
                                        -0.935-05
                                                     0 -405+05
                                                                 0.75E+05
                                        -0.39E-04
                                                     0.38E+05
                                                                 0.758+05
                                        -0.89E-04
                                                     0.37E+05
164-0.199E-04-0.28E-04
105-0.829E-04-0.63E-04
                                                                 0.748+05
                             0-94L-04
                                                     0.355+05
                                                                 0.746+05
                             0.435-04 -0.116-03
                             0 . 0 3E - 04
                                                                 0.745+05
                                       -0.303-03
                                                     0.335+05
106-0.365E-03 0.23E-04
107 0.1135-02-0.46E-03
                             0.216-03
                                         0.13F-02
                                                     0.31E+05
                                                                 0.73E+05
```

Table B-7 continued.

)

J

J

Э

7

Table B-8 DKP and the location of the center of mass for the small-scale cluster (with corrections for position errors). This data is for a geographic coordinate system.

Table B-8 DKP and the location of the center of mass for the small-scale cluster (with corrections for position errors). This data is for a geographic coordinate system.

Table B-9 DKP and the location of the center of mass for the large-scale cluster using every 4th data point (without corrections for position errors). This data is for a geographic coordinate system.

Y CENTER	0.146+06 0.136+06 0.126+06 0.1166+06 0.1166+06 0.976+05 0.926+05 0.886+05 0.846+05 0.816+05
X CENTER	0.1006 0.1006 0.1006 0.1006 0.9106 0.926 0
S DEF	-00.32E-04 -00.12E-04 -00.12E-04 -00.12E-04 -00.13E-04 -00.39E-05 -00.36E-05 -00.34E-05 -00.34E-05 -00.34E-05 -00.26E-05
N 00F	0.31E-04 0.22E-04 0.37E-04 0.36E-04 0.17E-05 0.25E-05 0.13E-05 0.13E-05 0.25E-05 0.22E-05
V031Y	00.224
DIVER	46-0.166E-04 0.24E-04 50-0.714F-07 0.33E-05 58-0.190E-05 0.43E-05 58-0.183E-04-0.74E-06 65-0.279E-04-0.24E-04 66-0.385E-06-0.63E-05 74-0.314E-04-0.32E-04 74-0.314E-04-0.32E-04 78-0.101E-04-0.13E-05 96-0.496E-05-0.13E-05 96-0.982E-06-05 98-0.982E-06-05-0
HOUR	40000000000000000000000000000000000000

```
75 0.682E-D4 0.88E-04 -0.75E-04
76 0.796E-04 0.43E-05 -0.66E-04
                                                    0.13E-C4
0.87E-C4
                                                                   C.83E+05
                                                                                  0.98E+05
                                                                                  0.96E+05
                                                                   0.82E+05
                                                 C.26E-04
-0.40E-04
  77 0.302E-04-0.52E-05
78-0.611E-04-0.21E-05
                                   -0.20E-C4
                                                                   0.81E+05
                                                                                  0.95E+05
                                                                   0.79E+05
                                     0.45E-04
                                                                                  0.94E+05
                                   0.81E-C4 - C.99E-04
-0.80E-C4 0.21E-04
                                                                                  0.93E+05
 79-0.943E-04 0.30E-04
80 0.142E-03 0.13E-03
                                                                   C. 78E+05
                                                                                  0.92E+05
                                                                   C. 76E+05
                                                    0.30E-05
 81 0.317E-04 0.61E-04
                                                                   0.75E+05
                                                                                  0.90E+05
                                   -0.58E-C4
                                   -0.47E-C4
                                                                   0.73E+05
G.72E+05
      0.145E-04 0.51E-04
0.848E-05 0.25E-04
                                                 -0.16E-C4
-0.17E-G4
                                                                                  0.89E+05
 82
                                                                                  0.89E+05
 83
 84 0.219E-J4 0.23E-J4
85-Q-177E-O4 J-18E-Q4
                                   -0.57E-05
-0.13E-04
                                                                   C. 7 CE+05
                                                                                  0.88E+05
                                                 -0.16E-C4
                                                    C.80E-C5
                                                                   0.68E+05
                                                                                  0.87E+05
 86 0.660E-J6 J.17E-J4
87 J.359E-J4 J.96E-J5
88-0.535E-O4-J.50E-J4
89-0.827E-J4 O.78E-J4
90-0.147E-J4 J.45E-J4
                                   -0.17E-04
-0.59E-C4
0.51E-C4
                                                 -0.34E-05
C.77E-C4
C.31E-04
                                                                   0.66E+05
                                                                                  0.86E+05
                                                                   C. 65E+05
                                                                                  0.85E+05
                                                                   0.63E+05
                                                                                  0.84E+05
                                                                                  0.83E+05
                                   -0.31E-C4 -C.97E-04
                                                                   0.61E+05
                                   -0.42E-04 -0.69E-05
                                                                                  0.83E+05
                                                                   0.59E+05
                                   91 0.489E-04 0.31E-04
92-0.308E-04 0.91E-05
                                                                   0.58E+05
                                                                                  0.82E+05
                                                                   C. 56E+05
                                                                                  0.81E+05
                                                                   0.54E+05
                                                                                  0.81E+05
 93-0.459E-04 0.67E-04
                                   0.80E+05
                                                                   0.53E+05
 94-0.110E-03-0.57E-J4
                                                   C.48E-03
0.23E-03
 95 0.363E-03 0.39E-06
96 J.834E-04-J.23E-03
                                                                                  0.79E+05
                                                                   0.51E+05
                                    0.11E-03
                                                                   0.49E+05
                                                 - C.75E-C4
0.80E-05
0.70E-03
                                                                   C. 48E+05
                                                                                  0.78E+05
 97-0.195E-03-0.28E-03
                                    0.16E-C3
 98 0.135E-04 0.33E-03
99 0.190E-03-0.27E-03
                                   -0.27E-03
0.18E-03
                                                                   0.46E+05
                                                                                  0.77E+05
                                                                                  0.77E+05
                                                                   0.44E+U5
                                  -0.15E-C2
-0.81E-03
                                                   0.22E-C2
0.18E-04
100 0.556E-03 0.29E-02
101-0.112E-JJ J.13E-02
                                                                                  0.77E+05
                                                                   0.43E+05
                                                                   0.41E+05
                                                                                  0.76E+05
                    J.44E-03
J.12E-03
                                                   C • 23E - C4
O • 73E - O4
                                                                  C.40E+05
102 0.442E-05
                                   -0.15E-C3
                                                                                  0.75E+05
                                                                                  0 - 75E + US
103-0.637E-JA
                                   -0.21E-03
                                   -0.6 CE- C4
104 0.127E-D4 0.18E-04
                                                                                  0.74E+05
                                                    0.57E-04
                                                                   0.37E+05
                                                                  0.35E+05
0.33E+05
C.31E+05
135 0.332E-34 3.23E-34
106 3.261E-34-3.16E-35
137-0.166E-04 3.67E-35
                                  -0.16E-04
-0.60E-05
                                                   0.40E-C4
0.22E-04
                                                                                  0.74E+05
                                                                                  0.74E+05
                                  -0.31E-05
                                                                                  0.73E+05
                                                 - C . 20E - C4
```

Table B-8 continued.

2

)

)

Table B-10 DKP for the large-scale cluster using every 4th data point (without corrections for position errors). This data is for a natural coordinate system.

-				
	THE FOLLOWING ARE PARAMETERS	OF THE NATURAL SYSTEM	YSTEM	
Ó	HOUR ALPHA	SPEED	DEF S DE	DEF
. (1	46-0.186E+03 50-0.185E+03 54-0.188E+03	0.50E+00 0.49E+00 0.46E+00	0.37E-04 0.24E-04 0.29E-04	.25E-0 .74E-0
B-19	11111 2000 2000 2000	0.43E+00 0.40E+00 0.40E+00 0.42E+00	0.35E-04 0.26E-04 -0.43E-05 -0.13E-05	44 44 44 44 44 44 44 44 44 44 44 44 44
C	0000	4 4 9 6 4 9 6 9 6 9 6 9 6 9 6 9 6 9 6 9	-0.53E-05 -0.13E-05 0.26E-06	100mm 100mm 100mm 100mm 100mm
C	4-0.245 8-0.249 2-0.252	0.50E+00 0.49E+00 0.50E+00		11E-0 17E-0

Table B-9 DKP and the location of the center of mass for the large-scale cluster using every 4th data point (without corrections for position errors). This data is for a geographic coordinate system.

Y CENTER	0.146+06 0.136+06 0.126+06 0.1166+06 0.1166+06 0.976+05 0.926+05 0.886+05 0.846+05 0.816+05
X CENTER	0.1006 0.1006 0.1006 0.1006 0.9106 0.926 0
S DEF	-00.32E-04 -00.12E-04 -00.12E-04 -00.12E-04 -00.13E-04 -00.39E-05 -00.36E-05 -00.34E-05 -00.34E-05 -00.34E-05 -00.26E-05
N 00F	0.31E-04 0.22E-04 0.37E-04 0.36E-04 0.17E-05 0.25E-05 0.13E-05 0.13E-05 0.25E-05 0.22E-05
V031Y	00.224
DIVER	46-0.166E-04 0.24E-04 50-0.714F-07 0.33E-05 58-0.190E-05 0.43E-05 58-0.183E-04-0.74E-06 65-0.279E-04-0.24E-04 66-0.385E-06-0.63E-05 74-0.314E-04-0.32E-04 74-0.314E-04-0.32E-04 78-0.101E-04-0.13E-05 96-0.496E-05-0.13E-05 96-0.982E-06-05 98-0.982E-06-05-0
HOUR	40000000000000000000000000000000000000

Potential vorticity equation components for the large-scale cluster using every 4th Table B-11

data point	$\overline{}$	ections for po	without corrections for position errors).	3 5 5 5 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7 7
Pot. Vort.	Eqn. Comp. s			
Hour	Time Der	Div*Vor	Res	
	-0.700E-09	-0.60E-11	-0.71E-09	
	-0.167E-09	-0.16E-09	-0.33E-09	
	-0.980E-09	-0.14E-08	-0.24E-08	
	-0.217E-09	-0.16E-08	-0.18E-08	
	0.160E-08	0.24E-09	0.18E-08	
	0.515E-09	0.39E-08	0.44E-08	
	-0.851E-09	0.27E-08	0.19E-08	
	-0.323E-09	0.78E-09	0.46E-09	
	0.126E-10	-0.11E-09	-0.98E-10	
98	-0.294E-09	0.38E-09	0.91E-10	
90	-0.629E-09	0.70E-09	0.75E-10	
94	-0.651E-09	0.58E-09	-0.67E-10	
86	-0.339E-09	0.42E-09	0.83E-10	

Table B-10 DKP for the large-scale cluster using every 4th data point (without corrections for position errors). This data is for a natural coordinate system.

-				
	THE FOLLOWING ARE PARAMETERS	OF THE NATURAL SYSTEM	YSTEM	
Ó	HOUR ALPHA	SPEED	DEF S DE	DEF
. (1	46-0.186E+03 50-0.185E+03 54-0.188E+03	0.50E+00 0.49E+00 0.46E+00	0.37E-04 0.24E-04 0.29E-04	.25E-0 .74E-0
B-19	11111 2000 2000 2000	0.43E+00 0.40E+00 0.40E+00 0.42E+00	0.35E-04 0.26E-04 -0.43E-05 -0.13E-05	44 44 44 44 44 44 44 44 44 44 44 44 44
C	0000	4 4 9 6 4 9 6 9 6 9 6 9 6 9 6 9 6 9 6 9	-0.53E-05 -0.13E-05 0.26E-06	100mm 100mm 100mm 100mm 100mm
C	4-0.245 8-0.249 2-0.252	0.50E+00 0.49E+00 0.50E+00		11E-0 17E-0

Table B-12 DKP and the location of the center of mass for the large-scale cluster using every 4th data point (with corections for position errors). This data is for a geographic coordinate system.

α	
Y CENTER	0.13 EE + 05 0.13 EE + 06 0.12 EE + 06 0.11 EE + 06 0.11 EE + 06 0.97 EE + 05 0.88 EE + 05 0.81 EE + 05 0.81 EE + 05 0.77 EE + 05 0.77 EE + 05
X CENTER	00000000000000000000000000000000000000
S DEF	
N DEF	00000000000000000000000000000000000000
VORTY	
DIVER	
HOUR	40000000000000000000000000000000000000

3

3

Potential vorticity equation components for the large-scale cluster using every 4th Table 8-11

data point		orticity equal rections for p	Potential vorticity equation components for the large- (without corrections for position errors).
Pot. Vort.	. Eqn. Comp. s		
Hour	Time Der	Div*Vor	Res
20	-0.700E-09	-0.60E-11	-0.71E-09
54	-0.167E-09	-0.16E-09	-0.33E-09
58	-0.980E-09	-0.14E-08	-0.24E-08
62	-0.217E-09	-0.16E-08	-0.18E-08
99	0.160E-08	0.24E-09	0.18E-08
70	0.515E-09	0.39E-08	0.44E-08
74	-0.851E-09	0.27E - 08	0.19E-08
78	-0.323E-09	0.78E - 09	0.46E-09
85	0.126E-10	-0.11E-09	-0.98E-10
98	-0.294E-09	0.38E-09	0.916-10
06	-0.629E-09	0.70E - 09	0.75E-10
94	-0.651E-09	0.58E-09	-0.67E-10
86	-0.339E-09	0.42E-09	0.83E-10

DKP for the large-scale cluster using every 4th data point (with corrections for rors). This data is for a natural coordinate system. position errors) Table B-13

SYSTEM

THE NATURAL

P

PARAMET ERS

AR

FOLLOWING

니구

DEF ທ OEF SPEEC 46-0.186E+03 50-0.185E+03 58-0.188E+03 58-0.191E+03 62-0.191E+03 70-0.209E+03 74-0.219E+03 78-0.227E+03 82-0.249E+03 96-0.249E+03 96-0.249E+03 96-0.249E+03 ALPHA HOUR

(

Table B-12 DKP and the location of the center of mass for the large-scale cluster using every 4th data point (with corections for position errors). This data is for a geographic coordinate system.

α	
Y CENTER	0.13 EE + 05 0.13 EE + 06 0.12 EE + 06 0.11 EE + 06 0.11 EE + 06 0.97 EE + 05 0.88 EE + 05 0.81 EE + 05 0.81 EE + 05 0.77 EE + 05 0.77 EE + 05
X CENTER	00000000000000000000000000000000000000
S DEF	
N DEF	00000000000000000000000000000000000000
VORTY	
DIVER	
HOUR	40000000000000000000000000000000000000

3

3

Table B-14 Potential vorticity equation components for the large-scale cluster using every 4th

5													
Votential Vorticity equation components for (with corrections for position errors).	Res	-0.73E-09 -0.35F-09	-0.31E-08	2	23	71E-	0.19E-08	46E-	]][-	0.10E-09	.85	9	0.94E-10
rections for	Div*Vor	-0.64E-11 -0.17F-09	-0.17E-08	-0.18E-08	0.52E-09	0.62E-08	0.31E-08	0.82E-09	-0.12E-09	0.42E - 09	•	.61E-0	0.43E-09
oint (with cor	Time Der	-0.722E-09	-0.142E-08	-0.581E-09	0.237E-08	0.914E-09	-0.120E-08	-0.356E-09	0.121E-10	-0.316E-09	-0.665E-09	-0.672E-09	-0.336E-09
data point	Hour	50 54	58	29	99	70	74	78	85	98	8	94	88

DKP for the large-scale cluster using every 4th data point (with corrections for rors). This data is for a natural coordinate system. position errors) Table B-13

SYSTEM

THE NATURAL

P

PARAMET ERS

AR

FOLLOWING

니구

DEF ທ OEF SPEEC 46-0.186E+03 50-0.185E+03 58-0.188E+03 58-0.191E+03 62-0.191E+03 70-0.209E+03 74-0.219E+03 78-0.227E+03 82-0.249E+03 96-0.249E+03 96-0.249E+03 96-0.249E+03 ALPHA HOUR

(

Y CENTER	00.00000000000000000000000000000000000
X CENTER	00000000000000000000000000000000000000
S DEF	1
N DEF	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
VORIY	00000000000000000000000000000000000000
DIVER	7-0-3-4-4-4-4-4-4-4-4-4-4-4-4-4-4-4-4-4-4
HOUR	-4444444444444444444444444444444444444

Table B-15 DKP and the location of the center of mass for the small-scale cluster using every 4th data point (without corrections for position errors). This data is for a geographic coordinate system.

)

Table B-14 Potential vorticity equation components for the large-scale cluster using every 4th

5													
Votential Vorticity equation components for (with corrections for position errors).	Res	-0.73E-09 -0.35E-09	-0.31E-08	2	23	71E-	0.19E-08	46E-	]][-	0.10E-09	.85	9	0.94E-10
rections for	Div*Vor	-0.64E-11 -0.17E-09	-0.17E-08	-0.18E-08	0.52E-09	0.62E-08	0.31E-08	0.82E-09	-0.12E-09	0.42E - 09	•	.61E-0	0.43E-09
oint (with cor	Time Der	-0.722E-09 -0.178E-09	-0.142E-08	-0.581E-09	0.237E-08	0.914E-09	-0.120E-08	-0.356E-09	0.121E-10	-0.316E-09	-0.665E-09	-0.672E-09	-0.336E-09
data point	Hour	50 54	58	29	99	70	74	78	85	98	80	94	88

Y CENTER	0.21m+06 0.13m+06 0.17m+06 0.17m+06 0.15m+06 0.15m+06 0.12m+06 0.12m+06 0.12m+06 0.12m+06 0.12m+06 0.12m+06 0.12m+06 0.12m+06 0.12m+06 0.12m+06 0.12m+06 0.11m+06 0.95m+05 0.83m+05
X CENTER	0.98
S OCF	0.00
N DEF	0.057c-0033c-0037c
VORIY	0-11-0-0-0-0-0-0-0-0-0-0-0-0-0-0-0-0-0-
DIVER	00-0-0-0-0-0-0-0-0-0-0-0-0-0-0-0-0-0-0
400H	

Table B-16 DKP and the location of the center of mass for the small-scale cluster using every data point (with corrections for position errors). This data is for a geographic coordinate

Y CENTER	00.00000000000000000000000000000000000
X CENTER	00000000000000000000000000000000000000
S DEF	1
N DEF	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
VORIY	00000000000000000000000000000000000000
DIVER	7-0-3-4-4-4-4-4-4-4-4-4-4-4-4-4-4-4-4-4-4
HOUR	-4444444444444444444444444444444444444

Table B-15 DKP and the location of the center of mass for the small-scale cluster using every 4th data point (without corrections for position errors). This data is for a geographic coordinate system.

)

Y CENTER	0.21m+06 0.13m+06 0.17m+06 0.17m+06 0.15m+06 0.15m+06 0.12m+06 0.12m+06 0.12m+06 0.12m+06 0.12m+06 0.12m+06 0.12m+06 0.12m+06 0.12m+06 0.12m+06 0.12m+06 0.11m+06 0.95m+05 0.83m+05
X CENTER	0.98
S OCF	0.00
N DEF	0.057c-0033c-0037c
VORIY	0-11-0-0-0-0-0-0-0-0-0-0-0-0-0-0-0-0-0-
DIVER	00-0-0-0-0-0-0-0-0-0-0-0-0-0-0-0-0-0-0
400H	

Table B-16 DKP and the location of the center of mass for the small-scale cluster using every data point (with corrections for position errors). This data is for a geographic coordinate